Improving Economic Dispatch through Transmission Switching: New Opportunities for a Smart Grid

Kory Hedman and Shmuel Oren University of California, Berkeley (Based on joint work with Richard O'Neill, Emily Fisher and Michael Ferris)

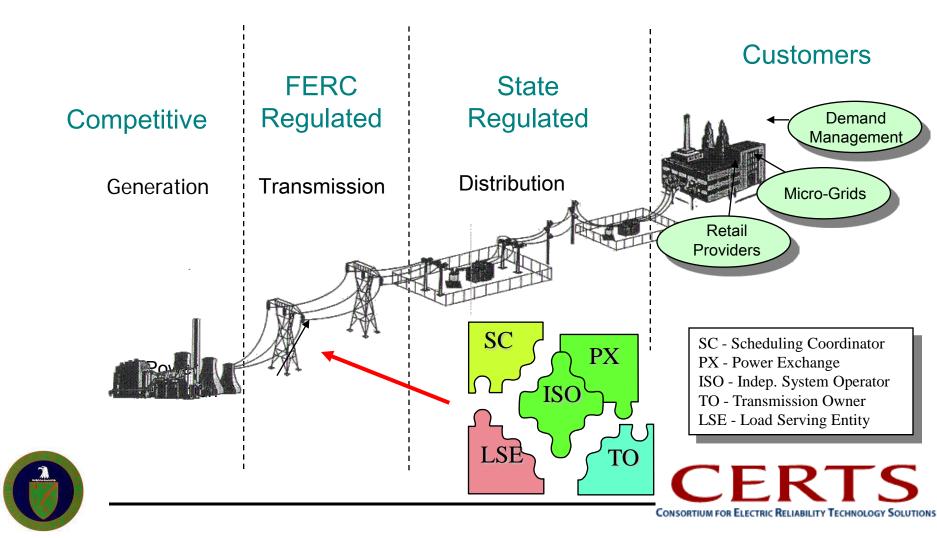
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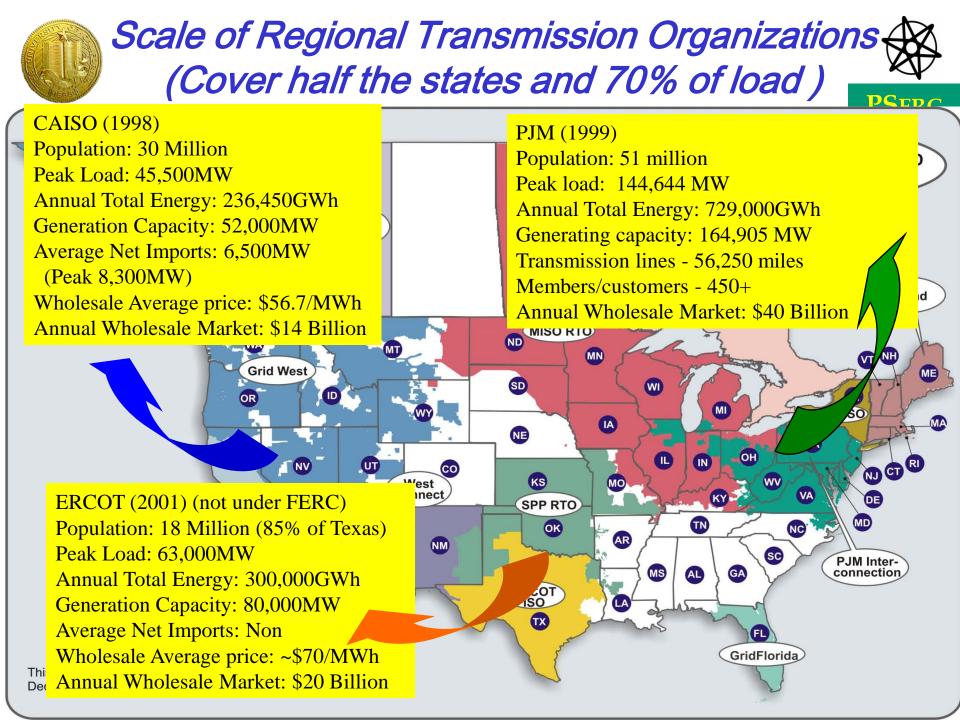
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POWER INDUSTRY RESTRUCTURING

**PSERC** 







# Market Mechanics at PJM



Day-Ahead Market closes



Day-ahead Results Posted & Balancing Market Bid period opens

# $\begin{array}{c} 11 \\ 10 \\ 9 \\ 8 \\ 7 \\ 6 \\ 5 \\ \end{array}$

Balancing (RT) Market Bid period closes



#### Reserve Adequacy Assessment

- focus is reliability
- updated unit offers and availability
- Based on PJM load forecast
- minimizes startup and cost to run units at minimum

