

# Estimating and Visualizing the Impact of Forecast Errors on System Operations

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Los Alamos National Laboratory

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Zeb Tate

University of Toronto

Dept. of Electrical and Computer Engr.

Energy Systems Group

e-mail: [zeb.tate@utoronto.ca](mailto:zeb.tate@utoronto.ca)

# Overview

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- Control center operations
- Modeling the impact of uncertainty
  - Modeling the uncertainty in variable generation forecasts
  - Modeling the reaction to forecast deviations
- Determining the impact of forecast deviations
- Extensions and future work

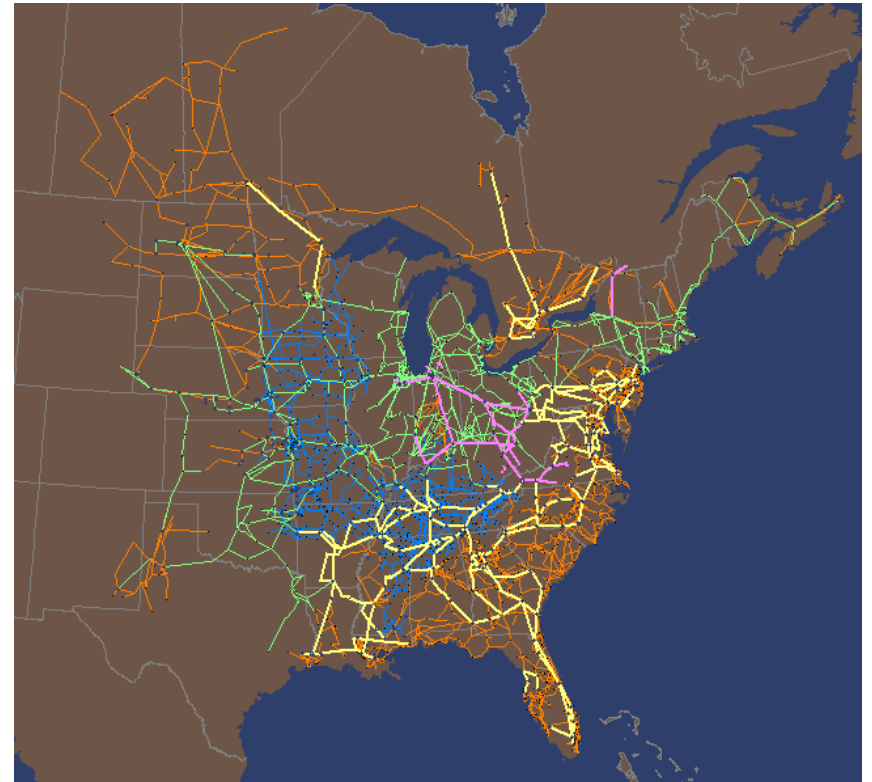
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# **CONTROL CENTER OPERATIONS & SITUATIONAL AWARENESS**

# Background on Power System Operations

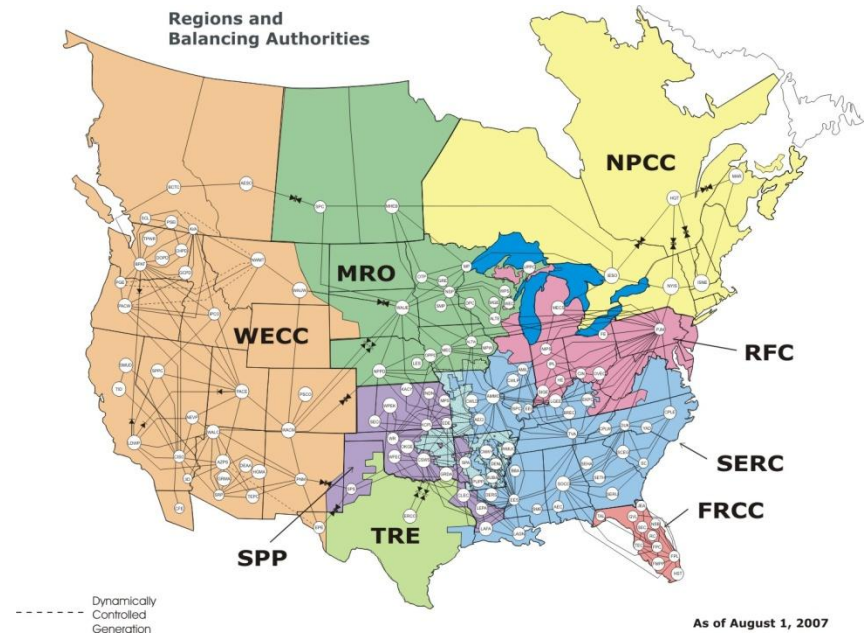
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- Synchronized power grids are (arguably) the most complex systems ever constructed
  - Eastern Interconnection has over 100,000 miles of transmission, over 600 GW of installed capacity
- In the North American power grid, system control is split amongst over 100 “balancing authorities”



# Control Center Operations

- Control centers operate their systems to meet performance standards set by:
  - International and national organizations (e.g., NERC)
  - Regional coordinating councils (e.g., NPCC, WECC)
  - Local rules (e.g., IESO and PJM Market Rules)



# Responsibilities of Operators

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- Maintaining sufficient primary frequency response resources
- Balancing power consumption and production
- Meeting voltage requirements
- Maintaining sufficient online and offline generation reserves
- Determining dispatch and commitment schedules

# Situational Awareness (SA)

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**What do grid operators need in order to responsibly manage their network?**

Situational awareness is “[u]nderstanding the current environment and being able to accurately anticipate future problems to enable effective actions.” [definition from PNNL]

# SA in Power Systems:

## “Understanding the Current Environment”

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- In power system operations, operators must have a sufficient grasp of current grid conditions so they can identify any existing problems and, when necessary, take immediate corrective actions
- Various data processing and visualization tools built into modern energy management systems (EMSs) for this purpose

Alarms

State estimation

Topology processing

Contingency Analysis

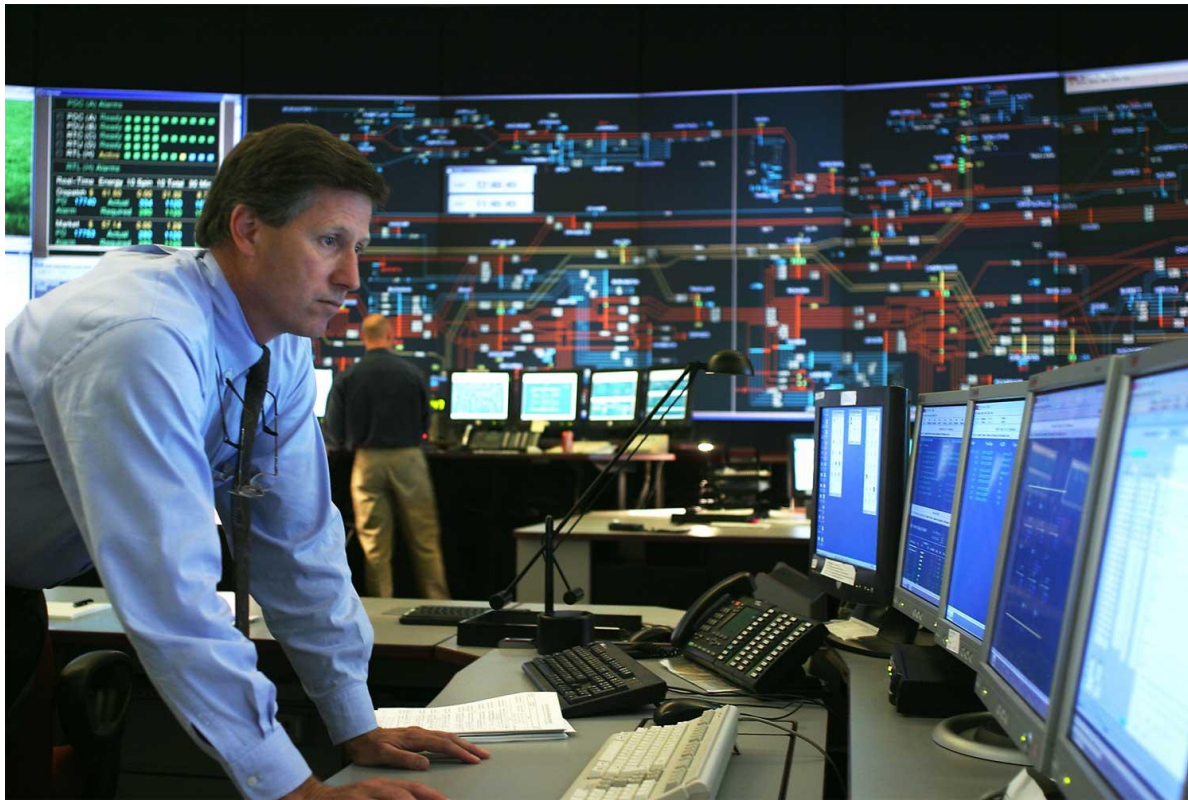
Dynamic security assessment

Voltage contours



# Example of a Modern Control Room

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Dynamic map board showing flows, voltages, and status information from the Independent Electricity System Operator (IESO)

