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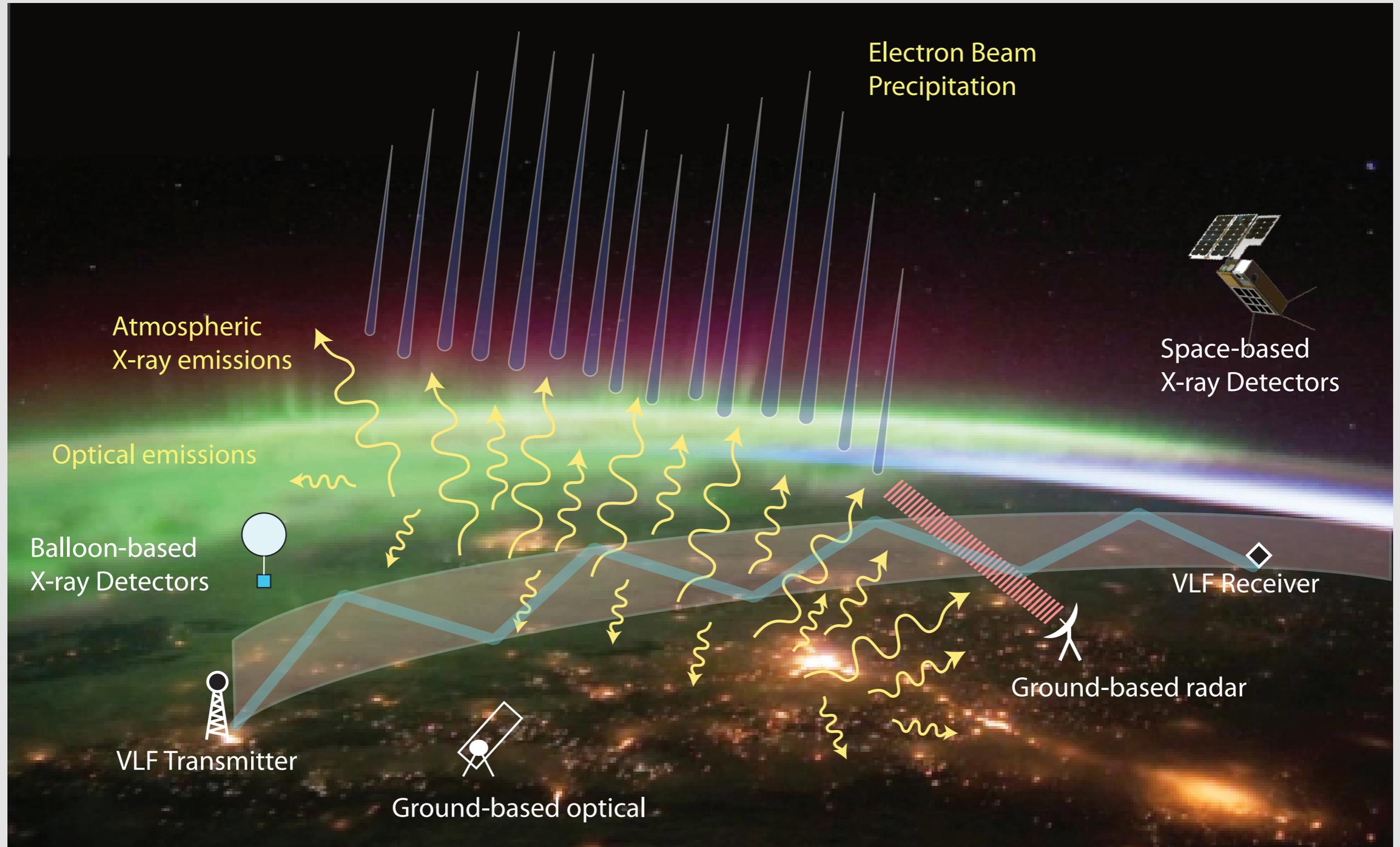
# Diagnostic of Relativistic Electron Beam Injection in the Upper Atmosphere

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With contributions from  
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**Rasoul Kabirzadeh (Stanford)**

# Atmospheric Signatures of Beam Precipitation



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# Outline

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## **1. Overview of secondary effects of precipitation**

1. Ionization, optical emissions, X-rays, chemistry
2. Associated diagnostic methods

## **2. Modeling framework to predict secondary signatures**

## **3. Beam simulation results**

1. Realistic beam parameters
2. Modeling scenario
3. Ionization signatures
4. Optical signatures
5. X-ray signatures
6. Chemical response

# Atmospheric Effects and Diagnostics

## ❖ Atmospheric Effects

❖ Ionization



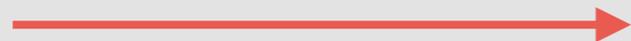
❖ Optical Emissions



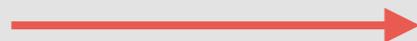
❖ X-ray emissions



❖ Chemistry



❖ Electrodynamics



## ❖ Diagnostics

❖ Ground-based radar

❖ Subionospheric VLF

❖ Ground-based or space-based optical detectors

❖ Space-based or balloon-based X-ray detectors

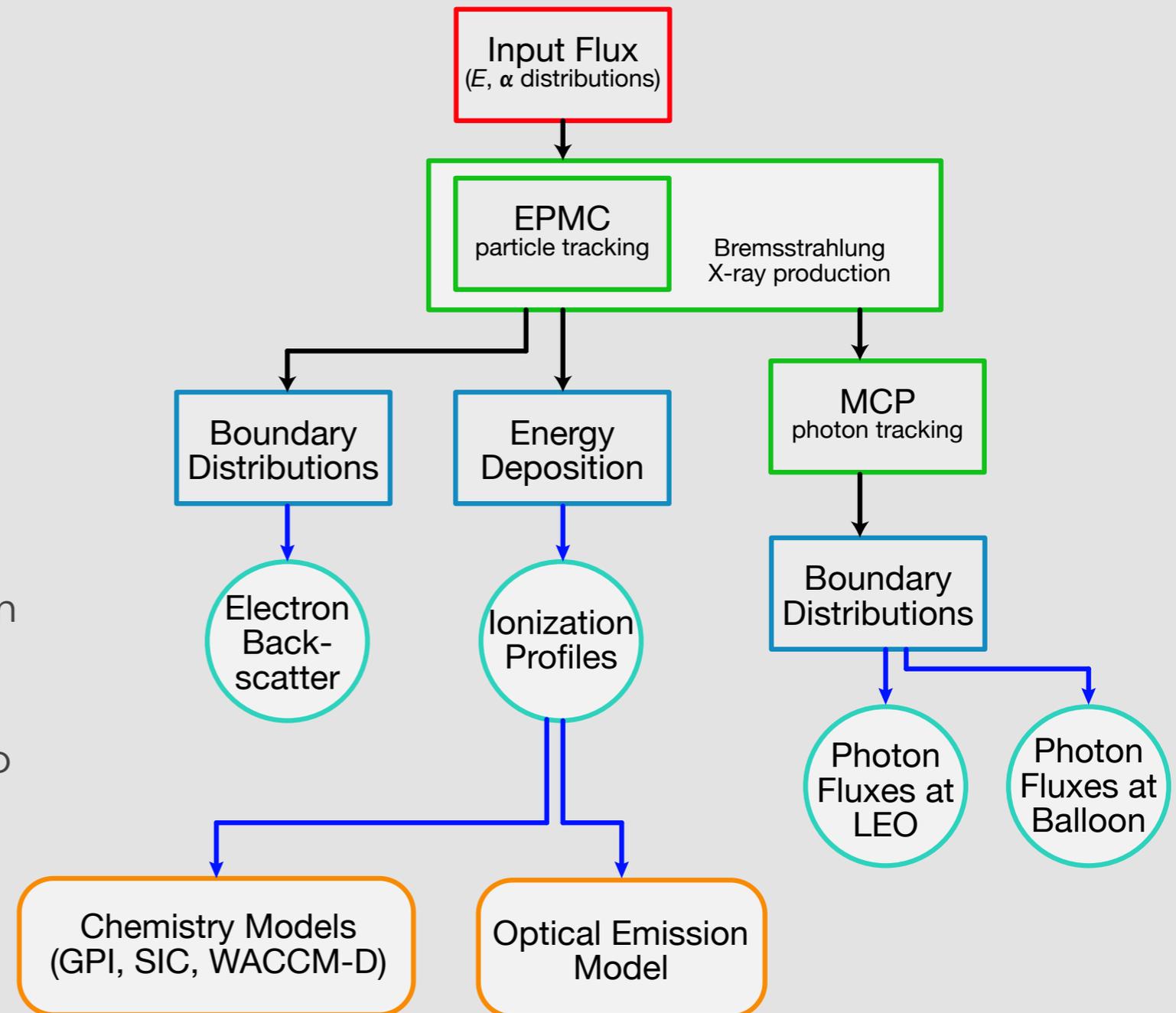
❖ NO<sub>x</sub> emissions (optical)

❖ TLEs?

# Atmospheric Effects: Forward Modeling

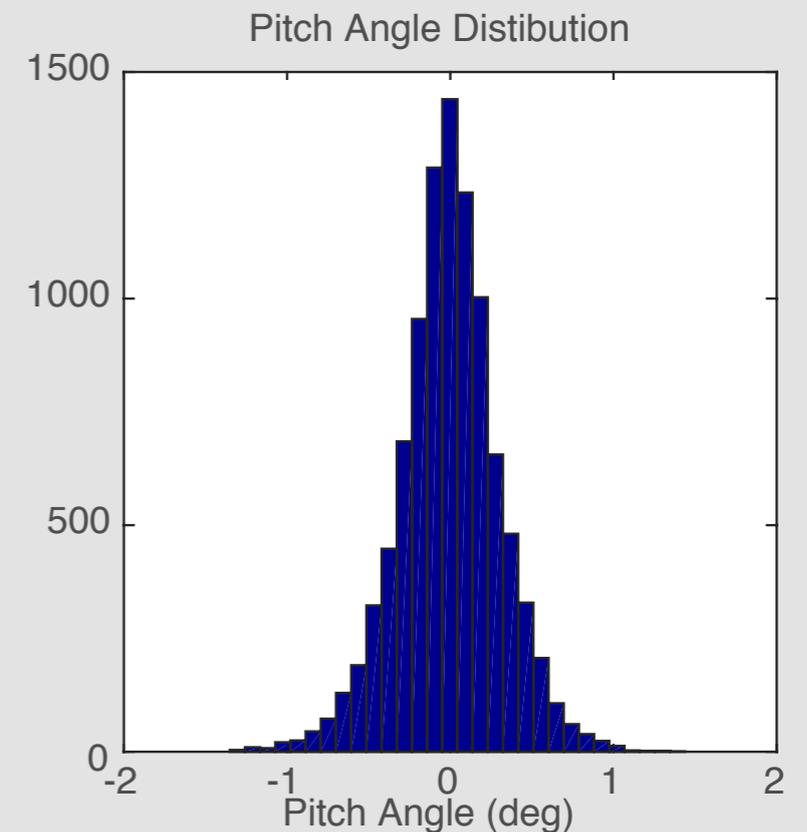
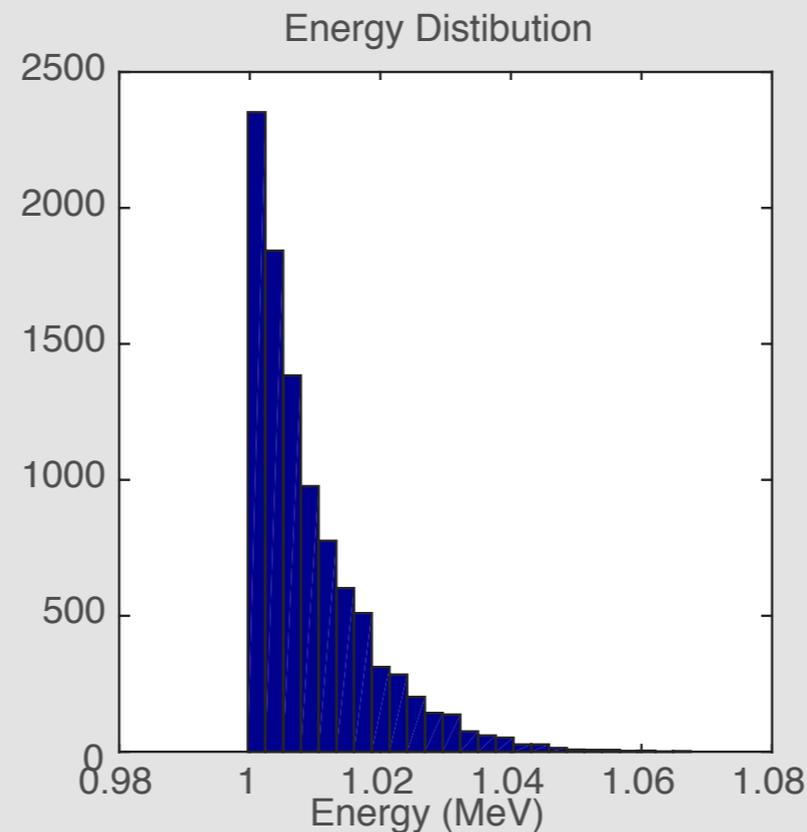
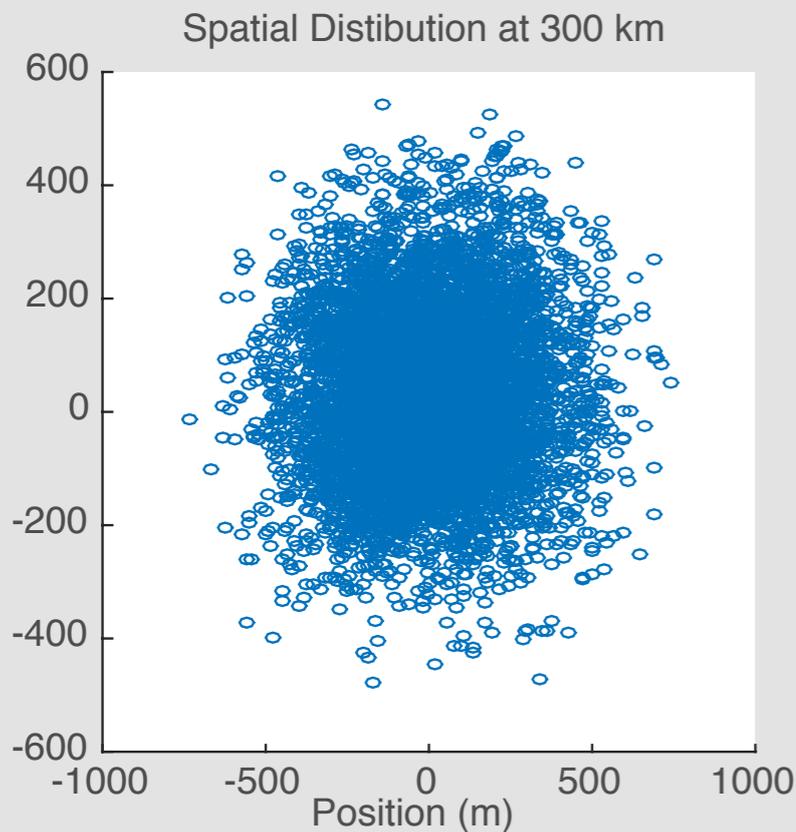
## ❖ We use the Electron Precipitation Monte Carlo (EPMC) model framework