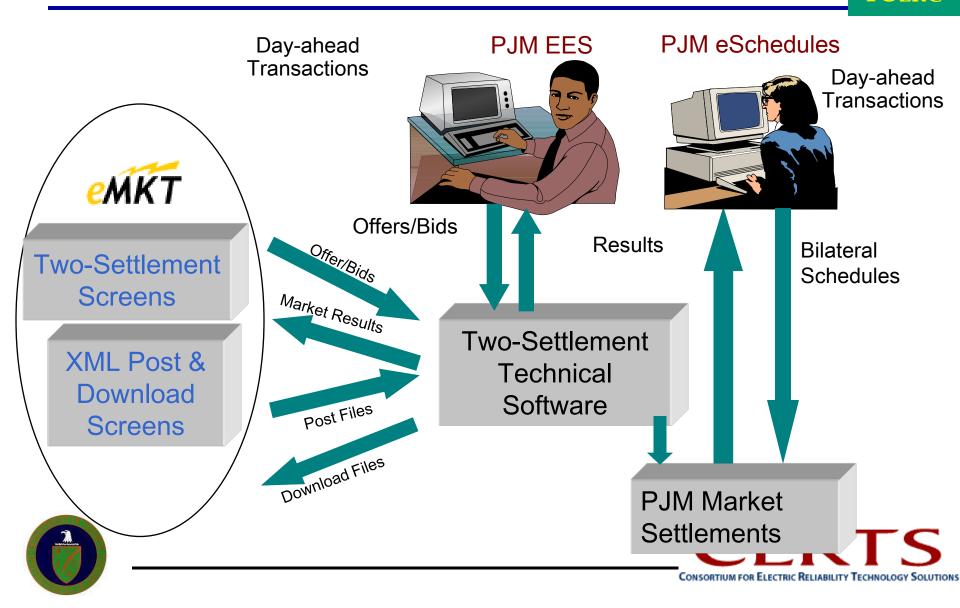


#### Day-ahead Market

 determines commitment profile that satisfies fixed demand, price sensitive demand bids, virtual bids and PJM Operating Reserve Objectives
minimizes total production









- Generation Unit Commitment
- Optimal Power Flow (OPF) Problems
  - Alternating Current Optimal Power Flow (ACOPF)
  - Direct Current OPF (DCOPF) Linearization of the ACOPF
- Reliability (Contingency) Requirements N-1 Standards
  - N-1 DCOPF, Security Constrained ACOPF







Power Flow Optimization (every five minutes) and Locational Marginal Pricing (LMP)



- General Statement of OPF
  - Objective <mark>f</mark>:
    - Vertical demand: *MIN* Cost =  $\Sigma$  Generator Costs
    - Elastic demand: MAX Net Benefits
      - = Σ (Consumer Value Generator Cost)
  - Decision variables X:
    - Generation
    - Accepted demand bids
    - Operating reserves
    - Real and reactive power flows
  - Constraints
    - Generator limits (including dynamic limits such as ramp rates)
    - Demand (net supply = load L at each bus for P,Q)
    - Load flow constraints (e.g., KCL, KVL)
    - Transmission limits
    - Reserve requirements
- Price of energy (LMP) at bus i = Marginal cost of energy at bus
  - Most readily calculated as dual variable to energy balance (KCL) constraint for the bus in an Optimal Power Flow (OPF)

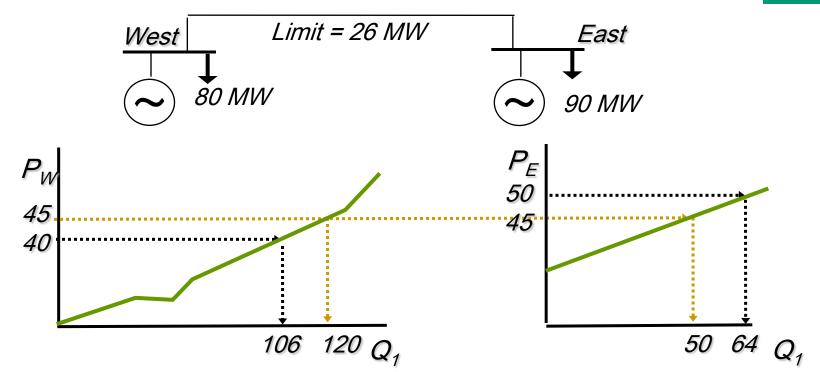






## LMP / Congestion Example





Marginal value of transmission = 10/MWh (=50 - 40) Total congestion revenue =  $10^{26} = 260/hr$ Total redispatch cost = 130/hrCongestion cost to consumers: ( $40^{106}+50^{64}$ ) – ( $45^{170}$ ) = 7440 - 7650 = -210/hr