## SA in Power Systems:

“Being Able to Accurately Anticipate Future Problems to Enable Effective Actions”

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- Knowing there are no existing problems isn't sufficient—operators must also be able to foresee future problems so they have sufficient time to act
  - 4 to 6 hours for changes to generator commitment schedules
- In an ideal world, the fidelity of these predictions would be sufficient to take any actions needed to maintain grid reliability
  - In reality, computational demands & forecast errors make this difficult

# Impact of Poor SA on Grid Reliability

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- Of the 6 major blackouts in North America within the past 50 years, 4 were due in part to a lack of SA
  - **November 9, 1965 Blackout:** Operators unaware of relay operations that eventually led to a cascading blackout (20,000 MW, 30 million people)
  - **December 22, 1982 Blackout:** Volume and format of raw data made it hard to gauge the extent of a disturbance and determine the corrective action to take (12,350 MW, 5 million people)
  - **August 10, 1996 Blackout:** Operators unaware of insecure system state after initial unscheduled line openings (28,000 MW, 7.5 million people)
  - **August 14, 2003 Blackout:** First Energy, MISO operators unaware of problems (61,800 MW, 50 million people)

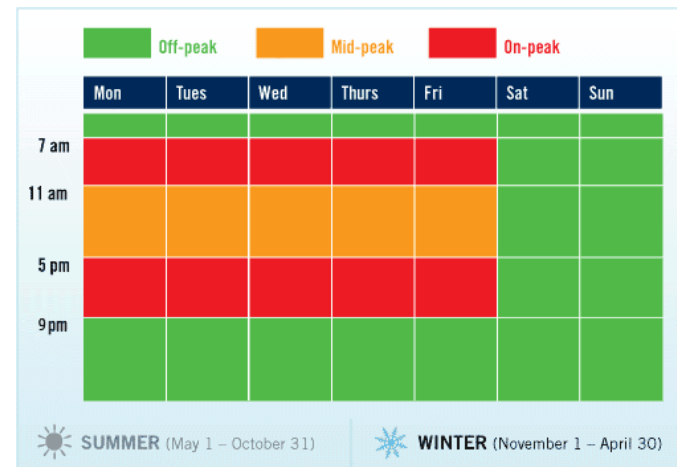
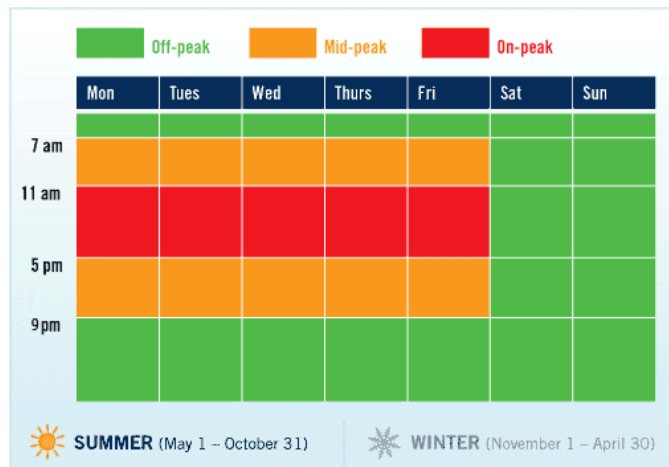
# Impact of Variable Generation on SA

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- There is a concerted effort by many federal and regional governments to promote generation technologies that are fundamentally stochastic, namely wind & solar generation
- A large build-up of variable generation will impact the ability of operators to:
  - Identify existing problems (lack of telemetry, particularly for VG connected to a distribution network)
  - Anticipate problems (forecast uncertainty)
  - Choose appropriate control actions (lack of actionable information to drive control decisions)

# Daily Load Variation

- The load variation throughout the day is highly predictable based on season, time of day, day of the week, and precipitation
  - Basis for time-of-use rates, which designate off-, mid-, and on-peak prices (and demand) for Ontario customers



[http://www.ieso.ca/imoweb/siteshared/tou\\_rates.asp](http://www.ieso.ca/imoweb/siteshared/tou_rates.asp)

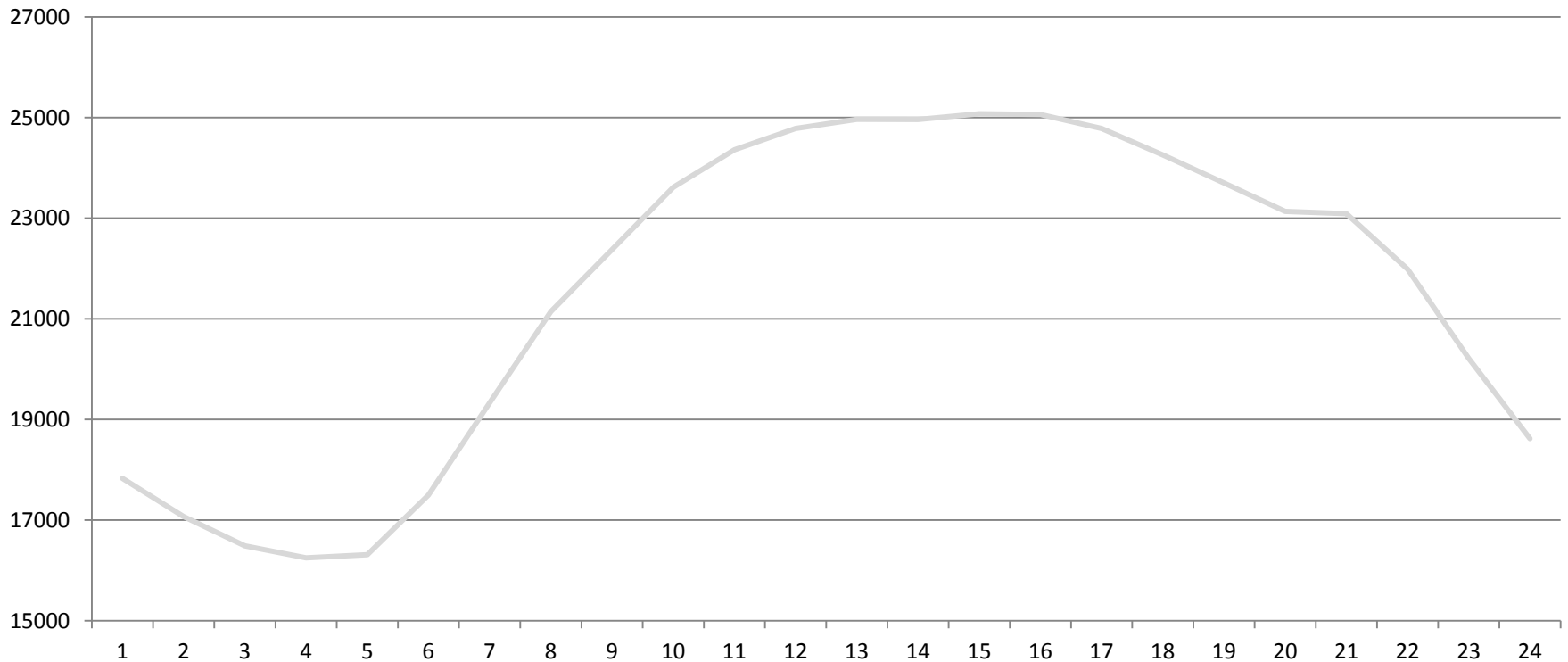
# Sample Daily Load Curve

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**Hourly Load - July 8, 2010**