- ❖ Initial electron distribution propagated through atmosphere
- ❖ Includes collisions, secondary ionization, energy loss, angular diffusion
- ❖ Calculates bremsstrahlung photon production probabilistically
- ❖ Photons separately propagated to determine observable fluxes
- ❖ Energy deposition profiles used for secondary effects: ionization, optics, chemistry



# Input Electron Distributions

- ❖ We simulate a finite number of electrons, say  $10^5$  or  $10^6$ 
  - ❖ Energy, pitch angle, and spatial distribution given by PPPL simulation outputs
- ❖ These represent a larger number of total electrons; outputs scale linearly
  - ❖  $10 \text{ mA} \times 500 \mu\text{s} = 3 \times 10^{13}$  total electrons in one pulse. At 1 MeV, that's 5 J per pulse

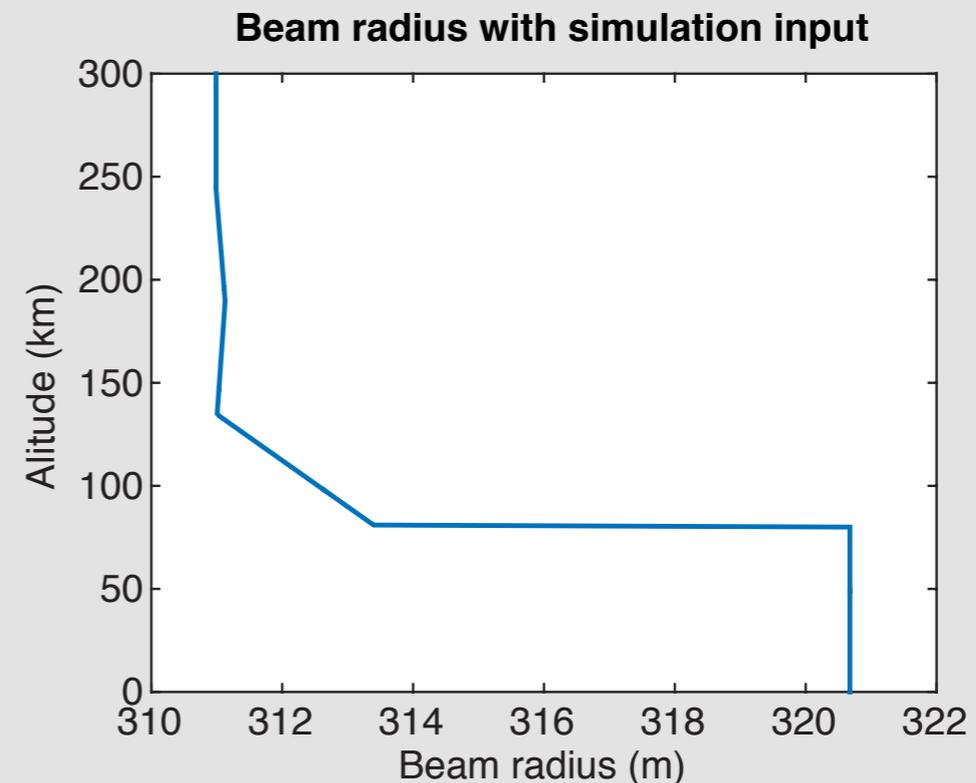
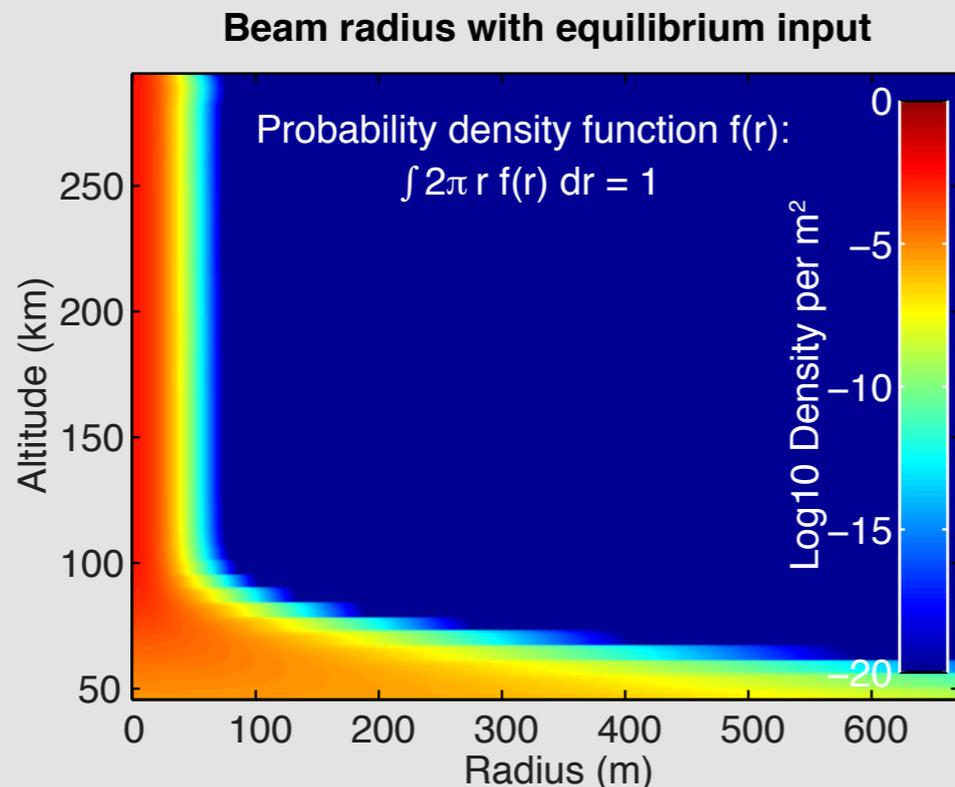


# Tracking the beam radius

- ❖ We must assume or simulate an initial beam size / distribution at the top of the atmosphere
  - ❖ Assume: use the equilibrium radius, determined by beam energy, divergence, and properties of region (see Marshall et al, 2014)
  - ❖ Simulate: determined by beam propagation simulations from PPPL (previous slide)
- ❖ During collisional interaction with the atmosphere, the distribution changes; need to track it to determine ionization density
  - ❖ We track electron distribution every 10 us and determine a beam radius

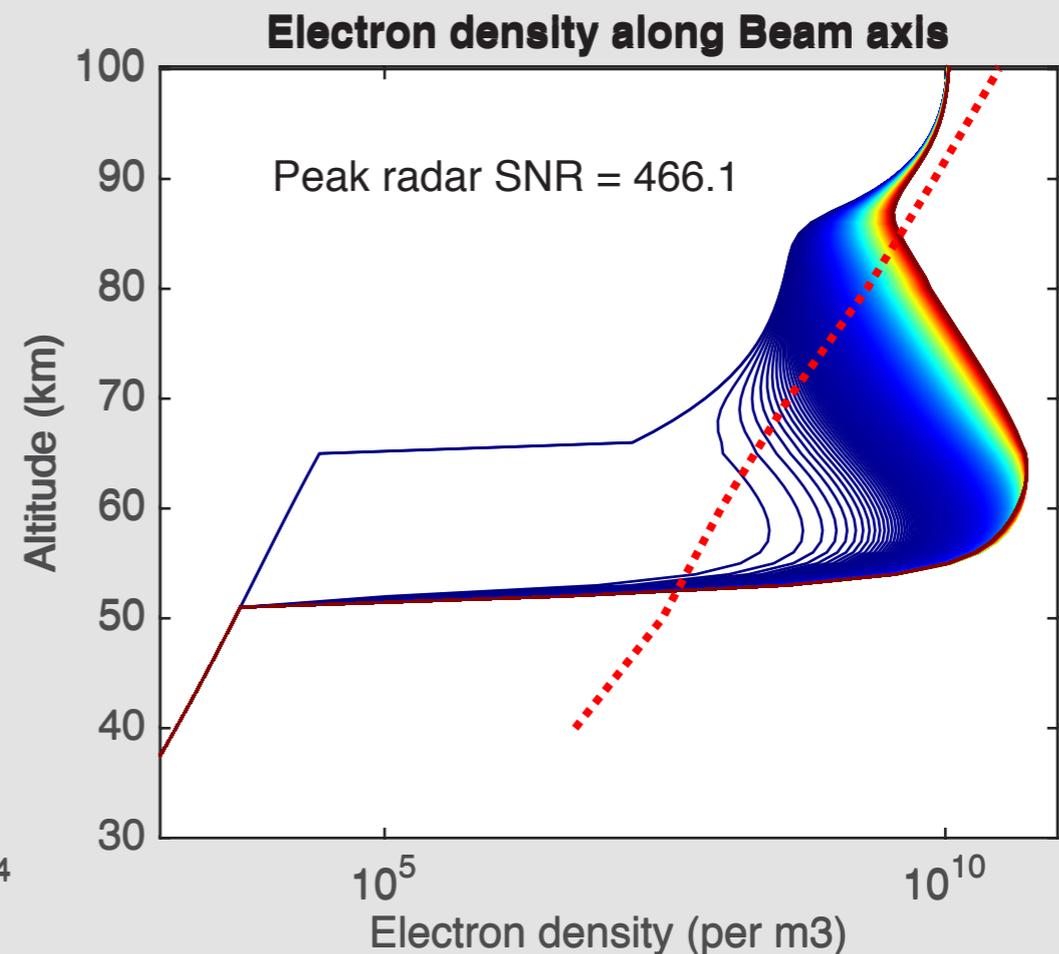
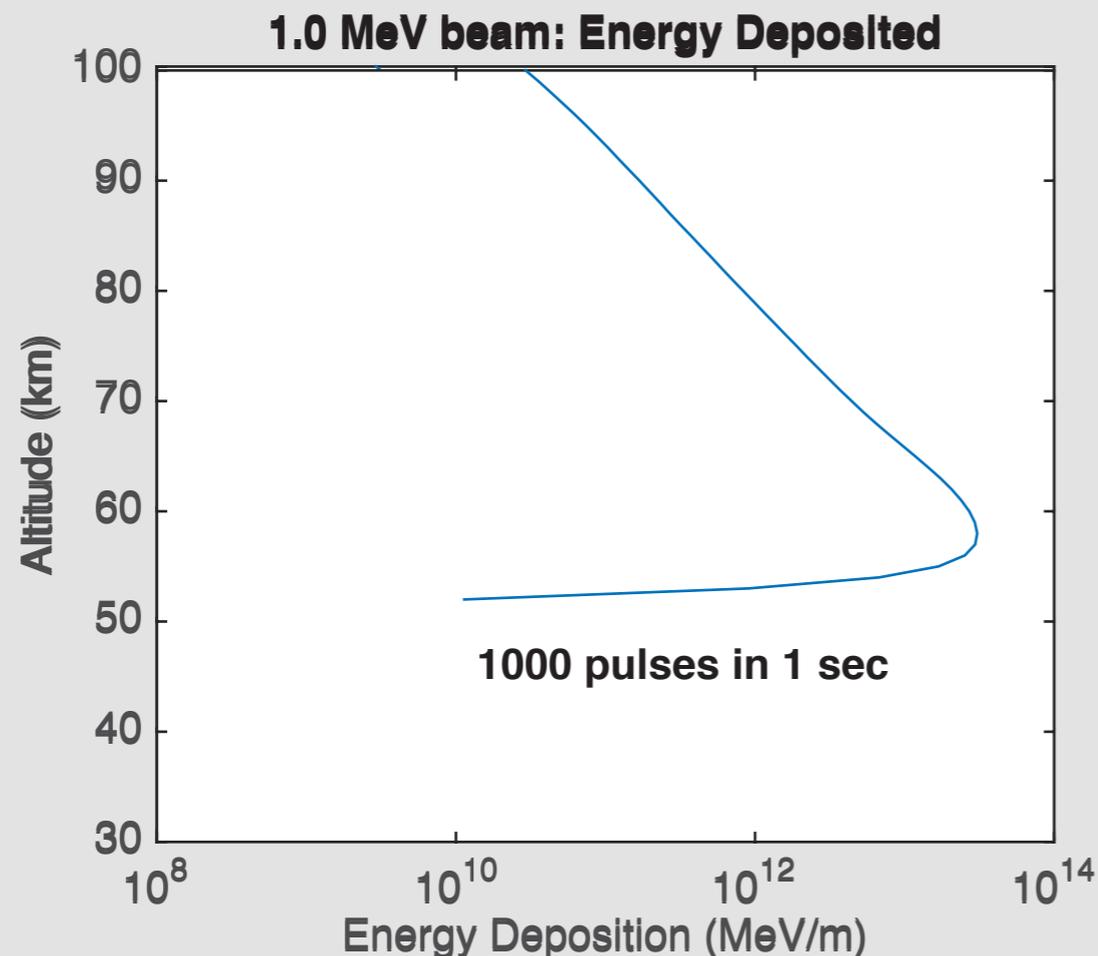
**Table 2.** Beam Equilibrium Radius for Given Beam Electron Energies

Electron energy (MeV)	0.5	1	2	5	10	20
$\beta$	0.8630	0.9412	0.9791	0.9957	0.9988	0.9997
$\gamma$	1.98	2.96	4.92	10.79	20.59	40.17
Beam radius (m)	1.2	2.0	3.4	7.6	14.6	28.6