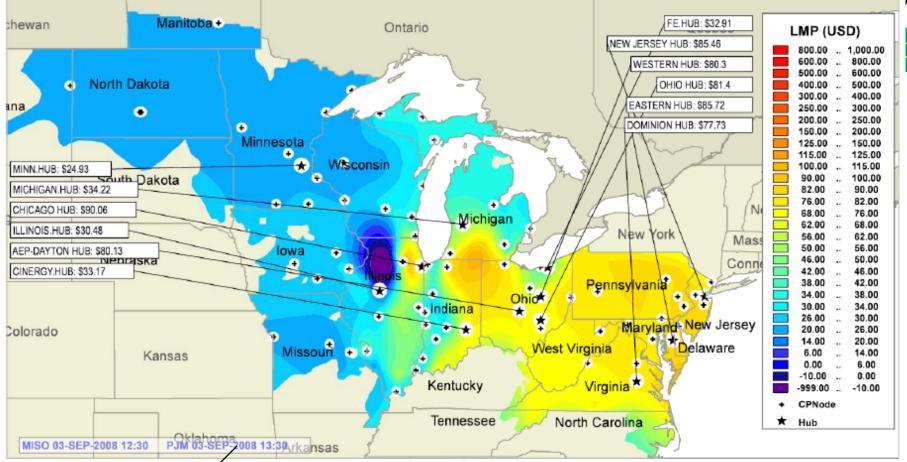




#### Locational Real Time Marginal Prices at PJM and MISO service 11 State



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Midwest ISO Market data is based on Eastern Standard Time (EST) while PJM Market data is based on Eastern Prevailing Time.



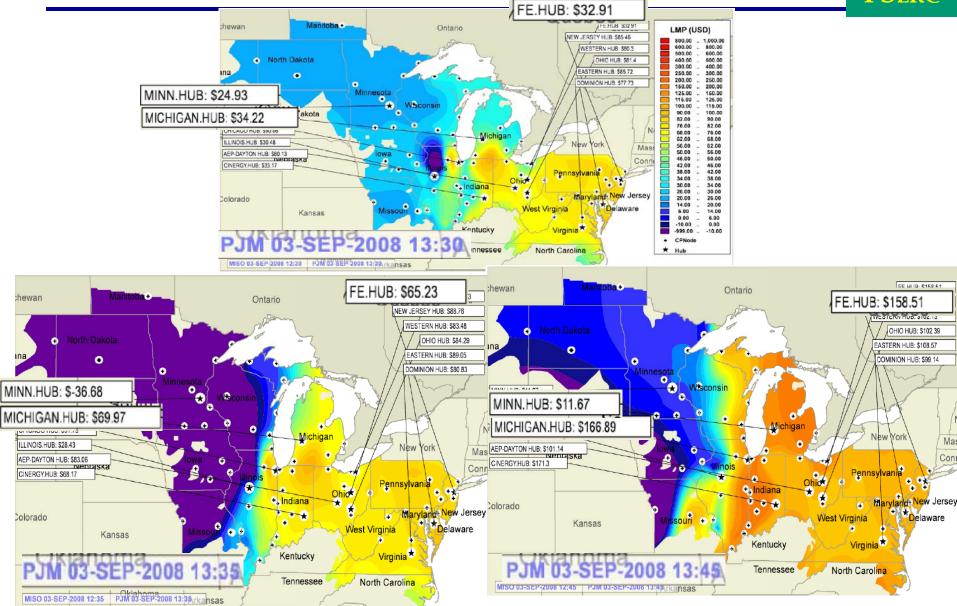
anuror PJM Interconnection. All rights reserved.