**Minimum: 16,250 MW / Peak: 25,075 MW**

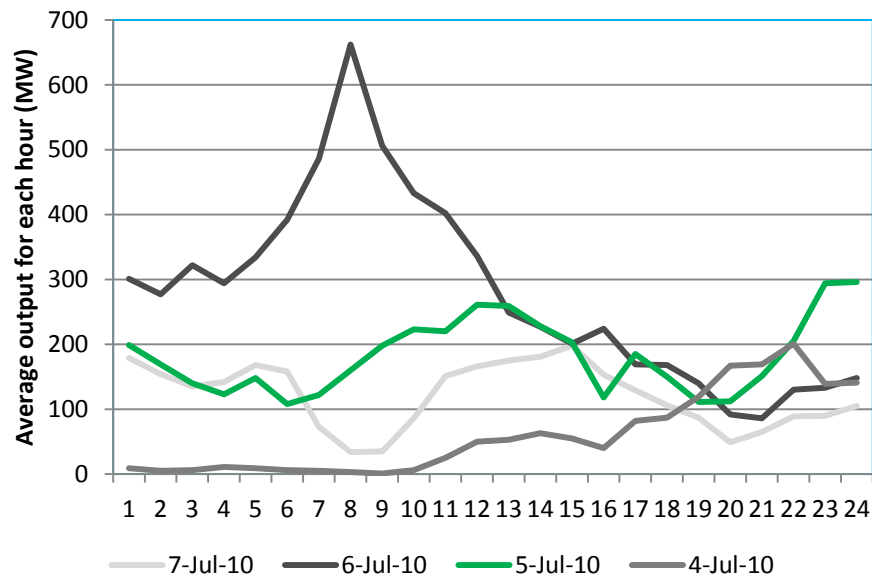
**Average: 21,539 MW**



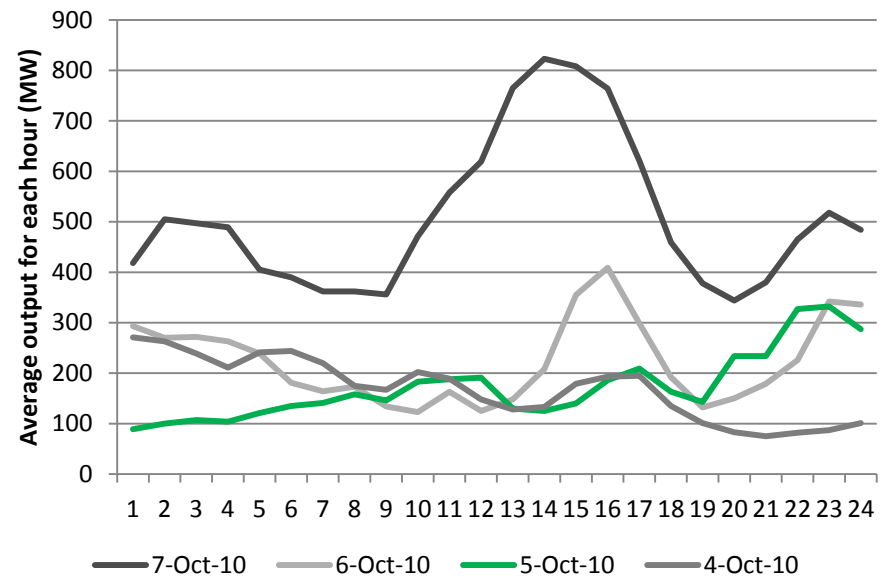
# Wind Variation

- Wind power output is much less predictable than the load, so old thinking and old tools built around load forecasting are unlikely to translate over directly

**Hourly Wind Output for July 4-7, 2010**



**Hourly Wind Output for Oct. 4-7, 2010**



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# **MODELING THE UNCERTAINTY IN VARIABLE GENERATION FORECASTS**



# Mitigating Potential Degradation in Reliability

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- The additional operational challenges associated with variable generation are due primarily to the uncertainty of output forecasts
- Reducing the uncertainty in renewable plant output can improve reliability and efficiency by:
  - Allowing operators to identify potential regulation shortfalls further in advance
  - Reducing the unnecessary commitment of additional generators or curtailment of variable generation due to overly conservative reserve estimates
- Complete elimination of uncertainty is not possible, but characterizing and improving forecast accuracy can and should be done insofar as it is possible

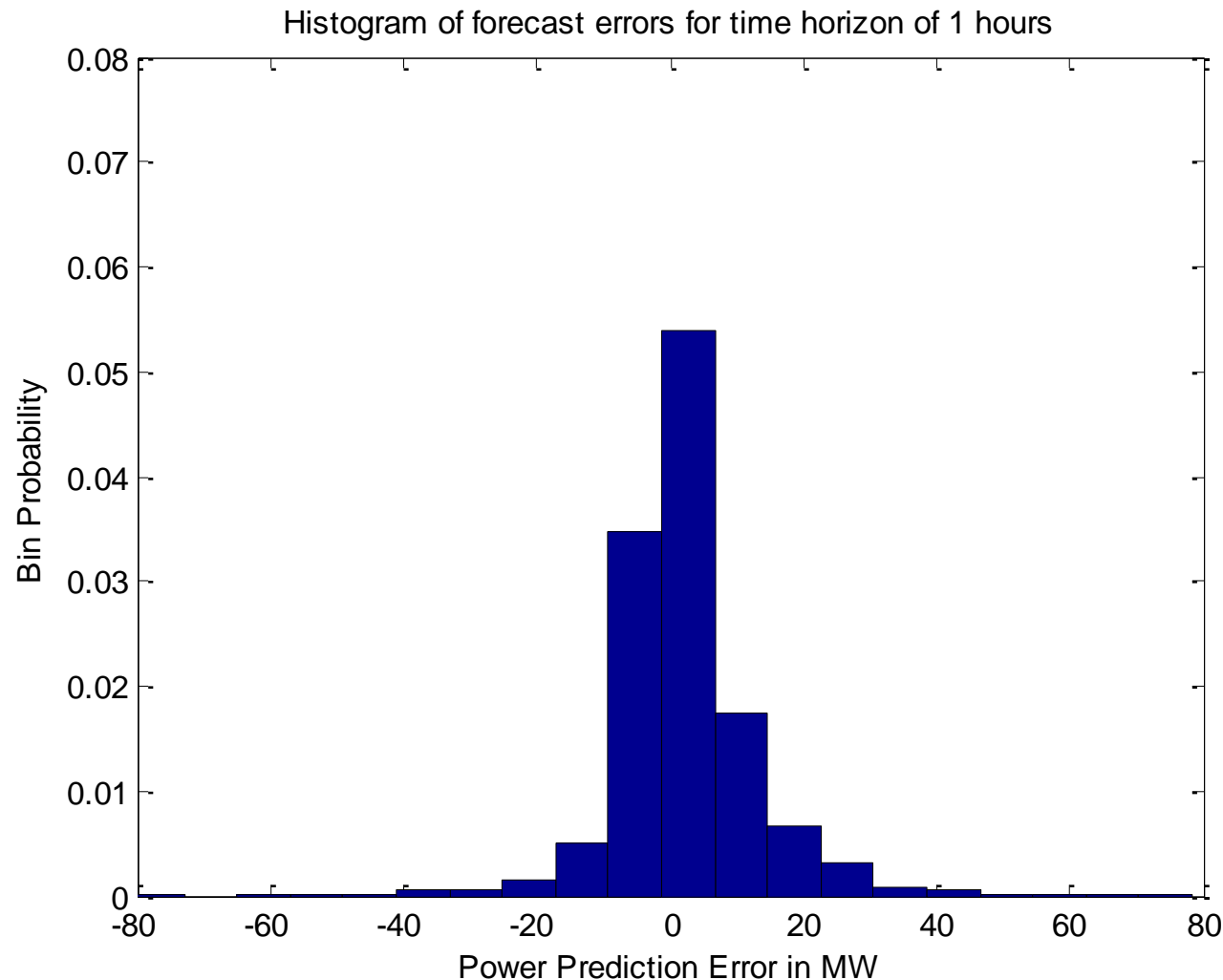
# Data Driven Characterization of Forecast Uncertainty

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- Development and population of renewable generation data archives is the first step towards improving the performance of renewable output forecasts and characterizing forecast errors
- Example: estimating the error distribution of a vendor's forecast product for a specific time horizon & output interval
  - Create a histogram of historical forecast error measurements and either use this directly for subsequent analyses or fit the histogram to a distribution via parameter estimation techniques
  - Empirical probability mass function will become a better approximation to the probability density function of the error as more samples are used, but this is limited by data availability
  - Can use results to conduct sensitivity analysis on interval length (e.g., evaluate the impact on NERC CPS2 performance by looking at 10-minute forecast errors) and forecast horizon (e.g., determine the minimum horizon that results in certain bounds on the forecast error)

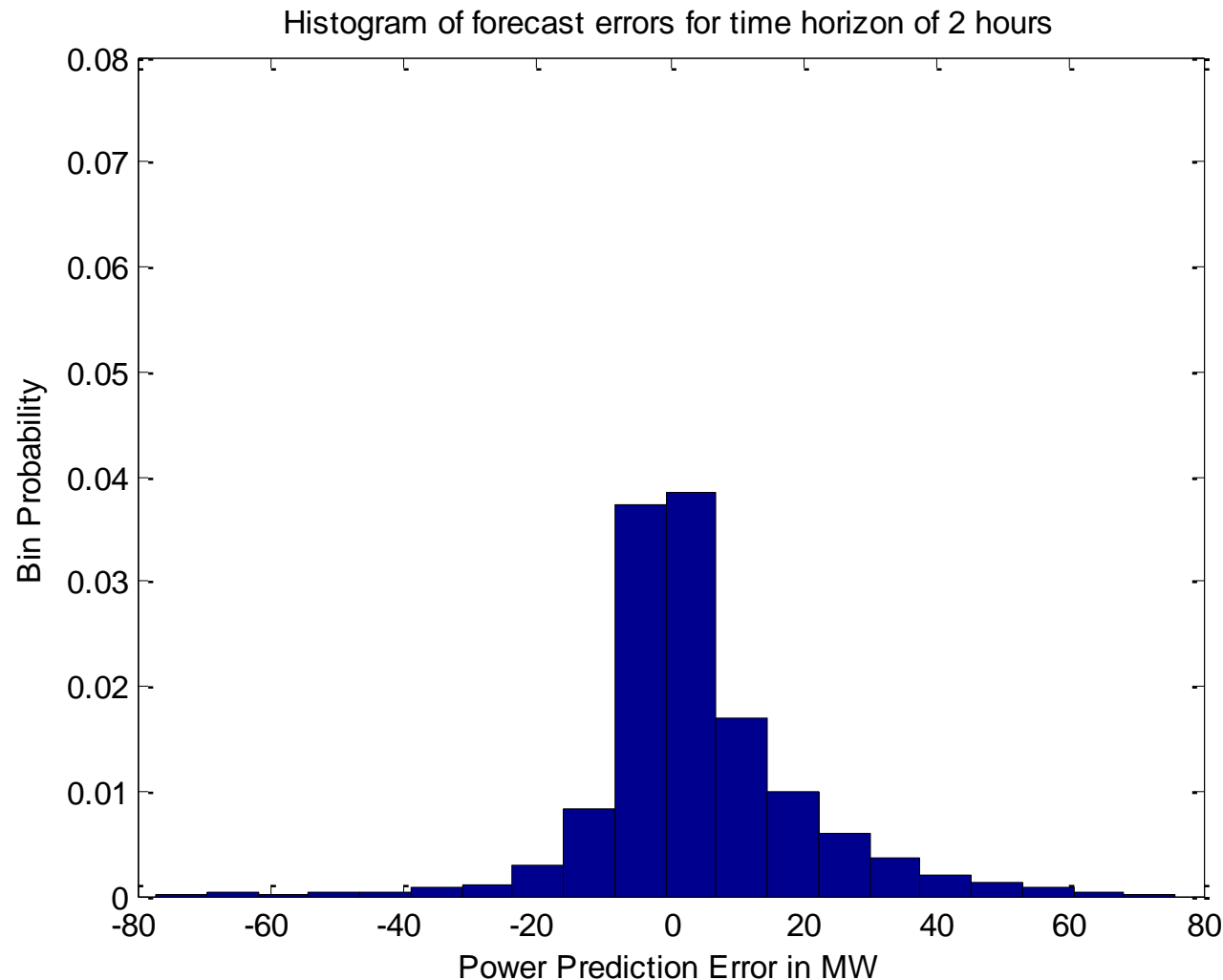
# ARMA Forecast Error for 1-Hour Output Interval with Time Horizon of 1 Hour