# Energy Deposition and Electron density

- ❖ Given an input energy / pitch angle distribution, EPMC determines the energy deposition profiles for a single pulse. Ionization follows from 1 pair per 35 eV.
  - ❖ Use D-region ion chemistry models to determine electron density disturbance
    - ❖ Below uses 5-species GPI chemistry model [*Glukhov et al, 1992; Lehtinen and Inan, 2009*]
  - ❖ Wish to determine signatures in radar and VLF

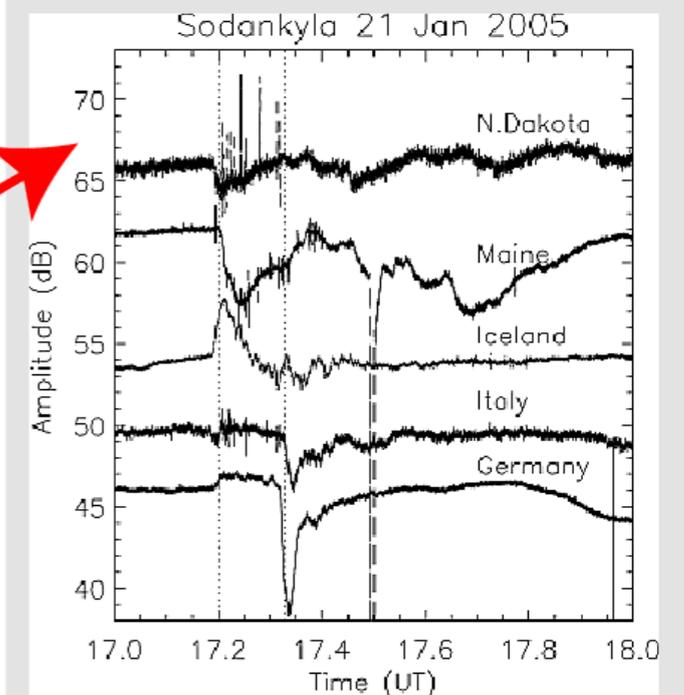
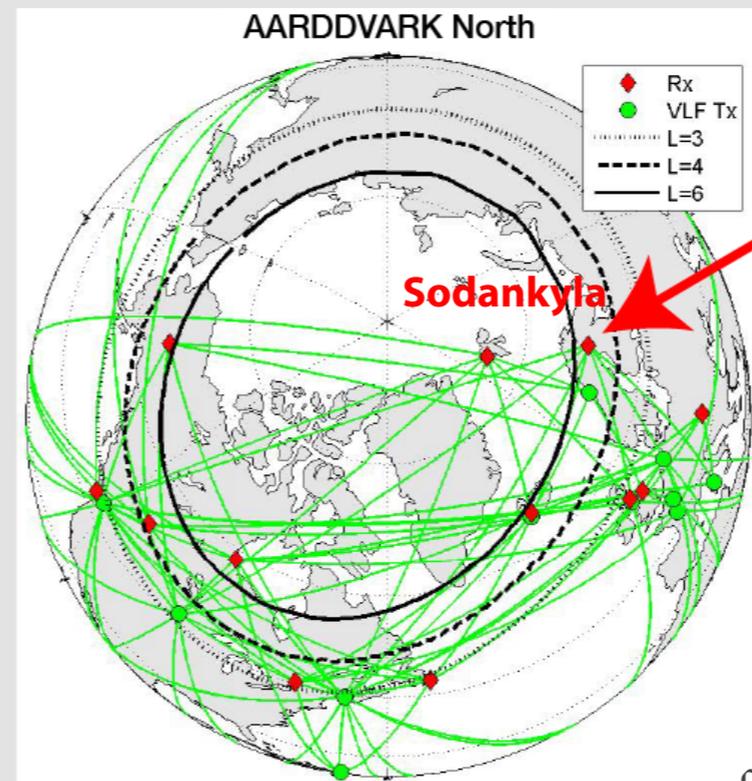


# VLF subionospheric remote sensing (VLF-SRS)

- ❖ VLF transmitter signals, broadcast by US Navy and others, are very sensitive to variations in the D-region
- ❖ Most operate in 15–40 kHz range; transmit ~100 kW – 2 MW
- ❖ Well-placed VLF receivers monitoring a range of transmitters can form a network of D-region remote sensing (e.g., AARDDVARK)

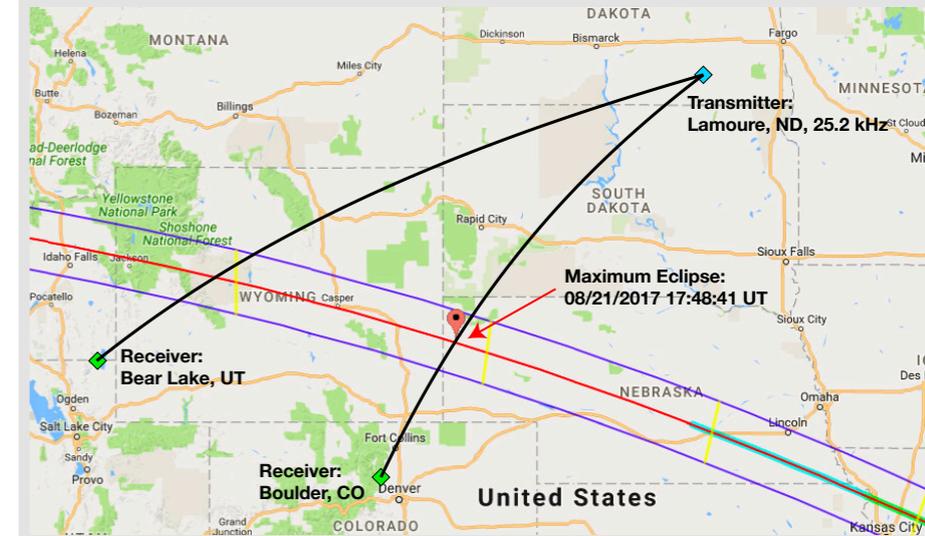
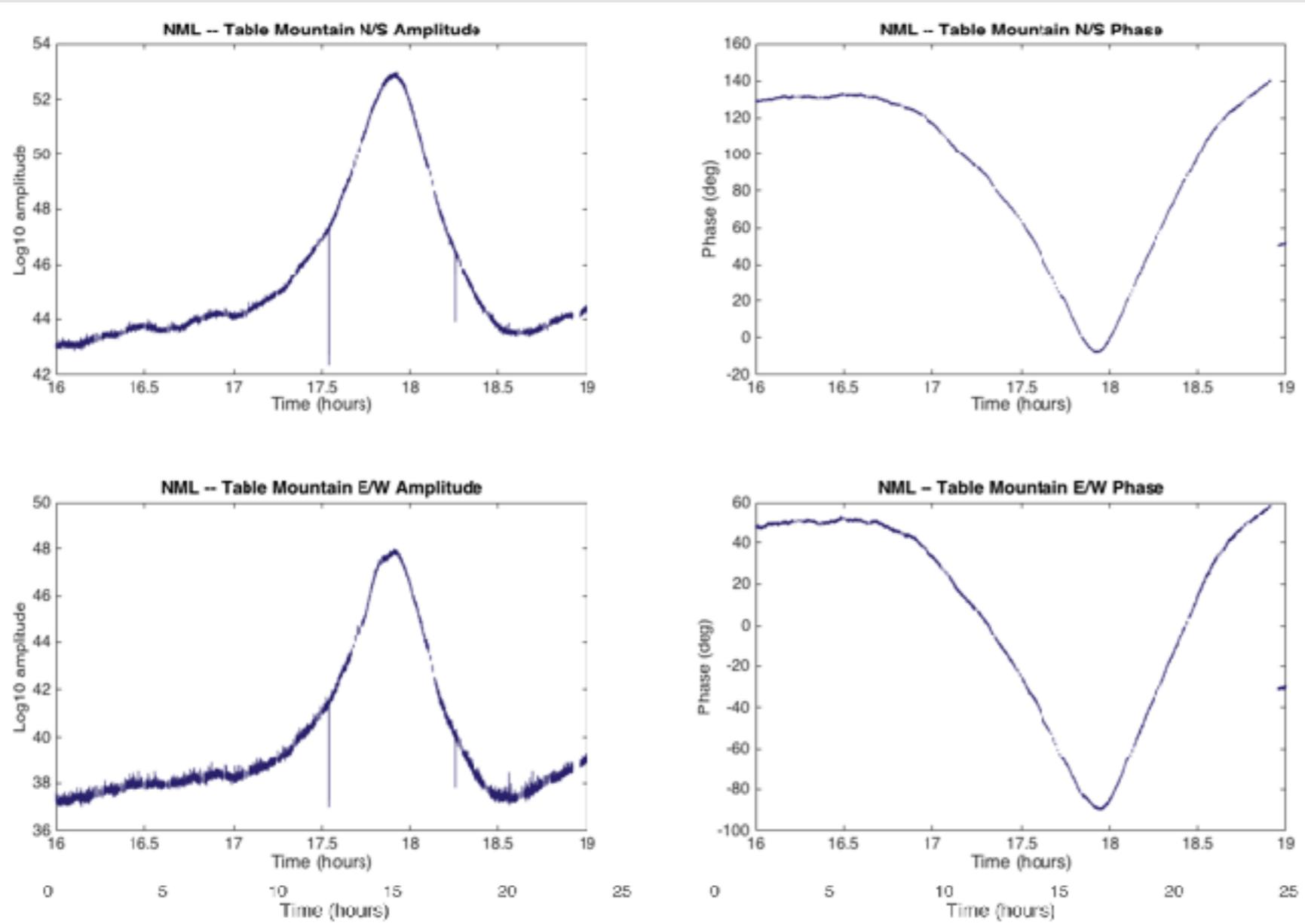


Table Mountain, Boulder, CO



from Clilverd *et al* [2009]

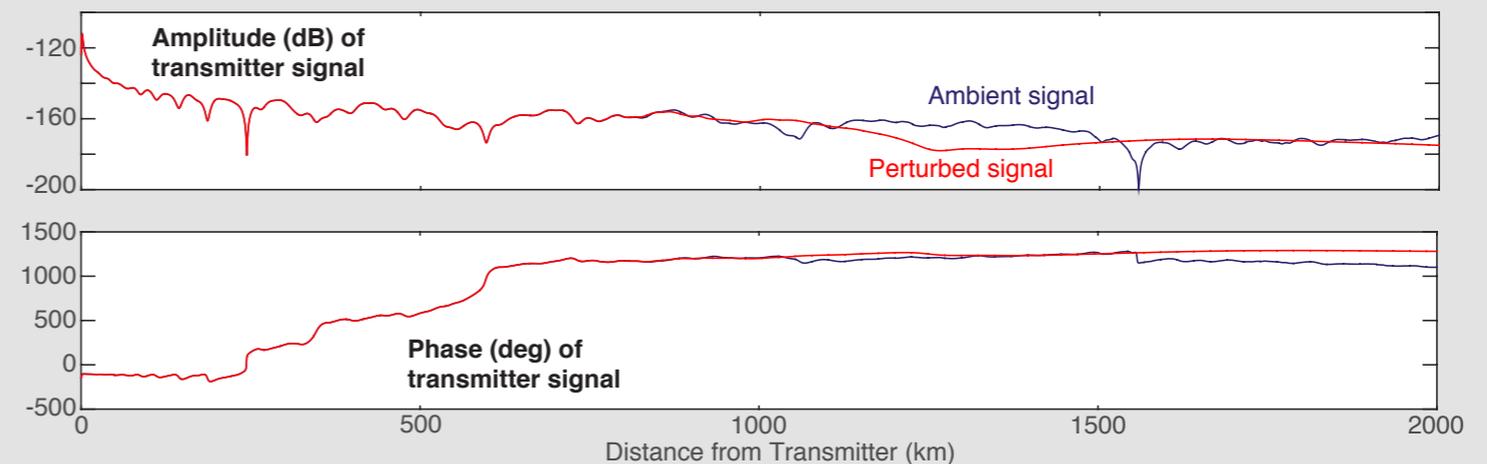
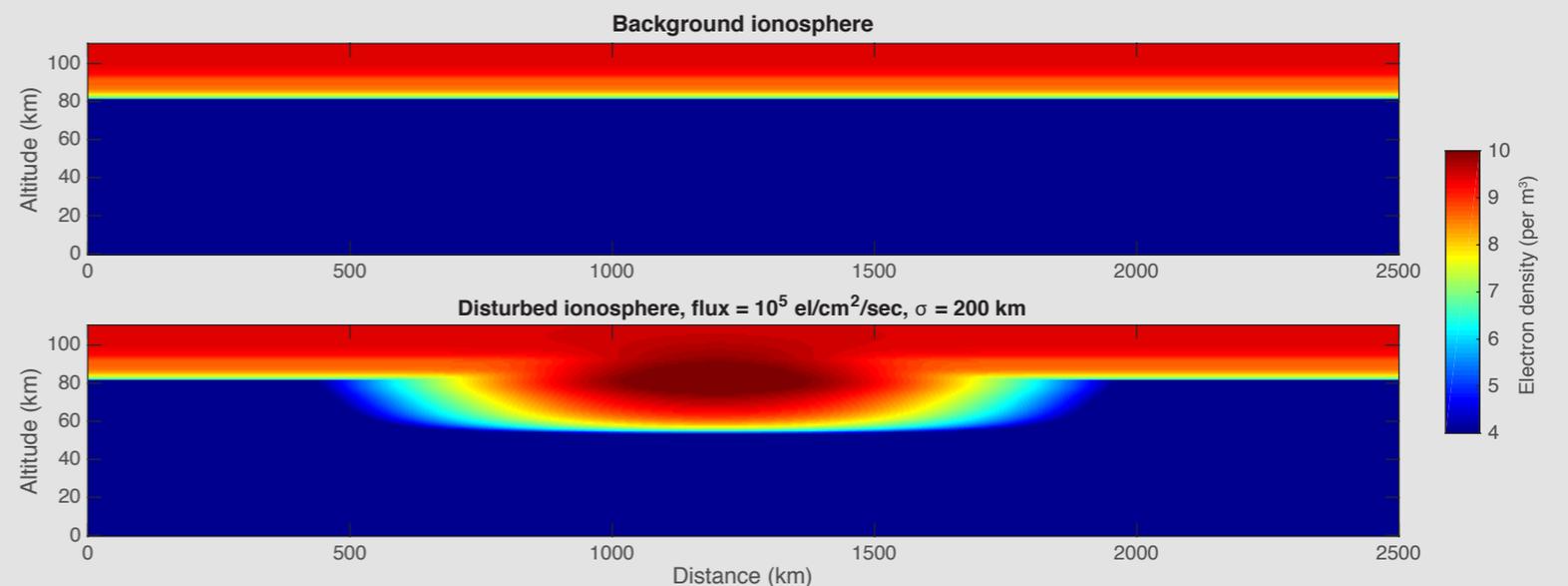
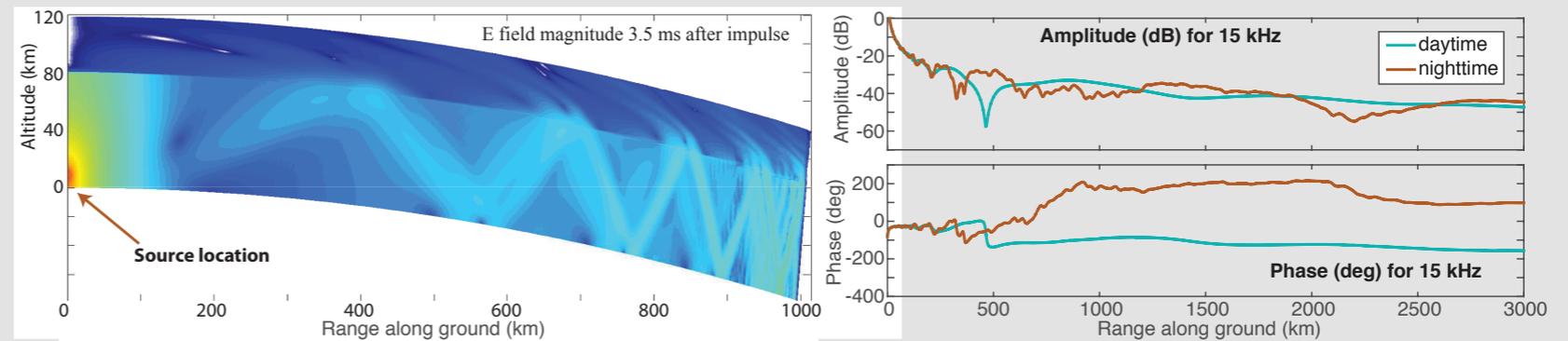
# Example data from Table Mountain