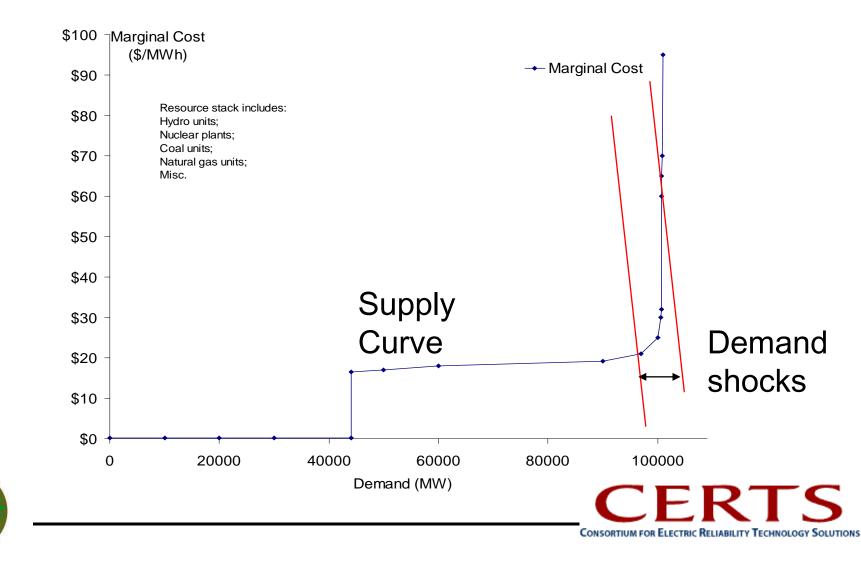
# Dispatch is reoptimized every five minutes and LMP updated to reflect shadow prices on transmission constraints















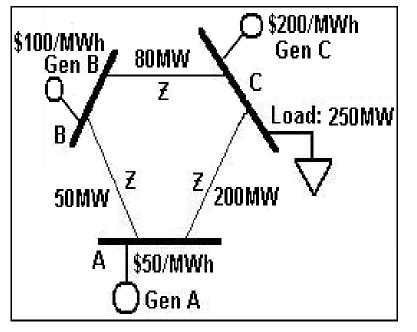


$$-50 \le \frac{1}{3}Gen_A - \frac{1}{3}Gen_B \le 50$$

$$-80 \le \frac{1}{3}Gen_A + \frac{2}{3}Gen_B \le 80$$

Line A-C:

$$-200 \le \frac{2}{3}Gen_A + \frac{1}{3}Gen_B \le 200$$





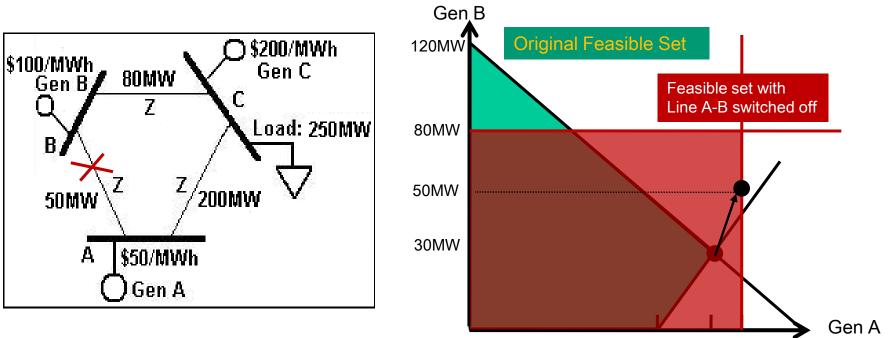






> Original Optimal Cost: \$20,000 (A=180MW,B=30MW, C=40MW)

Open Line A-B, Optimal Cost: \$15,000 (A=200MW, B=50MW)



150MW 180MW 200MW

CONSORTIUM FOR ELECTRIC RELIABILITY TECHNOLOGY SOLUTIONS









- Transmission planning addresses long term problem and a broad range of contingencies so the grid is built with redundancies that may not be needed in every state of the system
- Network redundancies motivated by reliability requirements may constrain generation dispatch create congestion and reduce economic efficiency
- Transmission assets are currently seen as static in the short term and control of transmission assets for economic reasons is underutilized
- Security constrained economic dispatch can be improved and congestion reduced through co-optimization of generation dispatch and the network active topology while ensuring reliability
- With appropriate Smart Grid switching technology, some backup transmission can be kept offline (just in time N-1)









- Currently operators change transmission assets' states on ad-hoc basis (e.g. PJM)
- National Directives:
  - FERC Order 890
    - Improve the economic operations of the electric transmission grid
  - Energy Policy Act of 2005
    - SEC.1223.a.5 of the US Energy Policy Act of 2005
    - "encourage... deployment of advanced transmission technologies"
    - "optimized transmission line configuration"
  - Energy Independence and Security Act of 2007
    - Title 13, Smart Grid:
    - "increased use of ... controls technology to improve reliability, stability, and efficiency of the grid"
    - "dynamic optimization of grid operations and resources"