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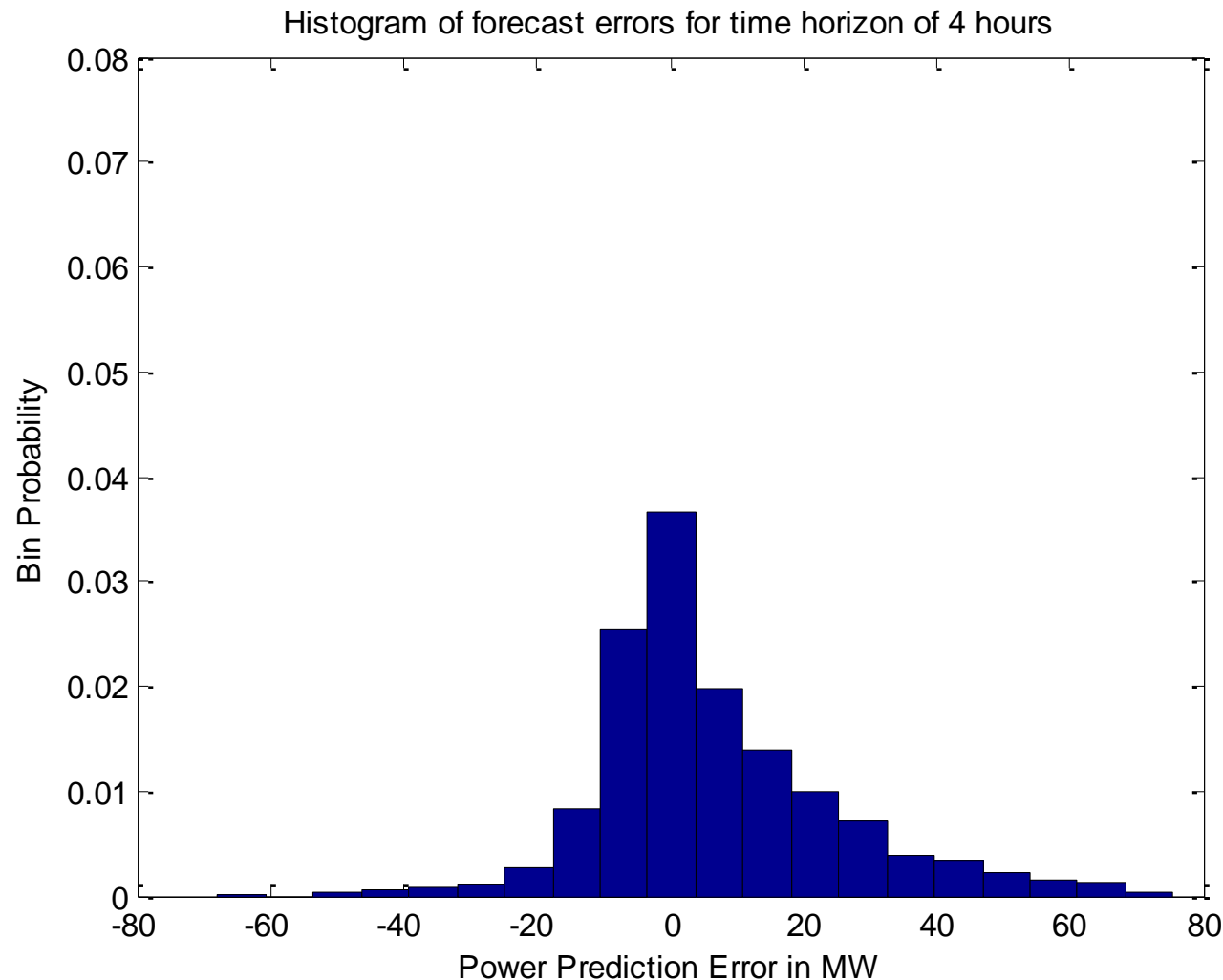
# ARMA Forecast Error for 1-Hour Output Interval with Time Horizon of 2 Hours

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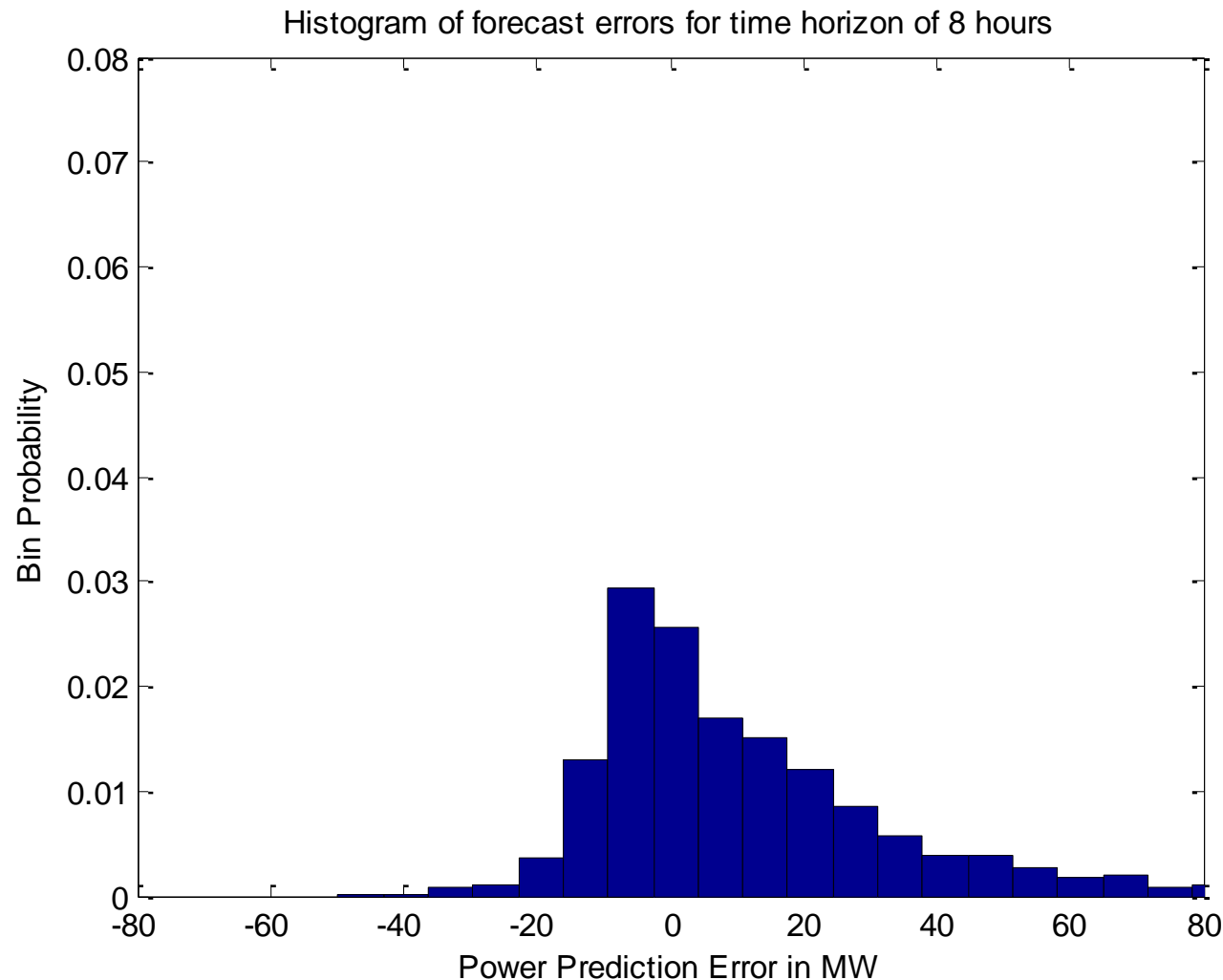
# ARMA Forecast Error for 1-Hour Output Interval with Time Horizon of 4 Hours