Rule of thumb: we can detect perturbations of  $\sim 0.1$  dB amplitude,  $\sim 1$  deg phase

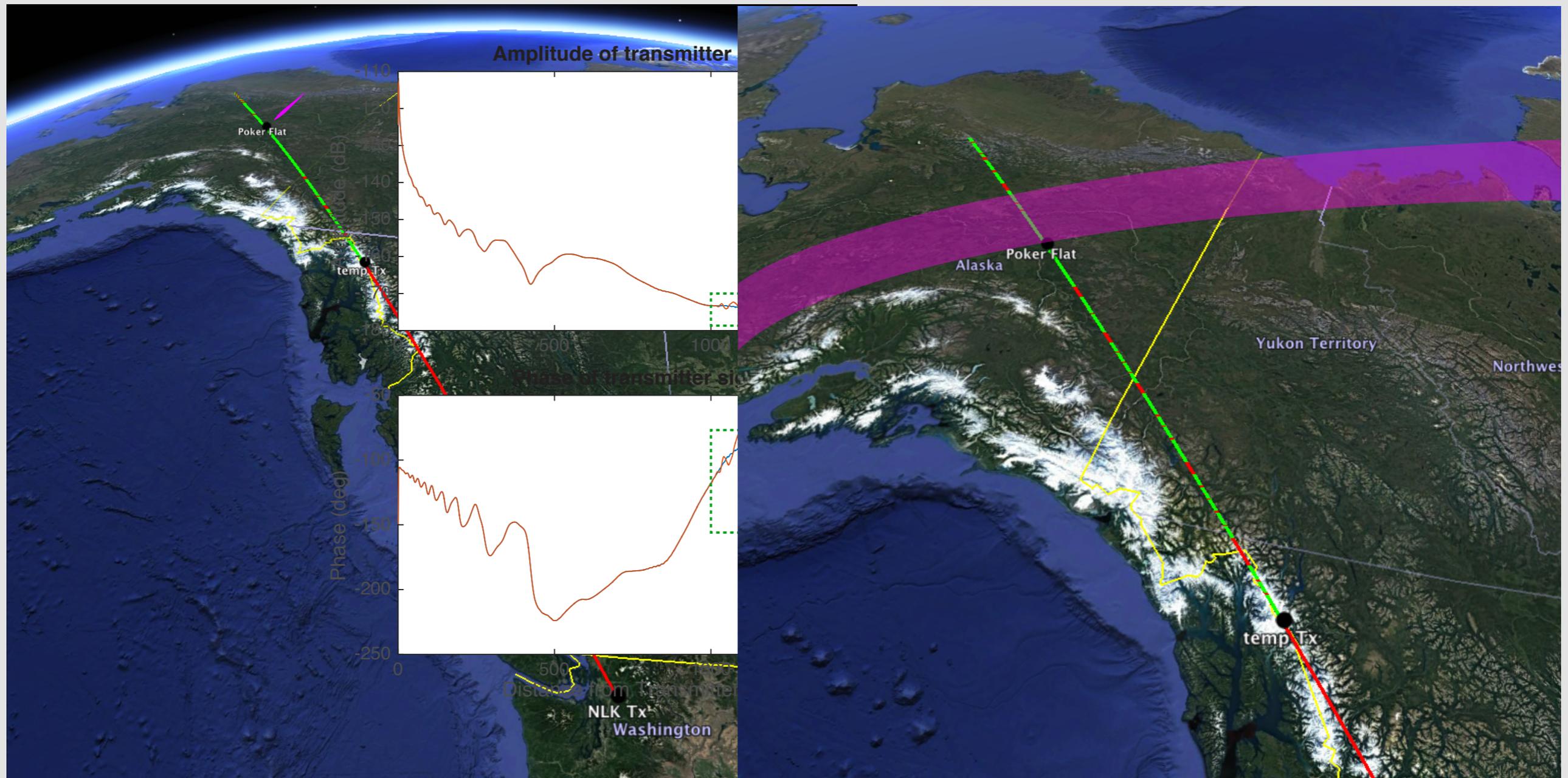
# Modeling VLF signatures of Precipitation

- ❖ Electron density perturbations are used as input to 2D Finite-Difference Time-Domain (FDTD) model [Marshall, 2012, JGR]
- ❖ FDTD model used to simulate amplitude and phase at locations along the ground for wide range of frequencies
- ❖ Model with and without precipitation; subtract to determine perturbation
- ❖ Use measure of “average” perturbation for correlation studies [Marshall and Snively, 2014; Kabirzadeh et al, 2017]



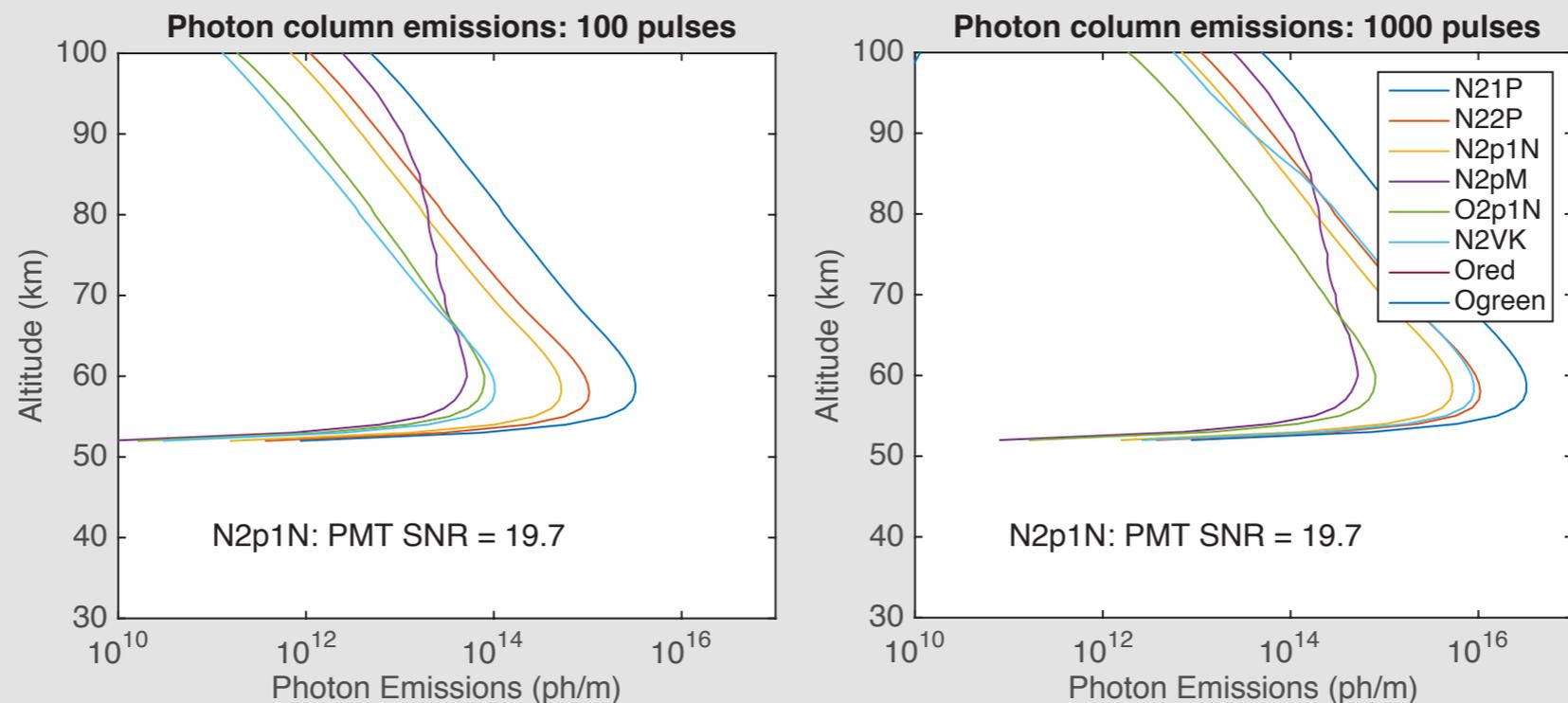
# Beam VLF perturbation: first test

- ❖ Input the 1000 pulse / 1 sec electron density disturbance into the FDTD model as a “disturbed” ionosphere
- ❖ Compare simulated Amplitude / phase with ambient case



# Optical emissions

- ❖ We use basic auroral optical physics [Vallance Jones, 1974] to calculate optical emission rates given ionization rates
  - ❖ Include quenching, cascading, lifetimes
- ❖ Ionization rates result of photon emission rates for each band of interest; integrate over total pulse duration to get total photons



- ❖ Next, propagate photons in  $4\pi$  steradians and include atmospheric transmission as function of wavelength; determine photon flux ( $\text{ph}/\text{m}^2$ ) reaching ground location

# Optical sanity check

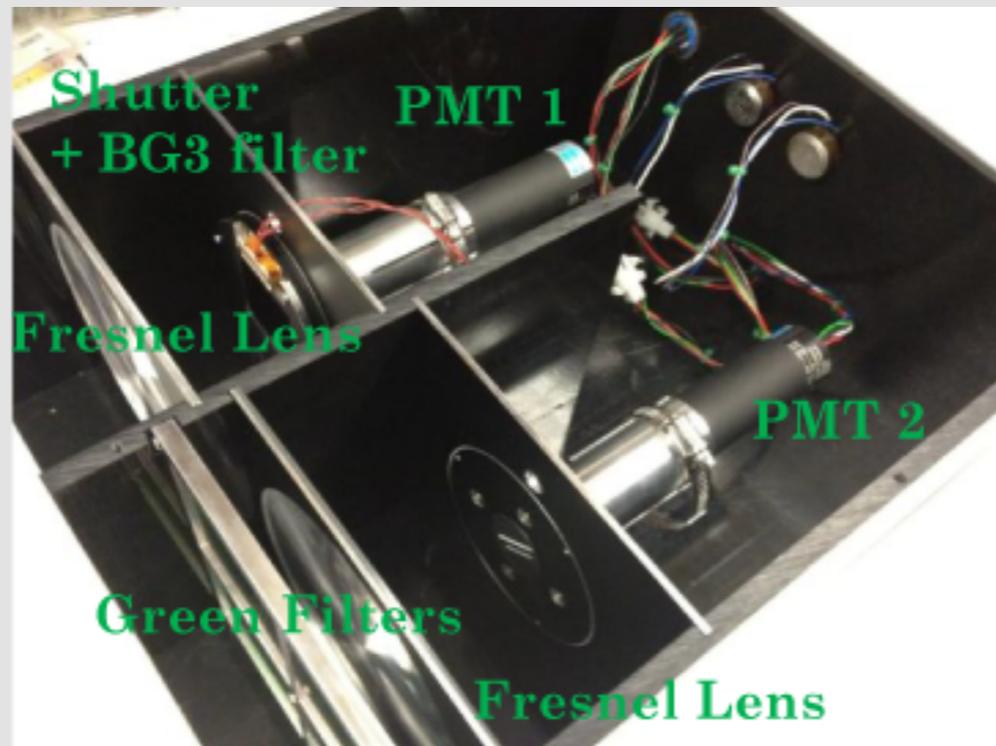
- ❖ **For 100 J injected into the atmosphere:**
  - ❖ Emitted as N<sub>2</sub> 1st positive photons: ~**2.2 J**
  - ❖ N<sub>2</sub> 2nd positive: ~**1.1 J**
  - ❖ N<sub>2</sub> Vegard-Kaplan: ~**1.0 J**
  - ❖ N<sub>2</sub><sup>+</sup> Meinel: ~**0.1 J**
  - ❖ N<sub>2</sub><sup>+</sup> 1N: ~**0.6 J**
  - ❖ O<sub>2</sub><sup>+</sup> 1N: ~**0.06 J**
  - ❖ O green line: ~**0.7 uJ**
  - ❖ O red line: ~**0.3 nJ**
- ❖ Total optical emissions = ~**5% of injected energy, consistent with auroral estimates of energy partitioning** [e.g., Vallance Jones, 1974]
- ❖ For 100 J injected, **1.2 x 10<sup>18</sup> photons** are emitted in N<sub>2</sub><sup>+</sup> 1N band system (0.6 J)
- ❖ When accounting for spreading over  $4\pi r^2$ , from each altitude, and considering atmospheric attenuation, **1.2 x 10<sup>7</sup> photons/m<sup>2</sup>** reach the ground
- ❖ Now, we can use any detection system we want to determine expected signal
  - ❖ Example: filter covering 380 to 392 nm → **factor of 0.27**
  - ❖ 2" lens aperture → **6 x 10<sup>4</sup> photons hit the lens**

# Optical Detection: PMT or All-sky

- ❖ Integrate photon flux to ground; use instrument parameters to estimate expected signal and SNR
- ❖ **Difficulty:** isolating RB precipitation from aurora!