- Co-optimize transmission topology and generation dispatch
- Efficiency improvements with no reliability degradation
- Smart grid application by exploiting short term reconfiguration flexibility
- Asses cost of achieving reliability through network redundancy (e.g. N-1 criterion)
- Explore options and lay foundation for new reliability concepts (just in time N-1)
- Explore market implications of dynamic transmission switching and impact on transmission rights
- Proof of concept: IEEE 118, IEEE 73 (RTS 96), ISO-NE 5000 bus model











- "Corrective Switching"
  - Changes the topology after the network optimization problem is complete to relieve constraints violations
  - Feasibility, search problems
- [Mazi, Wollenberg, Hesse 1986]: Corrective control of power systems flows (line overloads)
- [Schnyder, Glavitsch 1990]: Security enhancement using an optimal switching power flow
- [Glavitsch 1993]: Power system security enhanced by post-contingency switching and rescheduling
- [Shao, Vittal 2006]: Corrective switching algorithm for relieving overloads and voltage violations









Literature Review cont'd

After the fact switching to reduce losses

- Does not incorporate transmission switching into the overall OPF problem
- Changes topology to reduce losses after dispatch solution is known
- [Bacher, Glavitsch 1988]: Loss reduction by network switching
- [Fliscounakis, Zaoui, et al. 2007]: Topology influence on loss reduction as a mixed integer linear program









# Literature Review cont'd

#### > Optimal Switching to Relieve Congestion

- Similar MIP formulation
- Aims at relieving congestion rather than co-optimizing network topology and generation
- [Granelli, Montagna, et al. 2006]: Optimal network reconfiguration for congestion management by deterministic and genetic algorithms











### Variables:

 $P_{nmk}(Q_{nmk})$ : real (reactive) power flow through transmission line *k* connecting buses *m* and *n* 

- $P_{ng}$ : Generator g supply at bus n
- $V_n$ : Voltage magnitude at bus n
- $\theta_n$ : Bus voltage angle at bus n
- z<sub>k</sub>: Transmission line status (1 closed, 0 open)

## Parameters:

- $B_k$ : Susceptance of transmission line k
- $P_{nd}$ : Real power load at bus n











> AC Line Flow Equations (Kirchhoff's laws):

$$P_{nmk} = G_k V_n V_m \cos(\theta_n - \theta_m) + B_k V_n V_m \sin(\theta_n - \theta_m)$$

$$Q_{nmk} = G_k V_n V_m \sin(\theta_n - \theta_m) - B_k V_n V_m \cos(\theta_n - \theta_m).$$

- Non-convex constraints
- Linearization of the ACOPF to get DCOPF
- DCOPF used in Academia & Industry
- > DC Line Flow Equation:

$$B_k(\theta_n - \theta_m) - P_{nmk} = 0$$



(Alternative representation uses PTDFs)



# Optimal Transmission Switching with DCOPF

- > Z<sub>k</sub>: Binary variable
  - State of transmission line (0 open, 1 closed)

## Update line min/max thermal constraints:

- Original:  $P_k^{\min} \leq P_{nmk} \leq P_k^{\max}$ 

- New:

$$P_k^{\min} z_k \le P_{nmk} \le P_k^{\max} z_k$$

Update line flow constraints:

- Original:  $B_k(\theta_n \theta_m) P_{nmk} = 0$
- New:

$$B_k(\theta_n - \theta_m) - P_{nmk} + (1 - z_k)M_k \ge 0$$

$$B_k(\theta_n - \theta_m) - P_{nmk} - (1 - z_k)M_k \le 0$$

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$$\begin{array}{l} \text{Minimize: } \mathrm{TC} = \sum_{g} c_{ng} P_{ng} \\ \text{s.t.:} \\ \text{Bus angle constraints} & \text{Generator constraints} \\ \theta_{n}^{\min} \leq \theta_{n} \leq \theta_{n}^{\max}, \ \forall n & 0 \leq P_{ng} \leq P_{g}^{\max}, \ \forall g \\ \text{Node balance constraints} \\ \sum_{\substack{\sum P_{ijk} = -\sum_{\forall ij \neq n} P_{ijk} + \sum_{\forall g \mid s = n} P_{ig} - P_{nd} = 0, \forall n \\ \text{Transmission constraints} \\ P_{k}^{\min} z_{k} \leq P_{nmk} \leq P_{k}^{\max} z_{k}, \ \forall k \\ B_{k}(\theta_{n} - \theta_{m}) - P_{nmk} + (1 - z_{k})M_{k} \geq 0, \ \forall k \\ B_{k}(\theta_{n} - \theta_{m}) - P_{nmk} - (1 - z_{k})M_{k} \leq 0, \ \forall k \\ z_{k} \in \{0,1\}, \ \forall k \in K \end{array}$$