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# ARMA Forecast Error for 1-Hour Output Interval with Time Horizon of 8 Hours

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# Data Driven Characterization of Forecast Uncertainty

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- By utilizing a sufficiently large data set, such histograms could be used to approximate the distribution of forecast errors or error correlations between sites
- Example of comprehensive wind farm data collection
  - On the HQ system, SNC-Lavalin has installed a data collection system (SAGIPE) that collects 45,000 telemetry points every 10 minutes from 8 wind farms (total installed capacity of 990 MW)
  - Results in storage requirements of  $(45,000 \times 6 \times 24 \times 365) = 2.365 \times 10^9$  points per year = 8.81 GB per year (assuming single precision)
  - Extrapolating out to 4,000 MW = 35.6 GB per year
  - Manageable data requirements suggest that it should be possible to collect and archive the complete set of 10-minute data for every turbine

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# **MODELING THE REACTION TO FORECAST DEVIATIONS**



# System Response to Forecast Error

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- Substantial deviations from forecast could exhaust reserve margins
  - Operating reserve margins are based on the ability of the system to continue operating despite the occurrence of instantaneous, unscheduled events (e.g., trip of a nuclear plant or transmission line)
    - e.g., NPCC Operating Reserve Criteria require 10-minute reserves to be greater than or equal to the first contingency loss & 30-minute reserves to be greater than or equal to the second contingency loss
  - Managing uncontrolled, sustained ramps in generation could be more challenging than the loss of any single unit (e.g., 2000 MW / 1 hour vs. 1000 MW / instant)
- Method of modeling the redispatch due to forecast error is critical in evaluating reserve adequacy with variable generation

# Statement of the Problem

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- On the power grid, there must be a balance of produced and consumed power in the network
  - Otherwise, sustained frequency excursions will occur
- When there is a deviation from the scheduled output of a VG, the shortfall/surplus in generation must be compensated by other sources of generation
- Even if losses are neglected and a linearization of the power network equations is used, modeling the re-dispatch of the remaining system resources is nontrivial

$$\mathbf{1}_{1 \times \mathcal{G}} \Delta \mathbf{P}_{\mathbf{G}} + \mathbf{1}_{1 \times \mathcal{V}} \Delta \mathbf{P}_{\mathbf{V}} = 0$$

$\Delta \mathbf{P}_{\mathbf{G}} \in \mathbb{R}^{\mathcal{G}}$  : vector of redispatch in controllable resources  
 $\Delta \mathbf{P}_{\mathbf{V}} \in \mathbb{R}^{\mathcal{V}}$  : vector of forecast errors at each wind site

# Approaches to Redispatch Modeling

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- One common approach is to have a single generator (the “slack” generator) provide all necessary regulation

$$\Delta \mathbf{P}_G^{\text{slack}} = [0 \quad 0 \quad \cdots \quad 0 \quad -\mathbf{1}_{1 \times \mathcal{V}} \Delta \mathbf{P}_V \quad 0 \quad \cdots \quad 0]^T$$

- A generalization of the slack generator approach is to proportionally assign the forecast error to the controllable resources (a.k.a. re-dispatch using “participation factors”)

$$\Delta \mathbf{P}_G^{\text{p.f.}} = (-\mathbf{1}_{1 \times \mathcal{V}} \Delta \mathbf{P}_V) \begin{bmatrix} \alpha_1 & \alpha_2 & \cdots & \alpha_{\mathcal{G}} \end{bmatrix}^T$$
$$\sum_{i=1}^{\mathcal{G}} \alpha_i = 1$$

# Comments on the Participation Factor Approach

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- The participation factor approach is based on the assumption that the best way to allocate the forecast error to the remaining resources is known a priori
  - If this *is* known, then using the participation factor approach can be much faster than other methods of modeling forecast error reaction
  - However, participation factors have to be redistributed when an up/down re-dispatch limit is hit, and so are likely to only be valid for very small forecast errors

# Optimal Reaction to Forecast Error

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- An alternative method is to optimally re-dispatch the remaining generation (e.g., to minimize cost, control movement, or line violations) while enforcing generation limits and power balance

$$\begin{aligned} \Delta \mathbf{P}_{\mathbf{G}}^* &= \arg \min_{\Delta \mathbf{P}_{\mathbf{G}}} f(\Delta \mathbf{P}_{\mathbf{G}}, \Delta \mathbf{P}_{\mathbf{V}}) \\ \text{subject to } \quad &\Delta \mathbf{P}_{\mathbf{G}}^{\min} \preceq \Delta \mathbf{P}_{\mathbf{G}} \preceq \Delta \mathbf{P}_{\mathbf{G}}^{\max} \\ &\mathbf{1}_{1 \times \mathcal{G}} \Delta \mathbf{P}_{\mathbf{G}} + \mathbf{1}_{1 \times \mathcal{V}} \Delta \mathbf{P}_{\mathbf{V}} = 0 \end{aligned}$$

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# **DETERMINING THE IMPACT OF FORECAST DEVIATIONS**

# Determining the Impacts of Forecast Deviations

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- Assessing the impact of uncertainty is challenging, but it will be increasingly important as system operations becomes more reliant on probabilistic information
- We want to develop tools that quantify the impact of forecast errors based on three principles:
  1. **Forecast error distribution is important:** a forecast with an error bound of  $\pm 10\%$  at a confidence level of 99% has the potential to cause more trouble than a forecast with an error bound of  $\pm 1\%$  at the same confidence level
  2. **Location is important:** The transmission network may restrict which generators can compensate which VGs' forecast errors
  3. **Speed is important:** Any metrics and visualizations should be easy to explain, provide predictable output, and have computation times that make it usable in control centers

# Modeling the Effects of VG & Non-VG Generator Output on Line Flows

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- Model impacts on branch flows using dc (or linearized ac) power flow equations

$$\Delta \mathbf{f} = \mathbf{ISF}_G \Delta \mathbf{P}_G + \mathbf{ISF}_V \Delta \mathbf{P}_V$$

$\Delta \mathbf{f} \in \mathbb{R}^L$  : change in flow on branches

$\Delta \mathbf{P}_G$  ( $\Delta \mathbf{P}_V$ )  $\in \mathbb{R}^G$  ( $\mathbb{R}^V$ ) : change in output of controllable (variable) generators

$\mathbf{ISF}_G$  ( $\mathbf{ISF}_V$ )  $\in \mathbb{R}^{L \times G}$  ( $\mathbb{R}^{L \times V}$ ) : injection shift factors for controllable (variable) generators

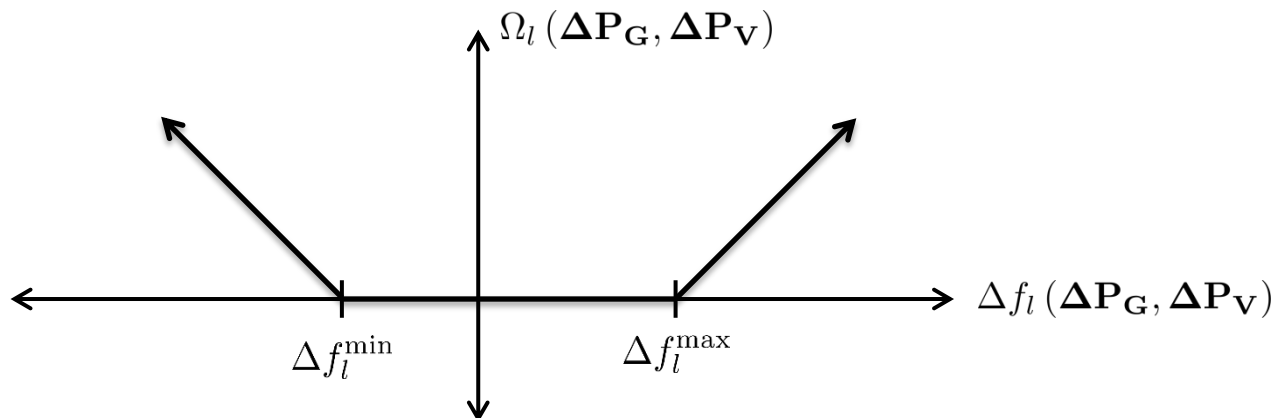
- The elements within the **ISF** matrix are used for contingency analysis and transmission loading relief, so the need for this data is unlikely to be a stumbling block for implementation



# Ranking System-Level Impacts

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- In contingency ranking and other techniques where the system impact of different events are being considered, penalty functions are often used to indicate the importance of violations
- For example, to penalize branch overcurrent:



# Determining the Worst Case Forecast Deviation

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- Using the models described above, the “worst case forecast deviation”,  $\Delta \mathbf{P}_V^*$ , is defined by:

$$\begin{aligned}
 & \Delta \mathbf{P}_V^* = \arg \max_{\Delta \mathbf{P}_V} \mathbf{1}_{1 \times \mathcal{L}} \Omega(\Delta \mathbf{f}) \\
 & \text{subject to } \Delta \mathbf{f} = \mathbf{ISF}_G \Delta \mathbf{P}_G + \mathbf{ISF}_V \Delta \mathbf{P}_V \\
 & \Delta \mathbf{P}_V \in \{ [\Delta P_{V_1}^{\min}, \Delta P_{V_1}^{\max}] \times \dots \times [\Delta P_{V_\nu}^{\min}, \Delta P_{V_\nu}^{\max}] \} \\
 & \Delta \mathbf{P}_G \in \left\{ \begin{array}{l} \arg \min_{\Delta \mathbf{P}'_G} \mathbf{1}_{1 \times \mathcal{L}} \Omega'(\Delta \mathbf{f}') \\ \text{subject to } \Delta \mathbf{f}' = \mathbf{ISF}_G \Delta \mathbf{P}'_G + \mathbf{ISF}_V \Delta \mathbf{P}_V \\ \Delta \mathbf{P}_G^{\min} \preceq \Delta \mathbf{P}'_G \preceq \Delta \mathbf{P}_G^{\max} \\ \mathbf{1}_{1 \times \mathcal{G}} \Delta \mathbf{P}'_G + \mathbf{1}_{1 \times \nu} \Delta \mathbf{P}_V = \mathbf{0} \end{array} \right\} \\
 & \Omega = \begin{bmatrix} \Omega_1(\Delta f_1) \\ \vdots \\ \Omega_L(\Delta f_L) \end{bmatrix} \in \Re^{\mathcal{L}} : \text{vector of penalty function evaluations for each line} \\
 & [\Delta P_{V_i}^{\min}, \Delta P_{V_i}^{\max}] \in \Re : \text{confidence interval of variable generator } i
 \end{aligned}$$

- “Maximin”, infinite Stackelberg game

# Challenges with the Original Formulation: Inner Equilibrium Constraint

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- One problem with the above formulation is that the feasible space of solutions is defined by an objective function (referred to as a mathematical programs with equilibrium constraints, or MPEC, in the literature)
- Because the inner optimization is a linear program, the equilibrium constraint can be replaced by the stationarity and complementarity conditions which must be satisfied
- Becomes a linear program with SOS1 constraints

# Challenges with the Original Formulation: Non-Convex Outer Objective

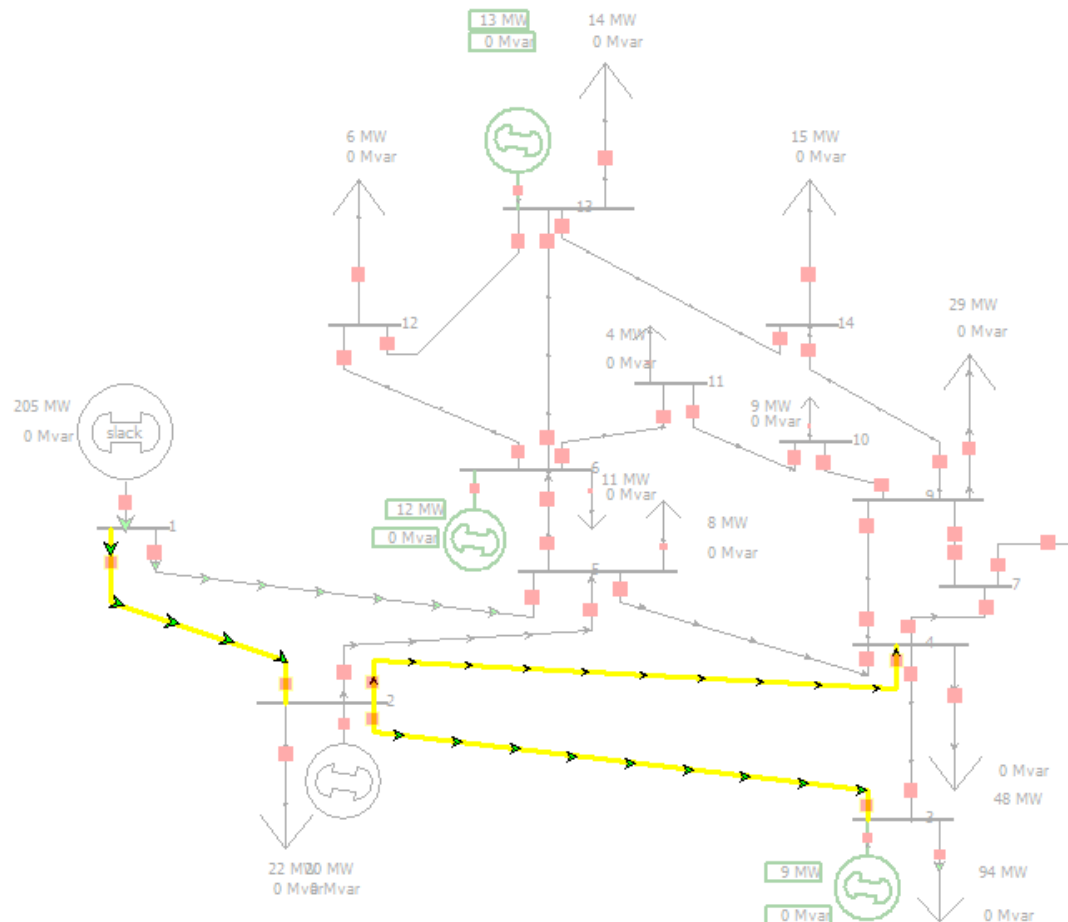
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- The outer optimization is a maximization over a sum of piecewise convex functions
- Can be rewritten as a linear program with SOS2 constraints
- Using these transformations, the problem can be solved using a standard ILP solver (e.g., CPLEX, GUROBI)

# Case Study:

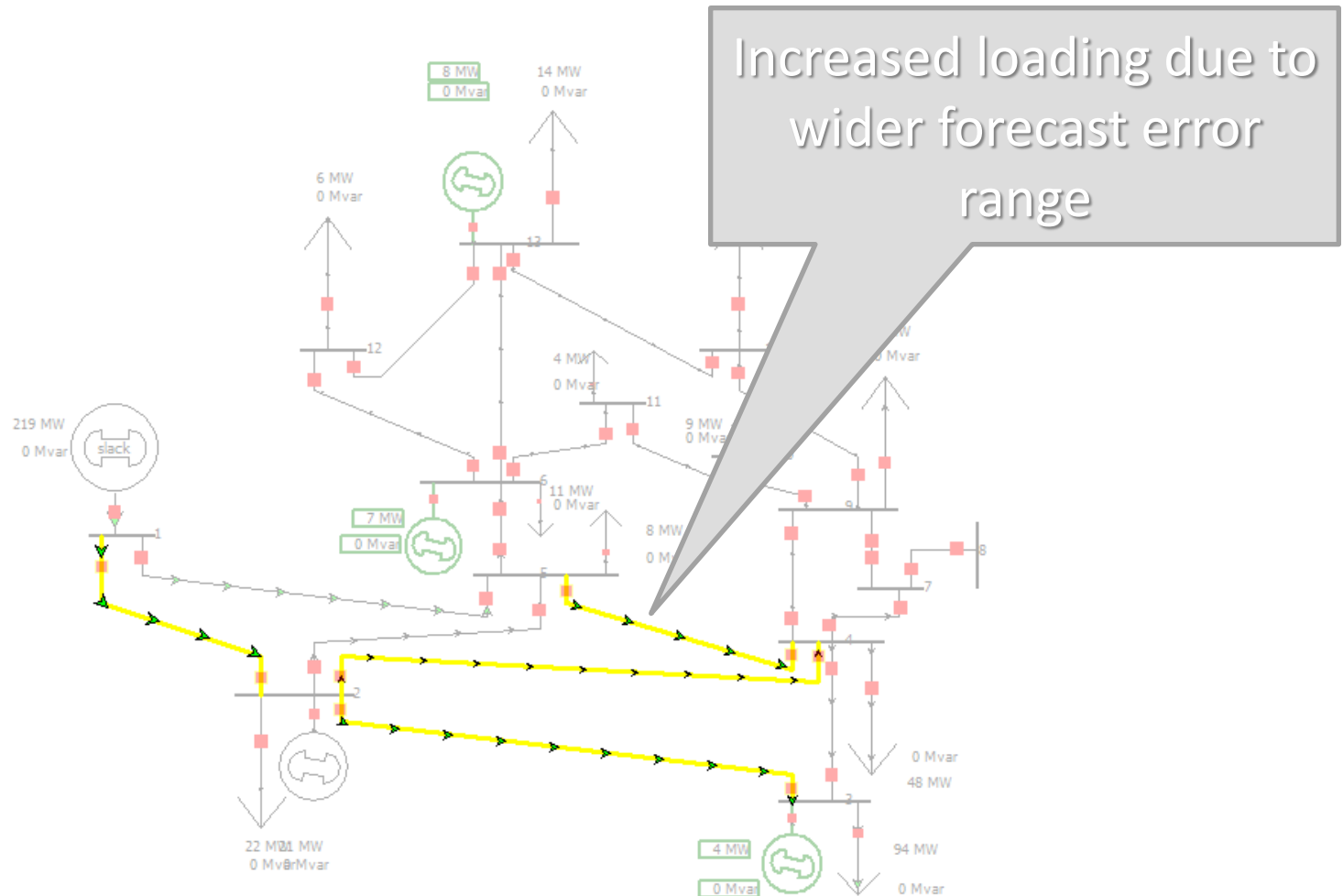
## 14 Bus System (Confidence Level: 50%)