## PMT features:

f/0.5 lens  
6" aperture  
10 nm filter  
28 mm PMT

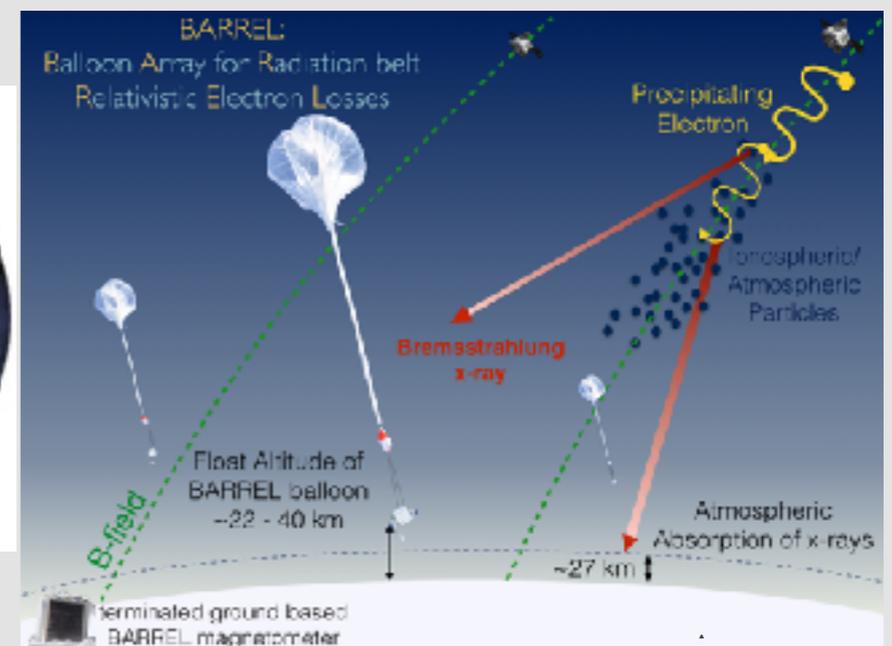
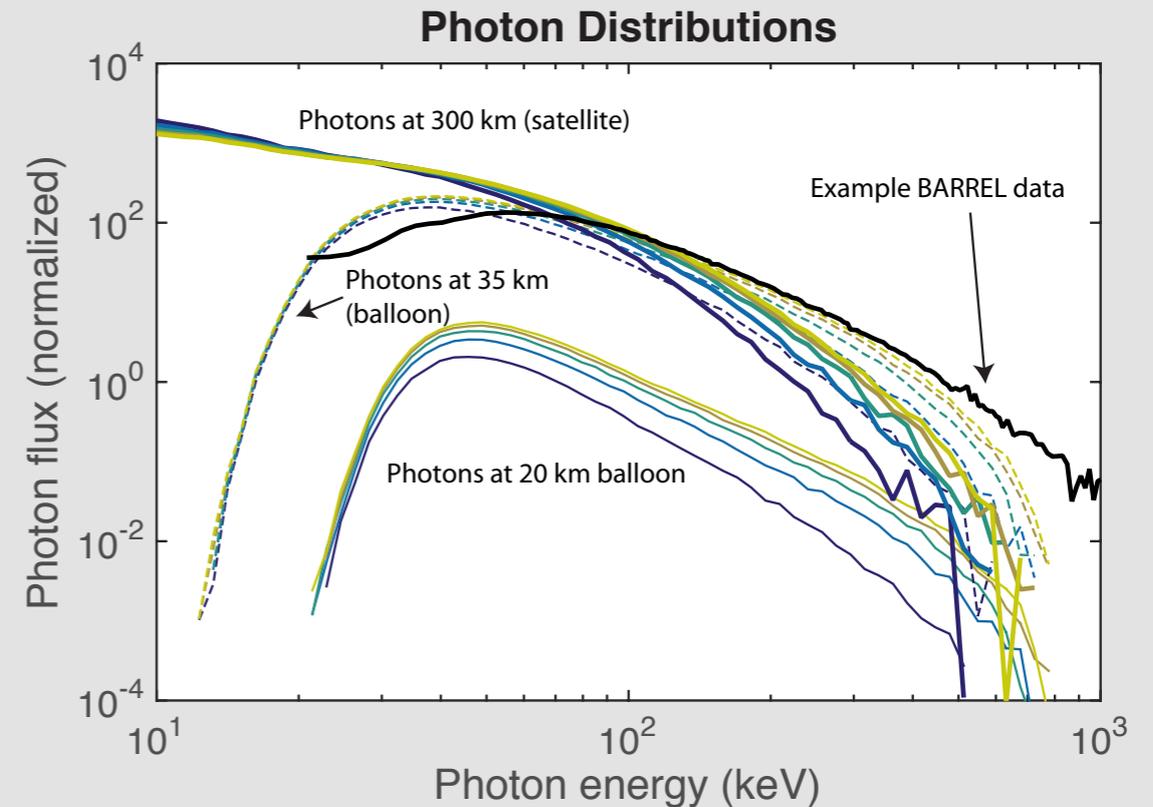


- ❖ **PMT SNR: ~20**
  - ❖ independent of number of pulses, because we assume 1 kHz sampling
  - ❖ Integration in time will help, of course
- ❖ **All-sky SNR: ~50**
  - ❖ assuming 0.5 second integration
  - ❖ 500 J injected over 0.5 seconds; 70% detector QE; shot-noise limited



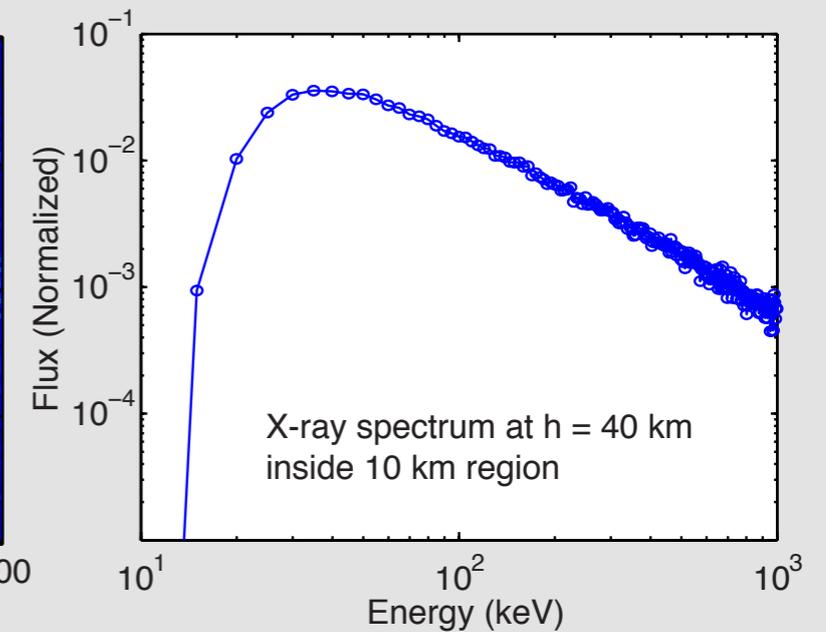
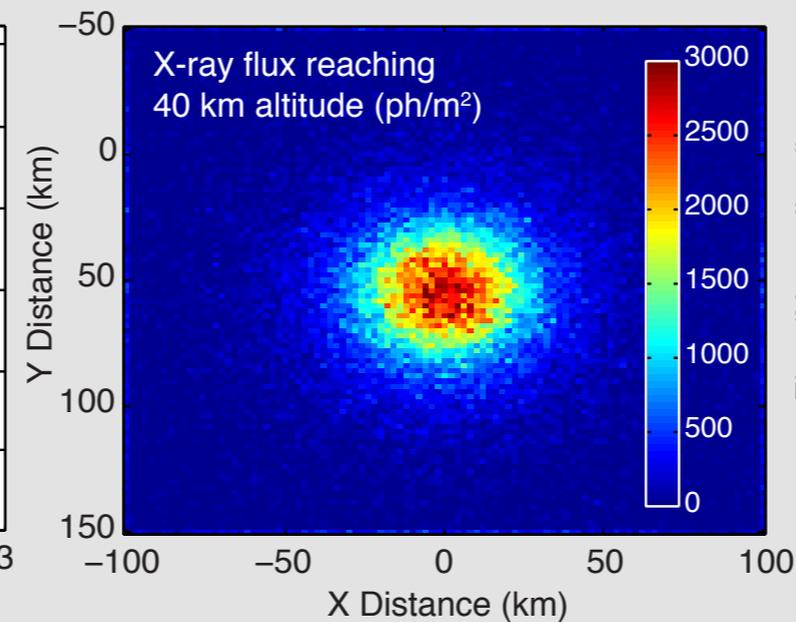
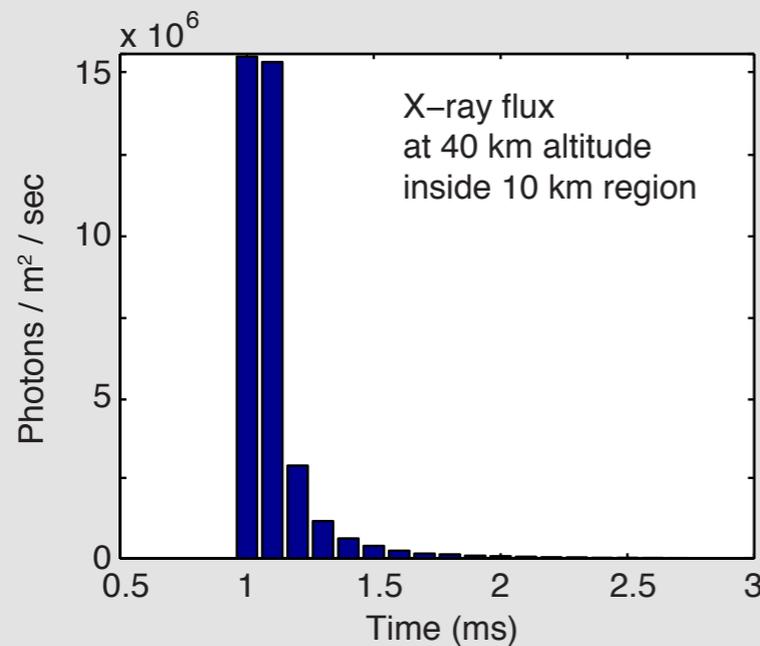
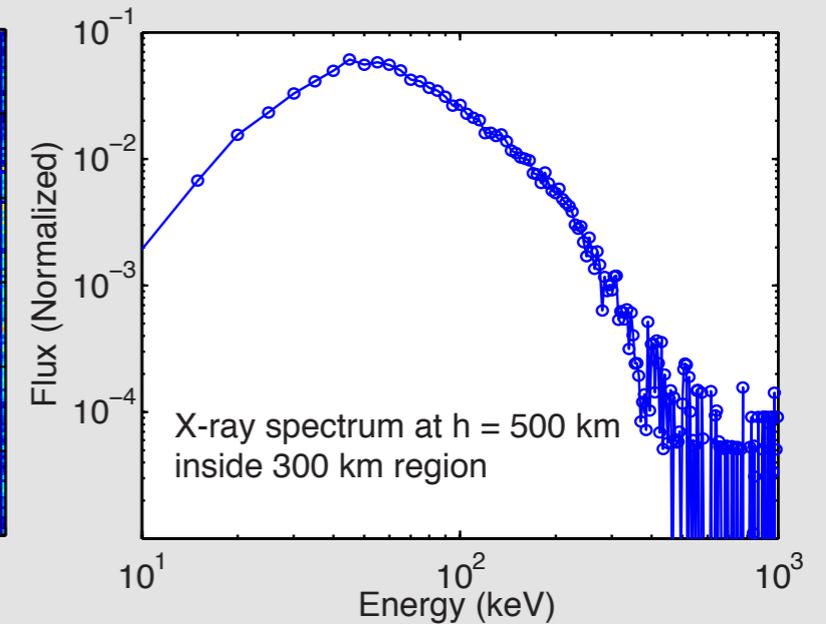
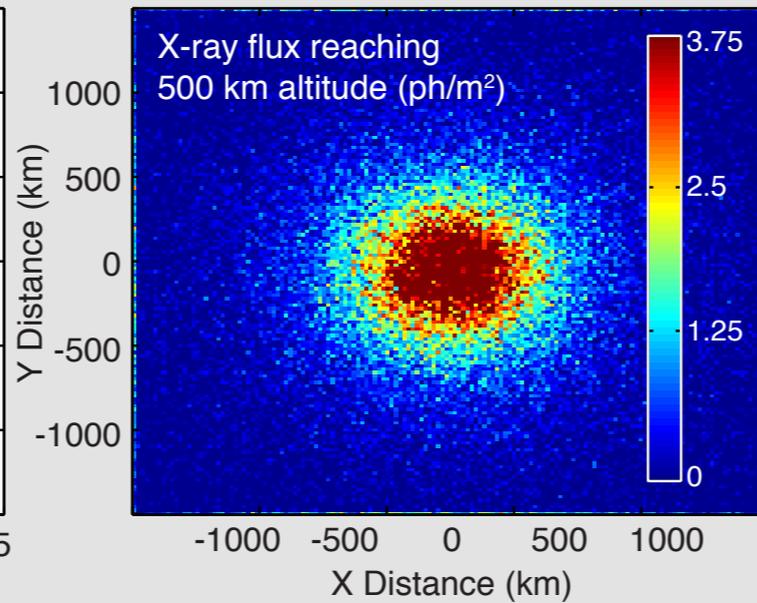
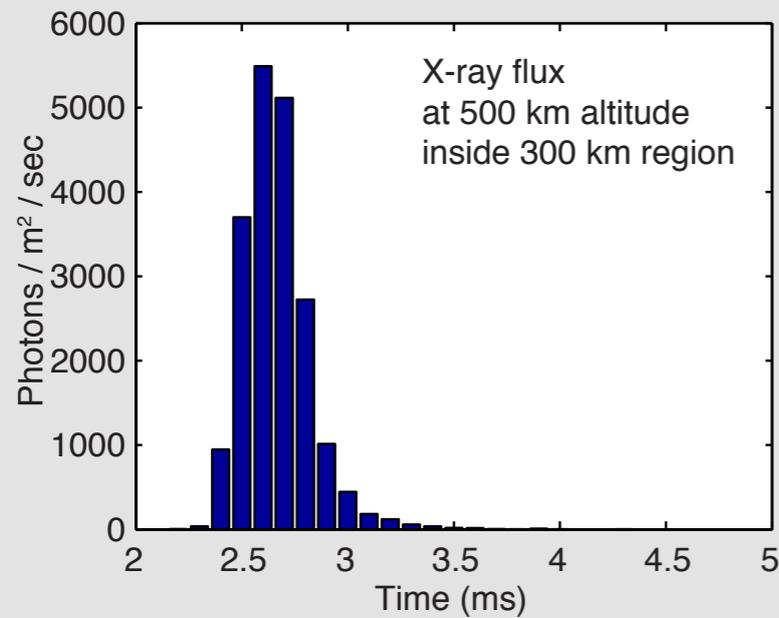
# X-ray emissions by bremsstrahlung