## IEEE 118 Bus Model:

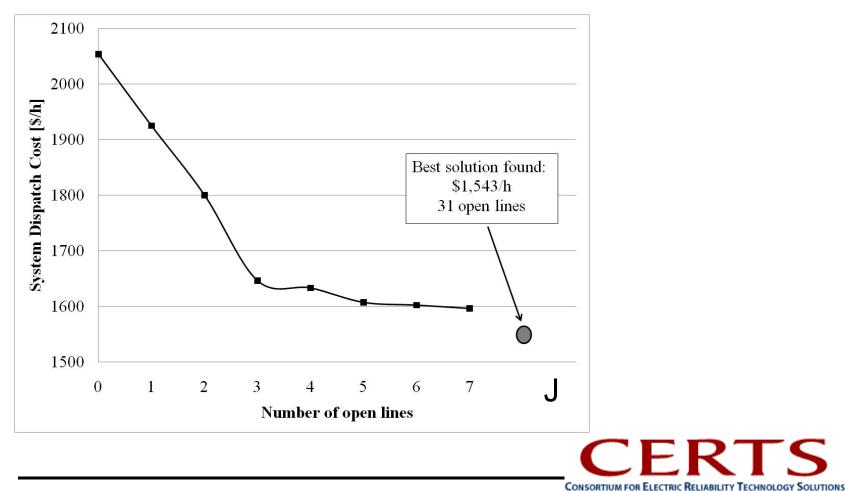
- DCOPF transmission switching solution with no contingencies saves 25% of total generation cost (10 lines switched off)
- Up to 16% savings with N-1 DCOPF transmission switching (for feasible solutions)
- IEEE 73 (RTS 96) Bus Model
  - Up to 8% savings with N-1 DCOPF transmission switching (for feasible solutions)







# Transmission switching solution saves 25% of total generation cost

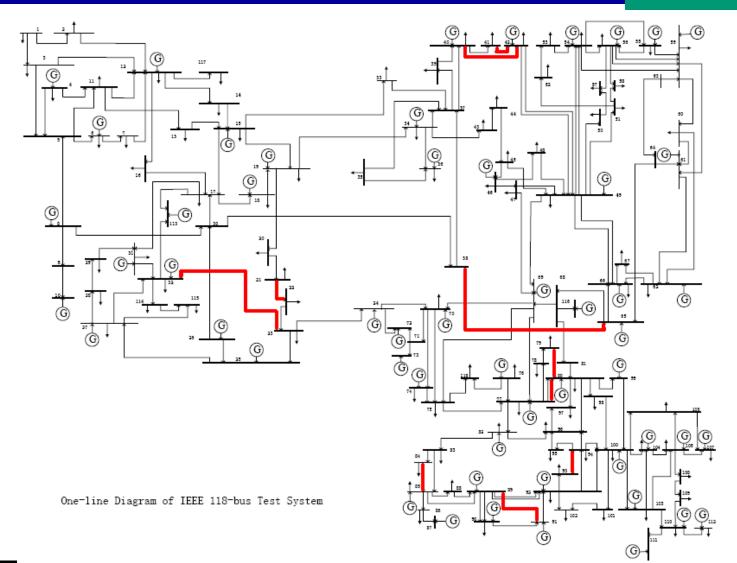






IEEE 118 opened lines for J=10

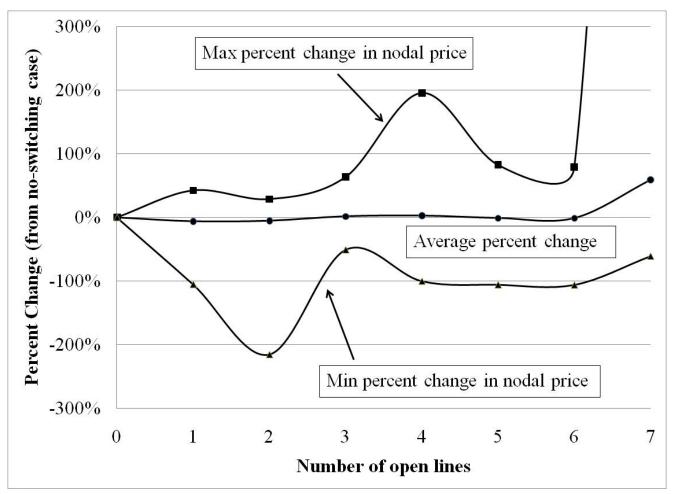
 Note: this diagram has additional gens than our model