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# Case Study:

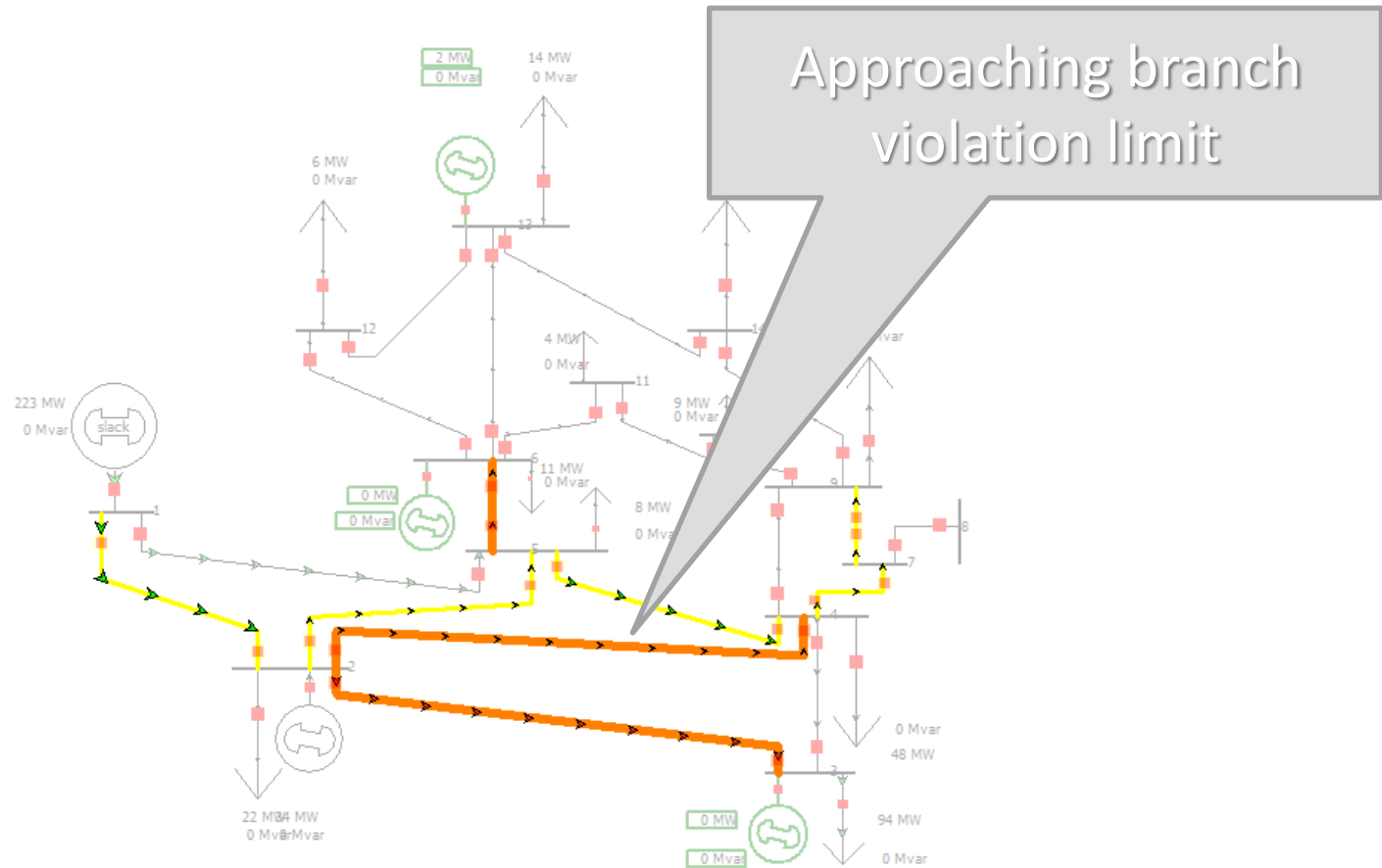
## 14 Bus System (Confidence Level: 75%)



# Case Study:

## 14 Bus System (Confidence Level: 95%)

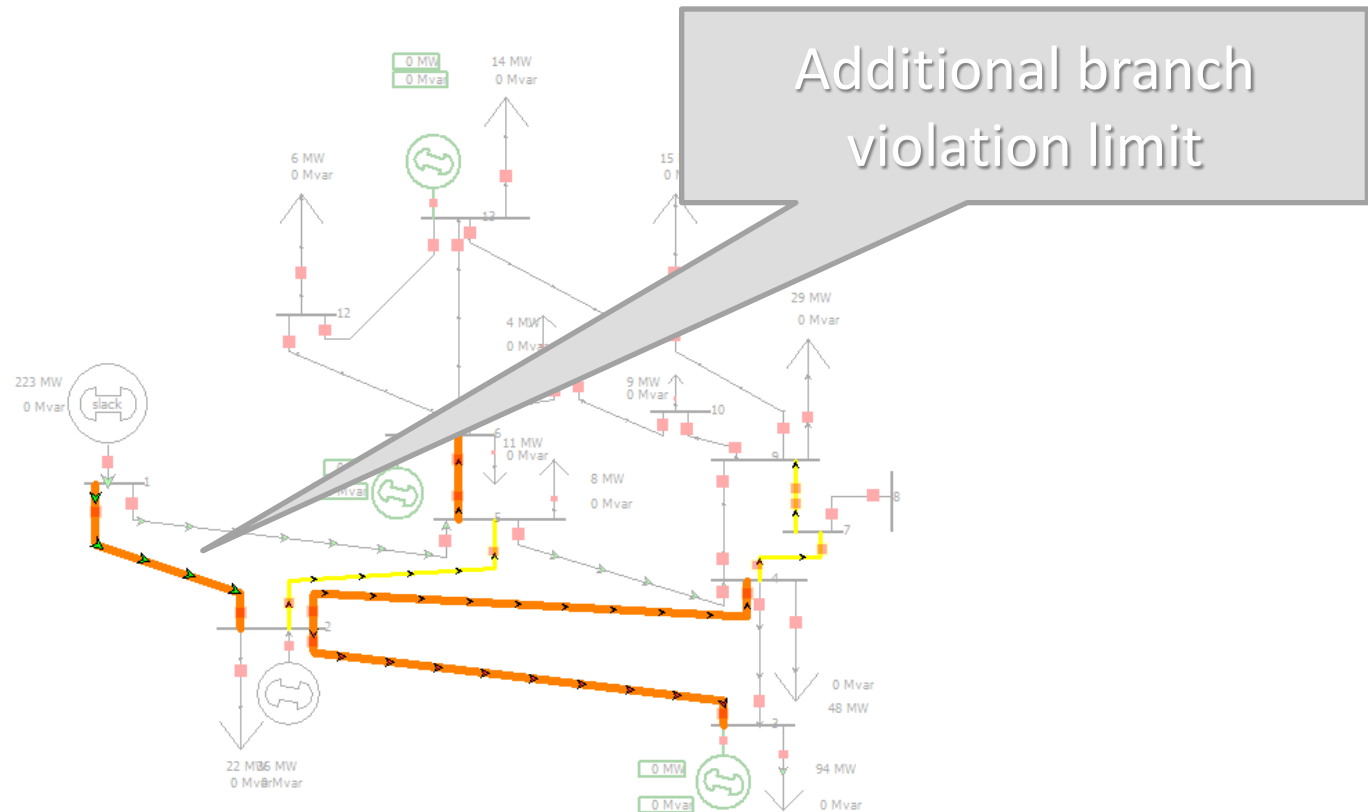
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# Case Study:

## 14 Bus System (Confidence Level: 99%)

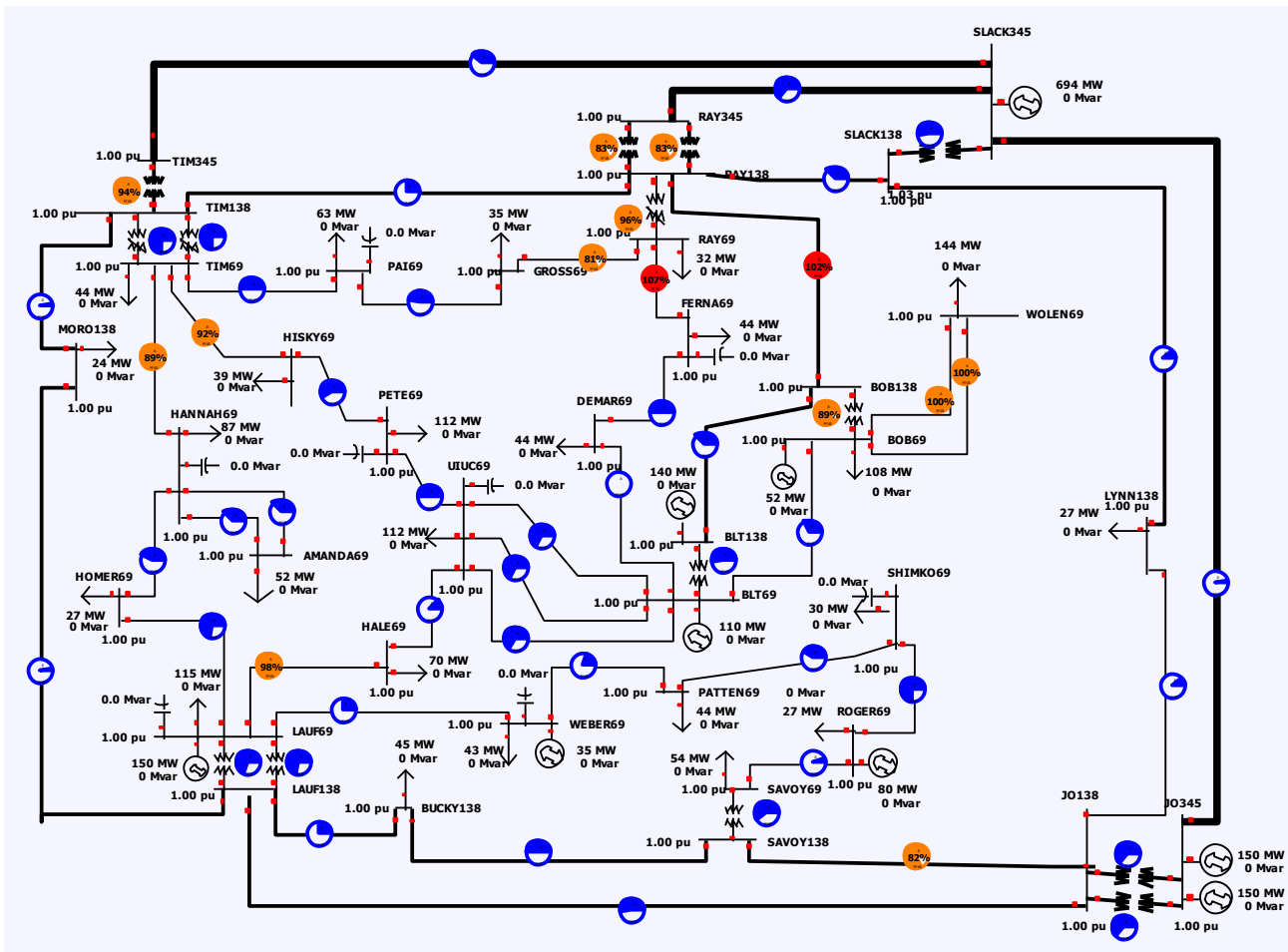
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# Case Study:

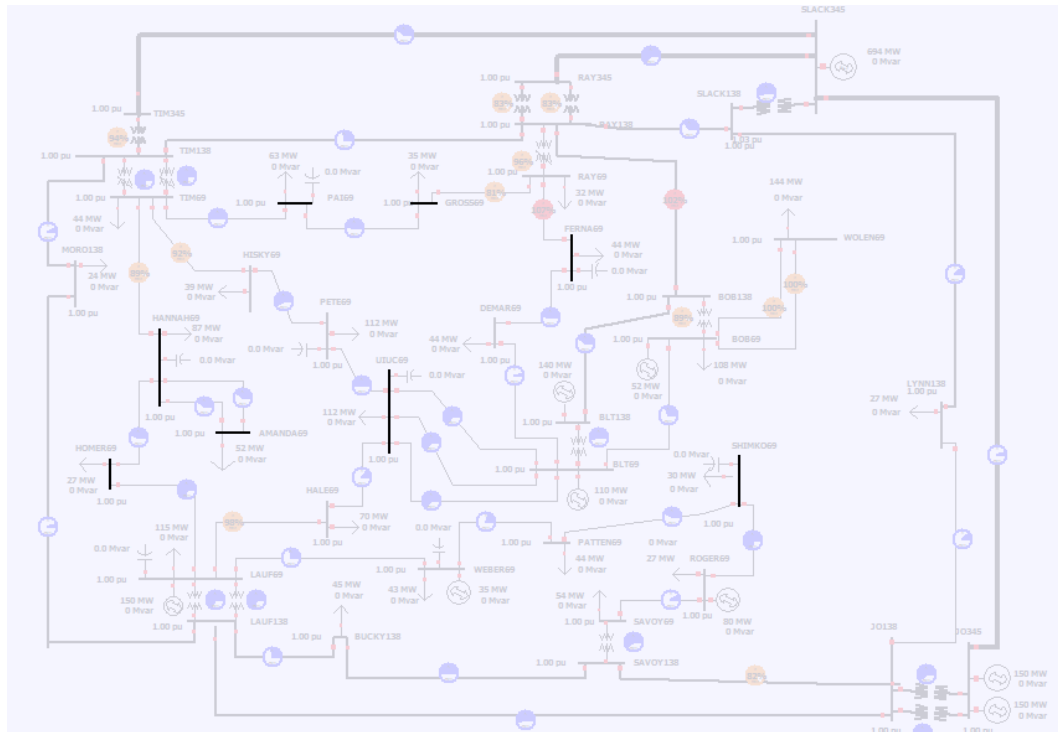
## 37 Bus System Oneline Diagram



# Case Study:

## 37 Bus Study Parameters

- Controllable generation capacity: 1828 MW
- Load: 1544 MW



# Case Study:

## 37 Bus - High Forecast Error

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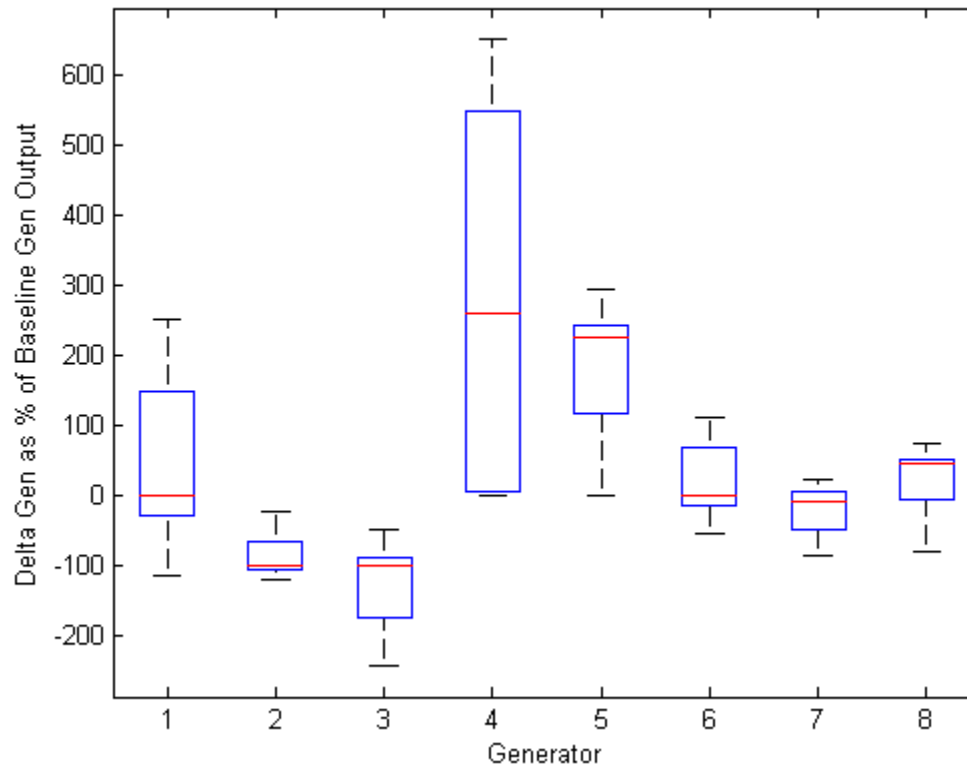
- Forecast: 55 MW
- Forecast error: +5/-50 MW
- Solution found with GUROBI in 10 seconds
- Maximum line overload is 6.65%
- Worst case wind error: [-50, +5, -50, -50, -50, +5, -50, -50]
  - Optimal re-dispatch: [+20, -166, +350, +87, -30, +46, -81, +63]

# Case Study:

## 37 Bus – Variation in Participation Factors

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- Tested boundary points from high forecast error (55 MW, +5 MW/-50 MW) set of data



# Case Study:

## 37 Bus - Low Forecast Error

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- Forecast: 15 MW
- Forecast Error: +10/-15 MW
- Solution found with GUROBI in 4 seconds
- Sum of overloads: 0%
- Maximum line overload: 0%
- Sample re-dispatch: [-19, -174, +59, +87, +30, +46, 0, +40]

# Extensions

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- Inclusion of commitment as decision variable
- Clearly show the tradeoff between the confidence level used to bound the forecast error & the maximal loading
- Use ramp up/down instead of line loading—should indicate where reserves are critical
- Extension to correlated forecast errors

# Closing Remarks

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- Developing new tools that help operators understand existing and potential system conditions should be a top priority, since they are ultimately responsible for maintaining a reliable electricity supply
- Thank you

...and special thanks to Xiaoguang Li, the M.A.Sc. student who's been working with me on this research.

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