- ❖ At each time step of the electron propagation, bremsstrahlung photons are produced probabilistically
  - ❖ Given statistically-determined energy and direction relative to parent electron
- ❖ Photons are propagated in atmosphere, and we consider Compton scattering, photoelectron production, and pair production
- ❖ Ultimately, energy spectrum of photons is collected at observing locations (balloon or satellite)



# X-ray fluxes from a beam input

5 MeV beam, 10 mA, 500 us,  $3 \times 10^{13}$  total electrons, field-aligned

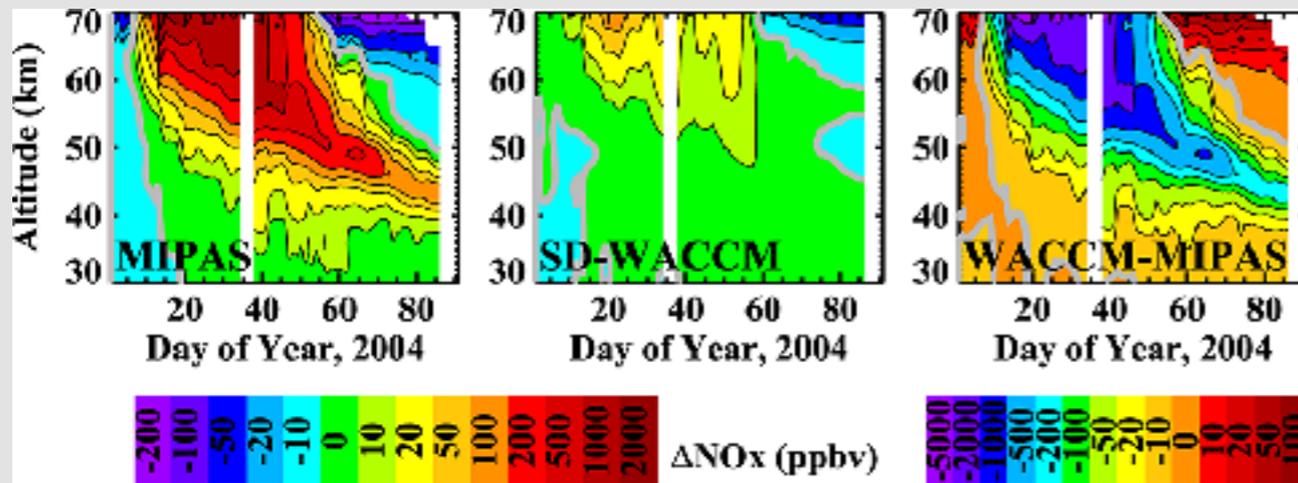


Expect lower photon flux by factor of ~5 or more for 1 MeV electrons

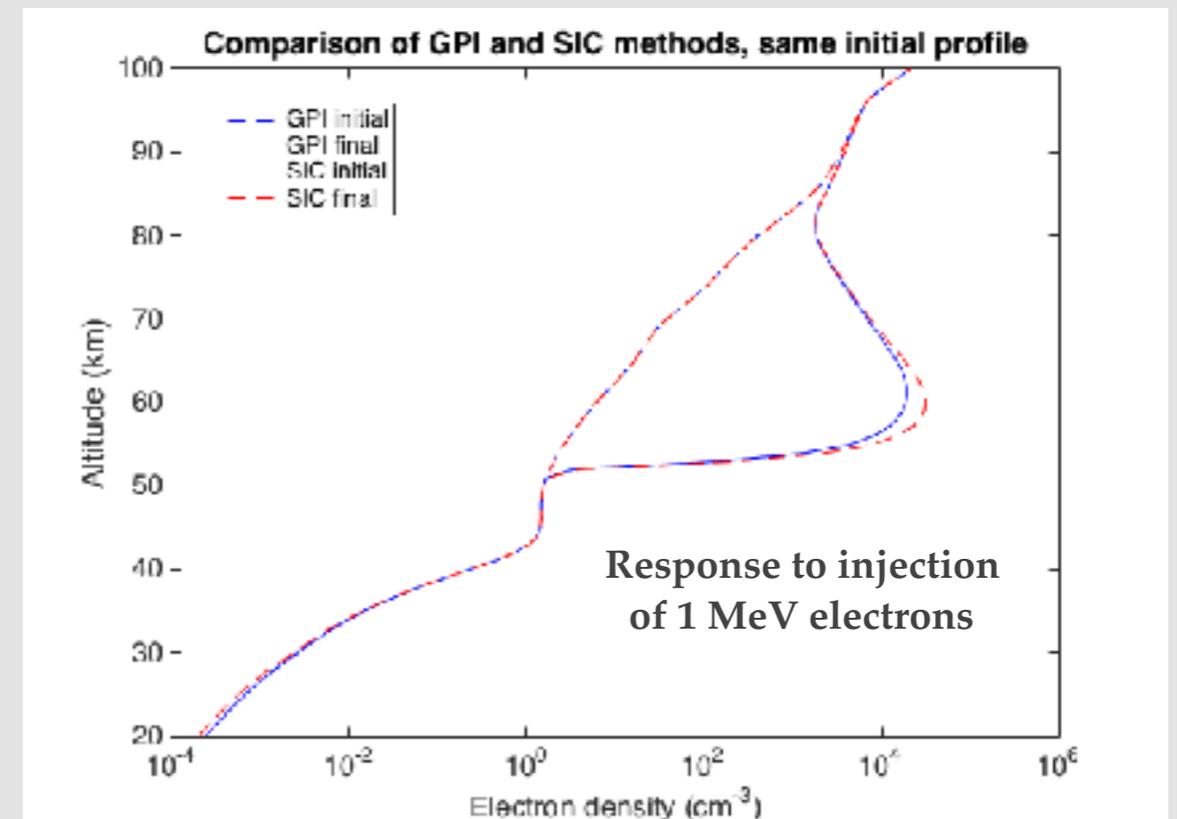
# Chemical Effects in the Atmosphere

- ❖ Chemical effects in atmosphere include NO<sub>x</sub> / HO<sub>x</sub> production and O<sub>x</sub> destruction
  - ❖ NO<sub>x</sub> descends to stratosphere and causes further O<sub>x</sub> destruction
- ❖ Precipitating fluxes / spectra important to quantify chemical effects
- ❖ Model / data discrepancy likely caused by incorrect flux / spectrum input

	About	Advantages	Disadvantages
GPI	Stanford; 5 or 6 species; Matlab code	Matlab code; time evolution; fast	only 1D; no detailed minor species (NO <sub>x</sub> , etc)
SIC	Sodankyla; hundreds of species	time evolution; fast; hundreds of species and reactions	only 1D; availability*
WACCM-D	NCAR	3D+time; horizontal transport;	slower (still pretty fast though!); fewer species / reactions than SIC

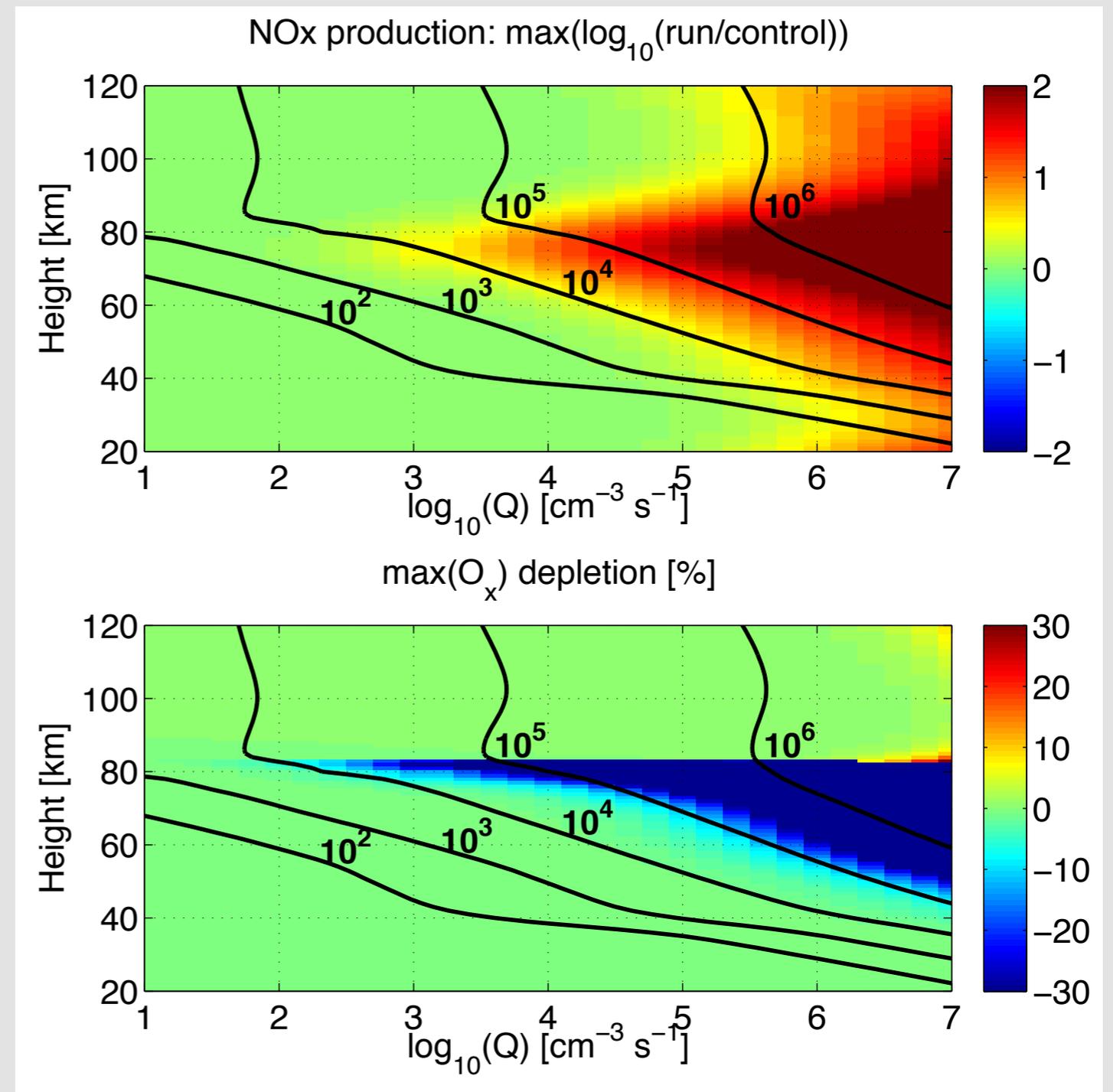


from *Randall et al* [2016]



# Chemistry modeling

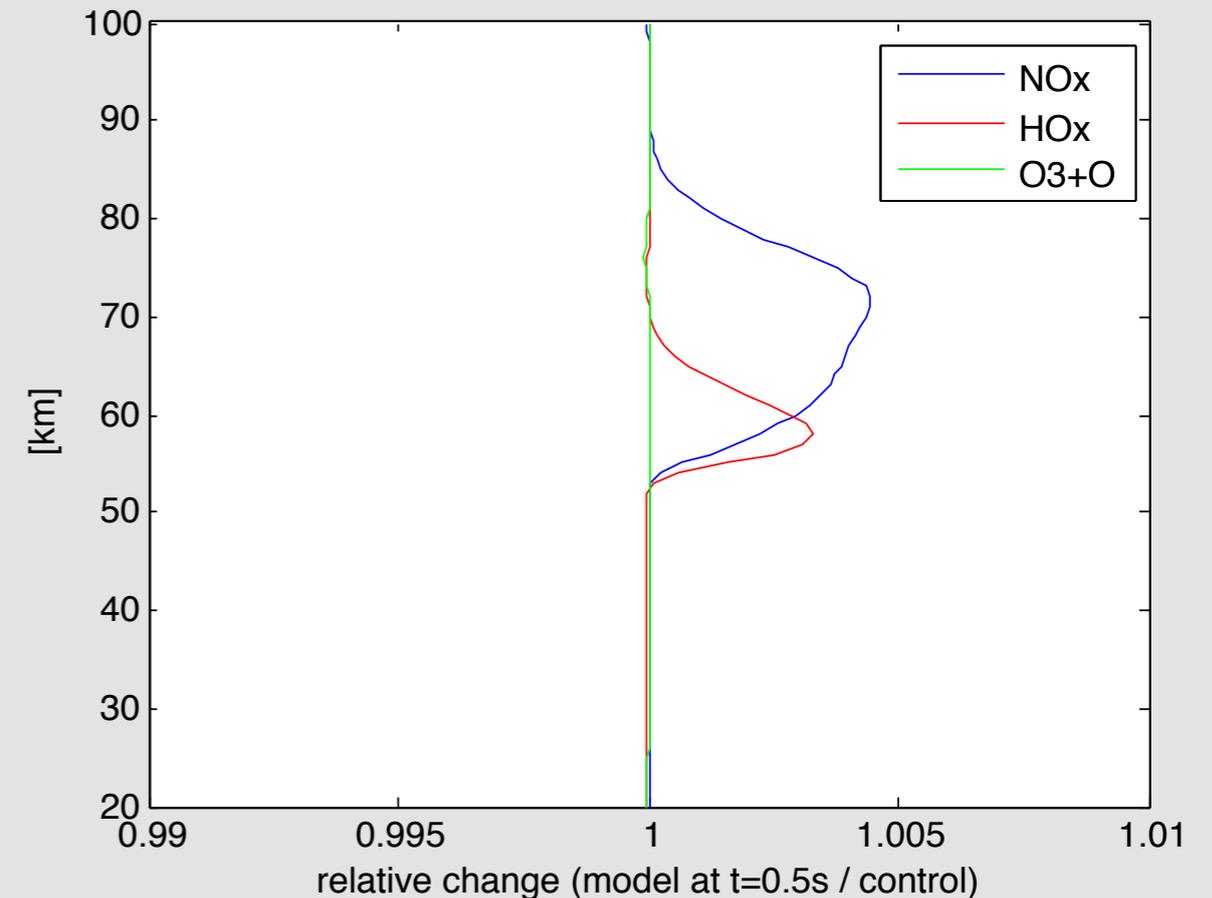
- ❖ Lookup table generated using SIC model:
  - ❖ provides NO<sub>x</sub> and O<sub>x</sub> enhancements at each altitude, for range of ionization rates
  - ❖ Generated for nighttime, winter atmosphere over Poker Flat, Alaska (~65 N, 147 W), site of PFISR radar
  - ❖ Results depend on background profiles and duration of forcing (30 minutes here)