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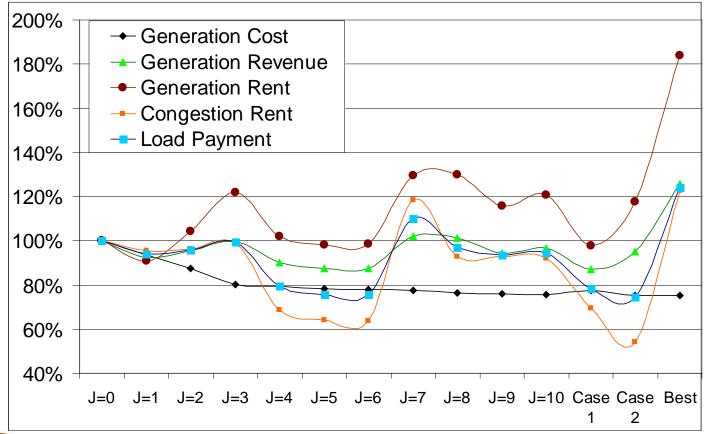








#### Results are % of static network's DCOPF solution







## Optimal Transmission Switching with N-1 DCOPF



$$\begin{array}{ll} \text{Minimize: } \mathrm{TC} = \sum_{g} c_{ng0} P_{ng0} \\ \text{s.t.:} \\ \text{Bus angle constraints} & \text{Generator constraints for each state} \\ \theta_{n0}^{\min} \leq \theta_{nc} \leq \theta_{n0}^{\max}, \ \forall n, c & 0 \leq P_{ngc} \leq P_{g0}^{\max} N \mathbf{l}_{gc}, \ \forall g, c. \\ \text{Node balance constraints} \\ \sum_{\forall k \not \models n} P_{ijkc} - \sum_{\forall k \not j \models n} P_{ijkc} + \sum_{\forall g \not \models n} P_{sg0} - P_{nd} = \mathbf{0}, \ \forall n, c = \mathbf{0}, \\ \text{transmission contingency states } c \\ \sum_{\forall k \not \models n} P_{ijkc} - \sum_{\forall k \not j \models n} P_{ijkc} + \sum_{\forall g \not \models n} P_{sg0} - P_{nd} = \mathbf{0}, \ \forall n, c = \mathbf{0}, \\ \text{transmission constraints for each state} \\ P_{kc}^{\min} z_k N \mathbf{1}_{kc} \leq P_{nmkc} \leq P_{kc}^{\max} z_k N \mathbf{1}_{kc}, \ \forall k, c \\ B_k(\theta_{nc} - \theta_{mc}) - P_{nmkc} + (2 - z_k - N \mathbf{1}_{kc}) M_{kc} \geq 0, \quad \forall k, c \\ B_k(\theta_{nc} - \theta_{mc}) - P_{nmkc} - (2 - z_k - N \mathbf{1}_{kc}) M_{kc} \leq 0, \quad \forall k, c \\ z_k \in \{0,1\}, \ \forall k \in K \qquad N \mathbf{1}_{sc} = \begin{cases} 0, \text{if } c = e \\ \mathbf{1}, \text{ otherwise} \end{cases}, \ \forall c > \mathbf{0}, e \end{cases}$$







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- Incorporation of N-1 reliability constraints:
- *N1<sub>ec</sub>*: N-1 binary *parameter* specifying what element *e* (transmission or generator) in the network is offline for state *c*

*c*=0 steadystate
operations

c>0
contingency
state

$$\mathcal{M}_{ec} = \begin{cases} \mathbf{0}, \text{ if } c = e \\ \mathbf{1}, \text{ otherwise} \end{cases}, \quad \forall c > \mathbf{0}, e^{-1} (13) \\ \sum_{\substack{c \geq \mathbf{0} \\ \forall c \geq \mathbf{0}}} \mathcal{M}_{ec} = N - \mathbf{1}, \quad \forall c \geq \mathbf{0} \qquad (14) \end{cases}$$









- Transmission contingencies:
  - Thermal ratings are set at emergency ratings
  - Generator dispatch is unchanged
- > Generation contingencies:
  - No ramp rate modeling of generators
  - Assume possible full redispatch of online generators
  - Thermal ratings are set at emergency ratings
- Determine modified N-1 contingency lists for test cases