*work conducted by Antti Kero, SGO*

# Chemistry Effects of 100 pulses in 0.5 sec

- ❖ Simulate 100 pulses of 5 J each, every 5 ms\* (earlier they were every 1 ms)
  - ❖ For chemical effects, timing at this scale is not important; total ionization is key
- ❖ NO<sub>x</sub> and HO<sub>x</sub> enhancements are relatively small (0.5% increase)
- ❖ Ox effects are negligible
- ❖ Note effects increase roughly linearly with total ionization
  - ❖ More pulses, more energy → more chemistry

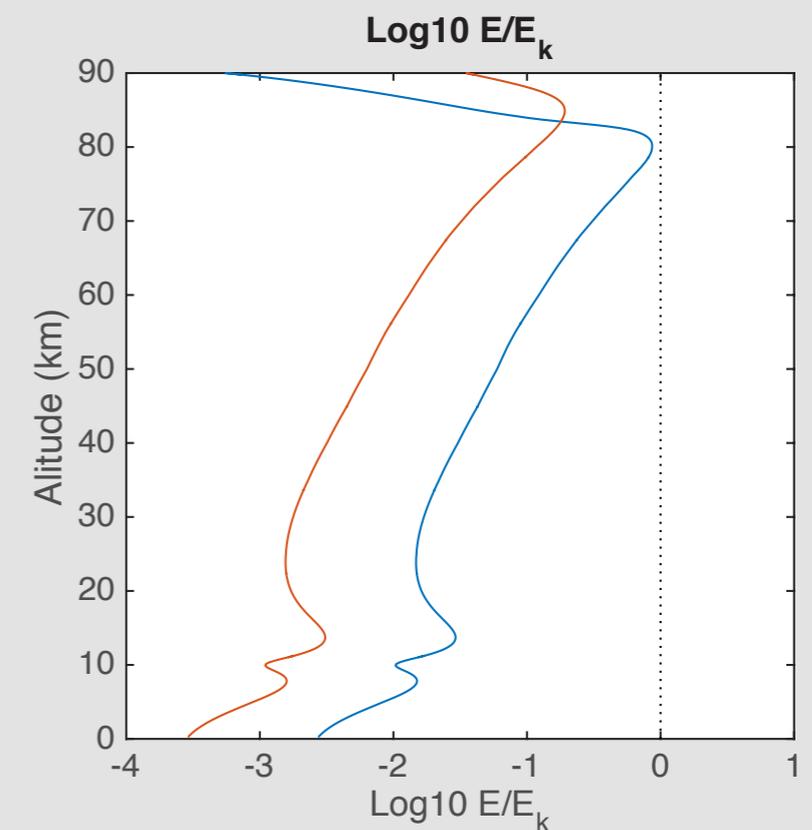
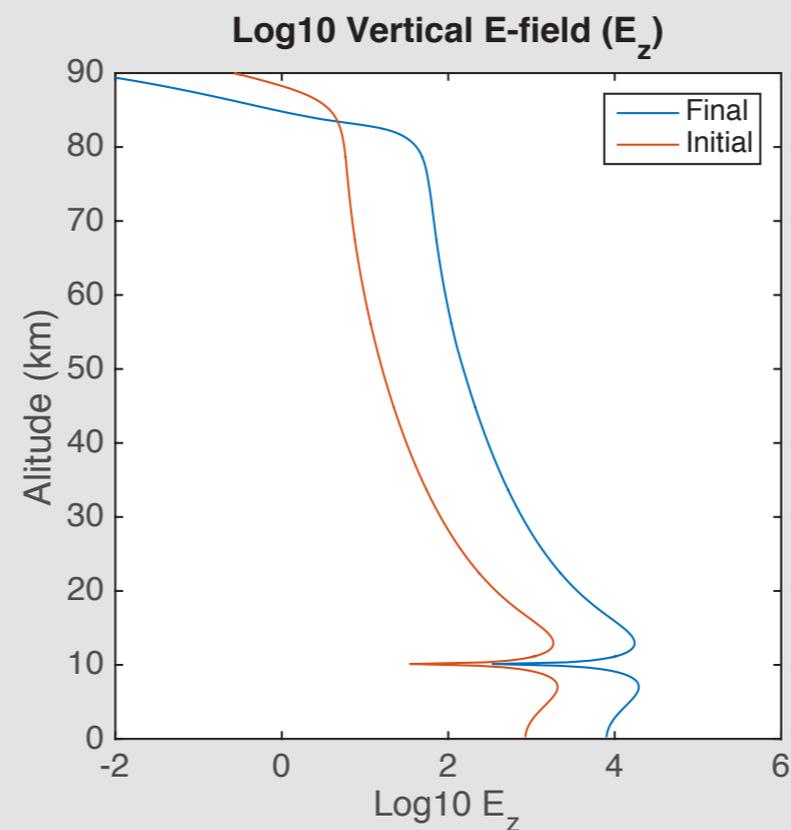
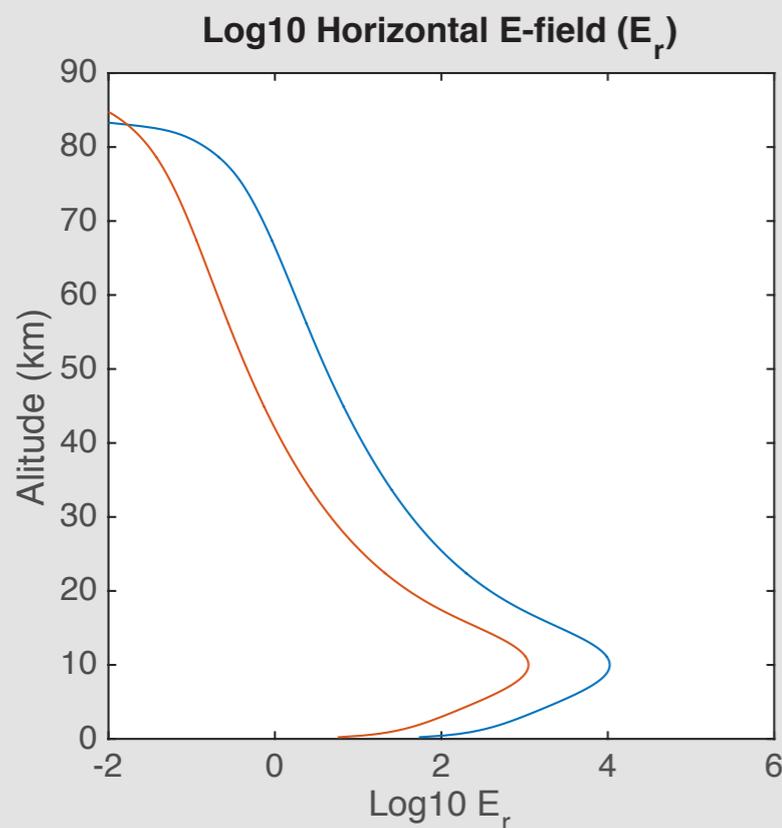
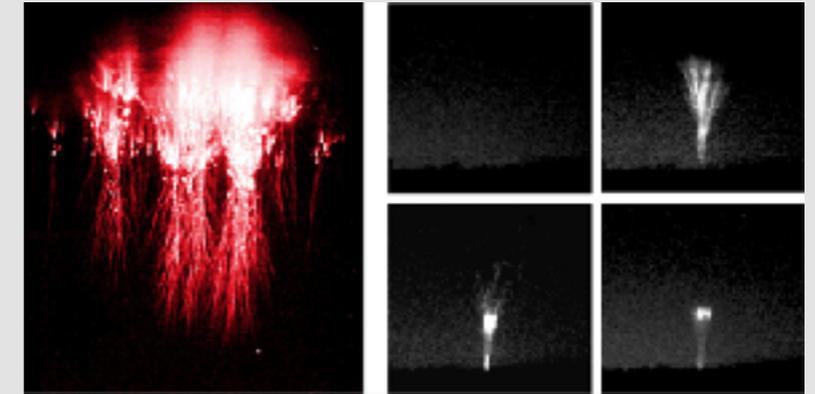


**Overall: chemical effects of pulse train likely to be negligible**

(For Active Experiments, this is likely good news)

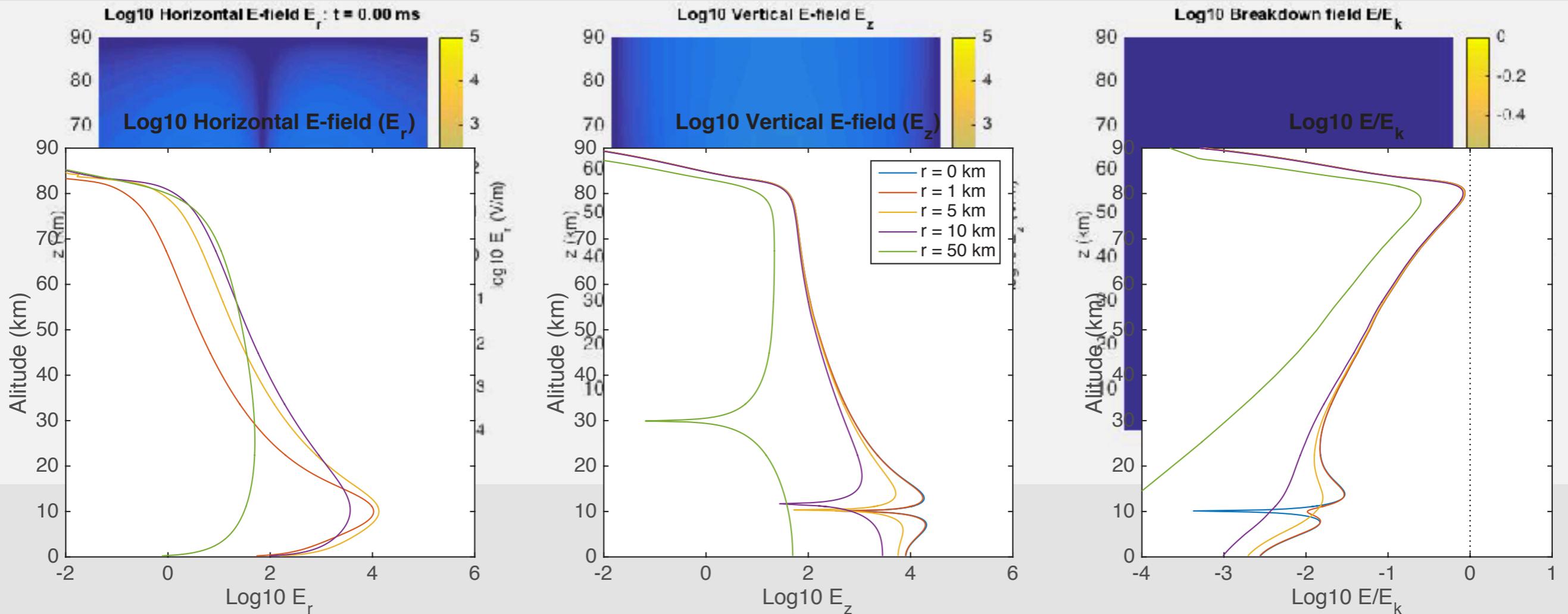
# Quasi-Electrostatic field effects

- ❖ Thunderstorm charge distributions produce electric fields that extend to the base of the ionosphere
- ❖ The breakdown field  $E_k$  scales with the neutral density  $N$ , and  $N \sim e^{-h/H}$
- ❖ when  $E > E_k$ , breakdown occurs – sprites!



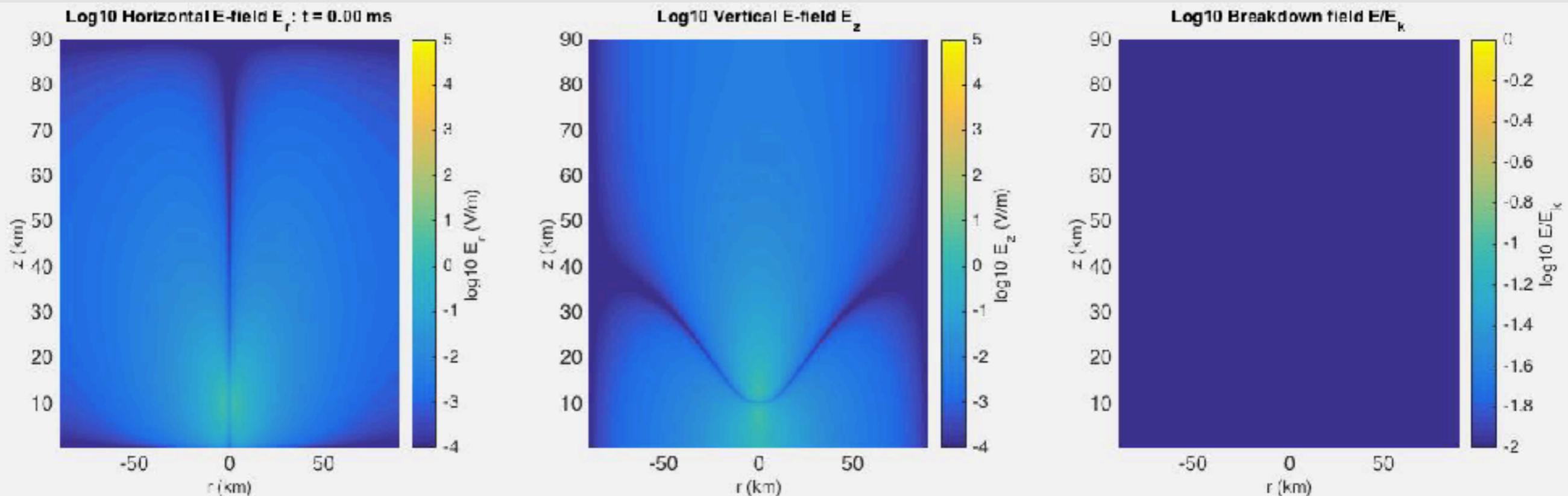
# QES calculation

- ❖ We use the 2D version of the QES field model of Kabirzadeh et al [2015]
- ❖ Consider initial charges of -50 C located at 5 km altitude and +50 C at 10 km
- ❖ Suddenly remove 50 C from 10 km altitude: a large positive cloud-to-ground
  - ❖ 500 C-km is just below the threshold for sprite initiation [Cummer et al, 2000]

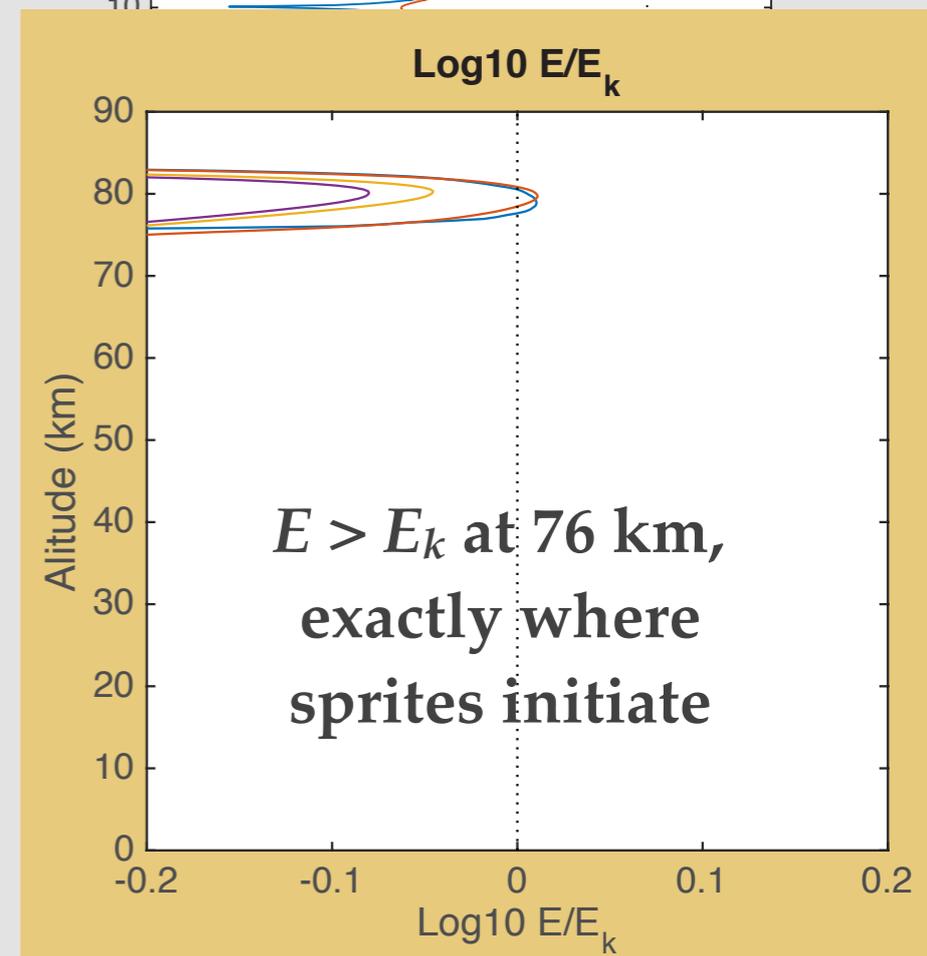
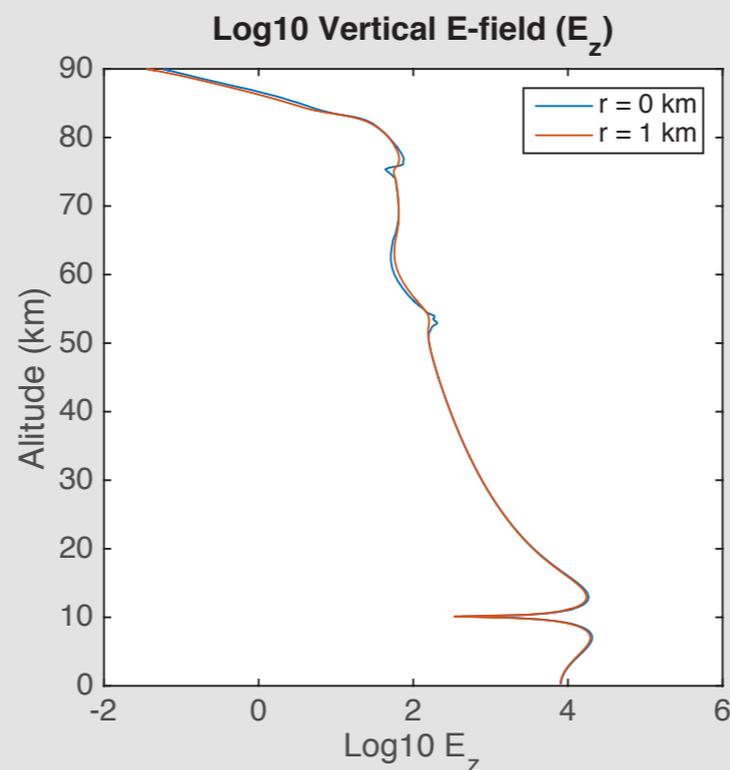
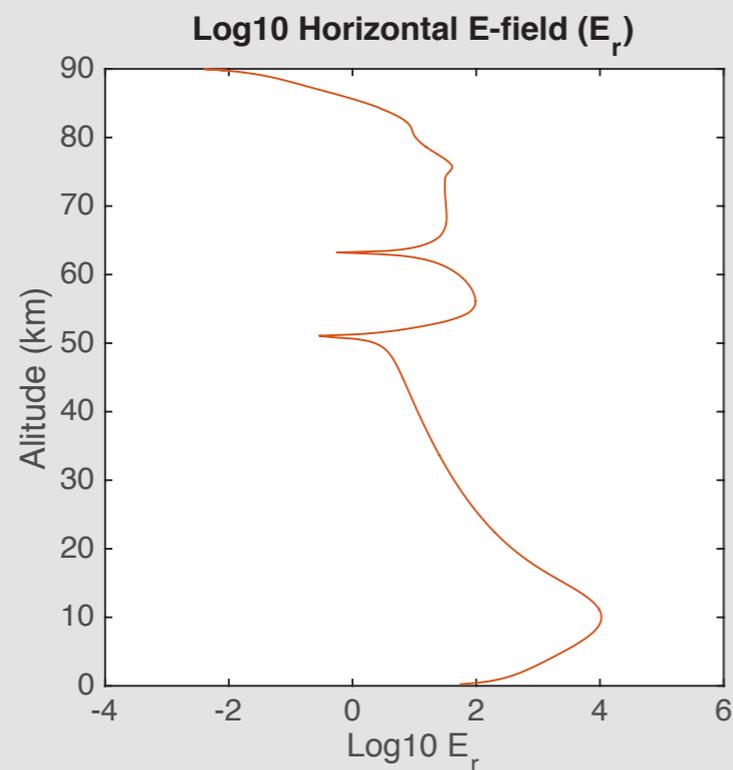
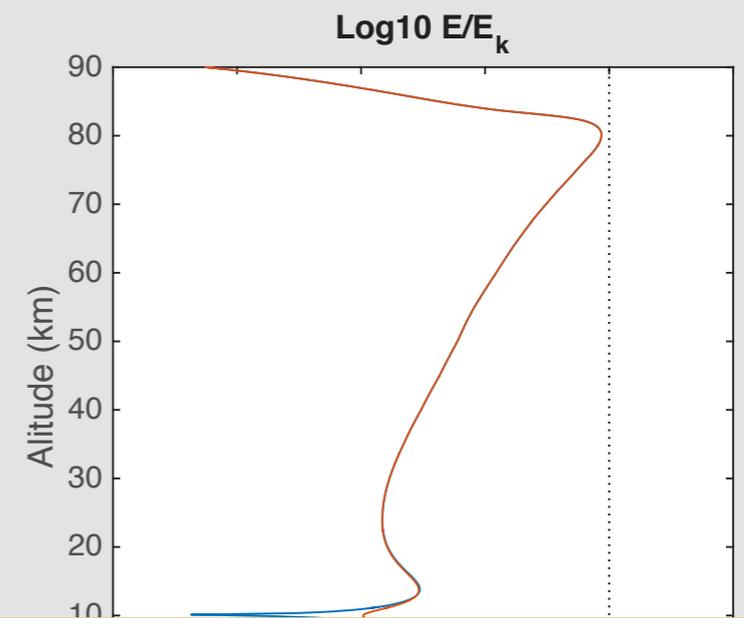
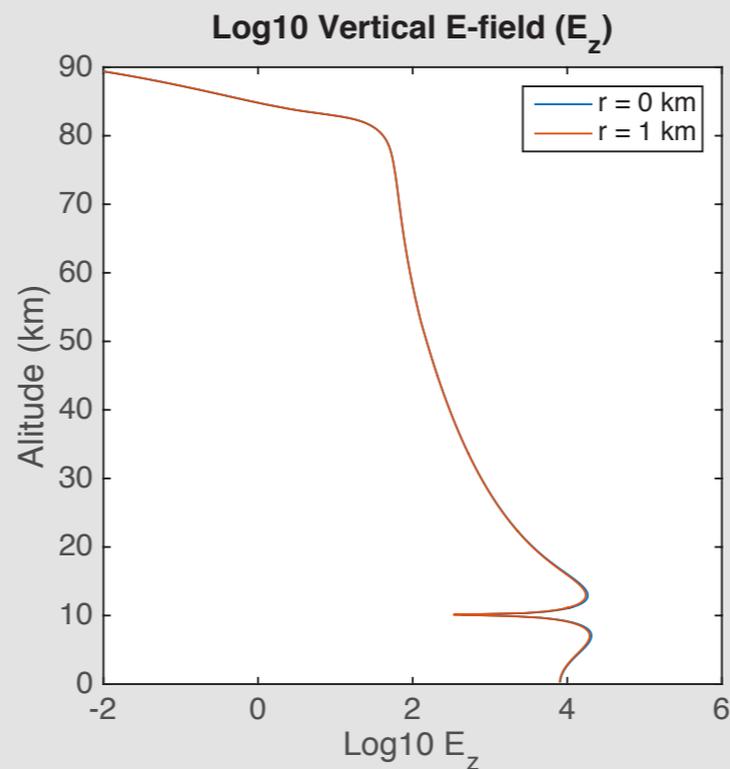
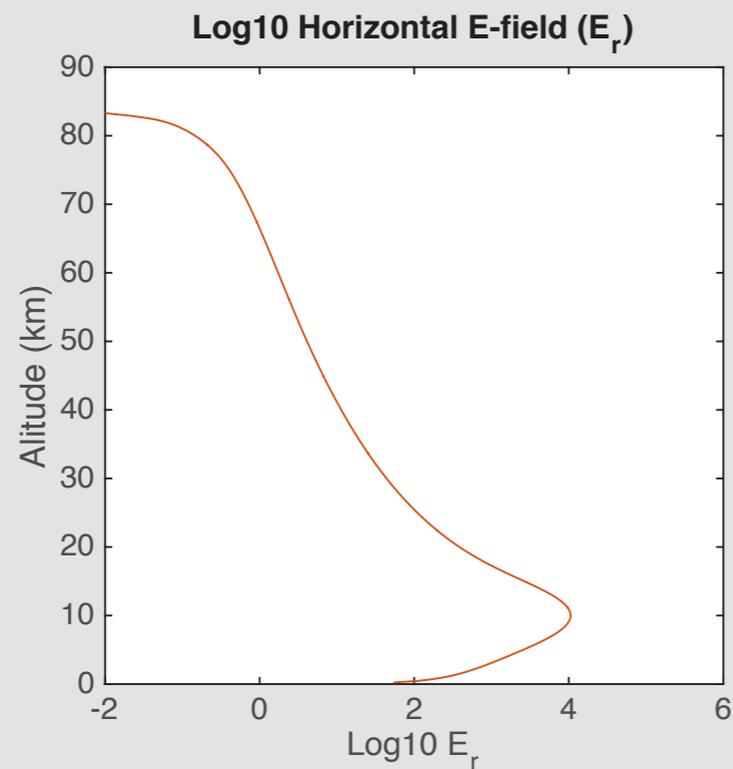


# QES after beam injection

- ❖ Neubert and Gilchrist [2004] first postulated that a beam injection could help trigger sprites
- ❖ We repeat our QES simulation with a column of enhanced electron density, 300 m in diameter with Gaussian distribution, given by Monte Carlo / chemistry simulation



# QES after beam injection



# Summary

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- ❖ **Explored atmospheric effects and diagnostics of 1 MeV electron beam injection**
  - ❖ train of 100 or 1000 pulses, every 1 ms; 500 us x 10 mA in each pulse
- ❖ **Ionization effects** suggest easy detection by ground-based radar (PFISR)
  - ❖ Possible detection by subionospheric VLF, but 3D modeling necessary
- ❖ **Optical emissions** (N<sub>2</sub><sup>+</sup> 1N lines) visible by photometer or all-sky camera
- ❖ X-ray fluxes likely too weak – simply not enough total energy injected
- ❖ Chemical effects negligible
- ❖ **Electrodynamics** suggest the ability to enhance fields above thunderstorms and **trigger sprites**
  - ❖ Timing of the experiment likely difficult!
- ❖ Models ready to explore different scenarios (energy, pulse sequence, etc.)