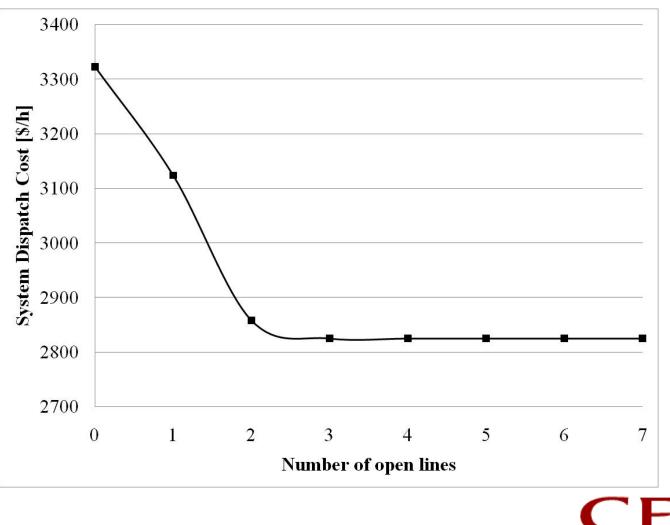














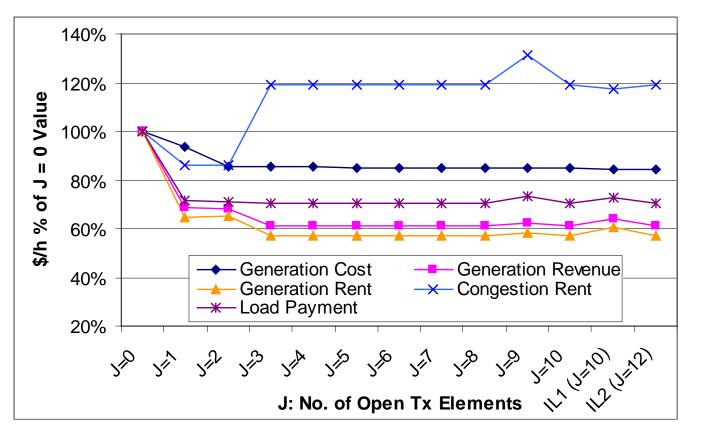
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#### Results are % of static network's N-1 DCOPF solution

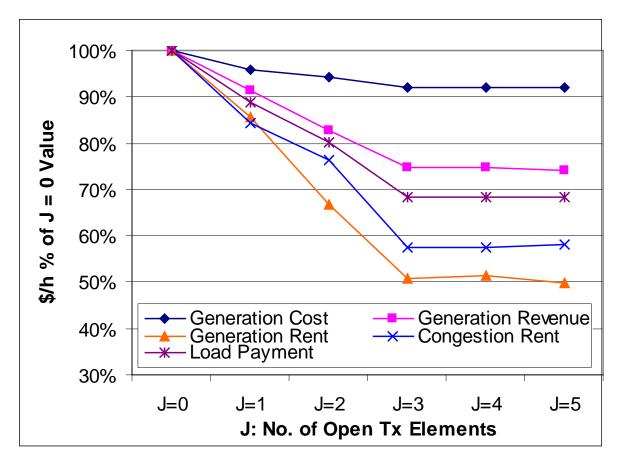








Results are % of static network's N-1 DCOPF solution







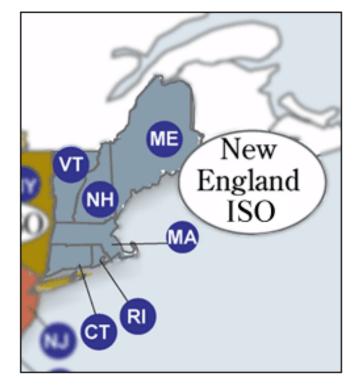






# ➢ISO-NE 5000 bus model

- 5% to 13% savings of \$600,000 total cost for NEPOOL for one hour (feasible solutions)
- Does not include reliability constraints

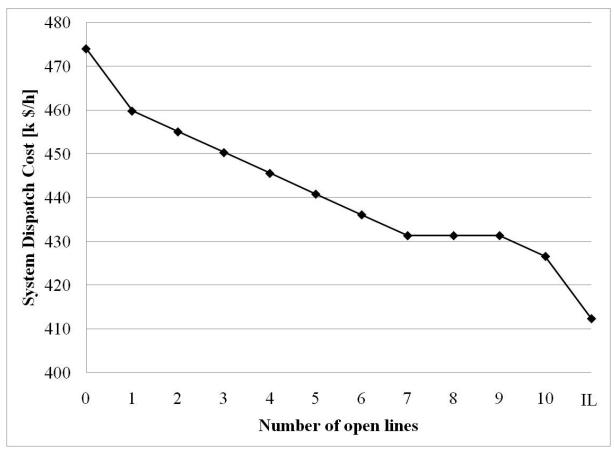








#### ISONE – Summer Peak Model (5000 bus network)



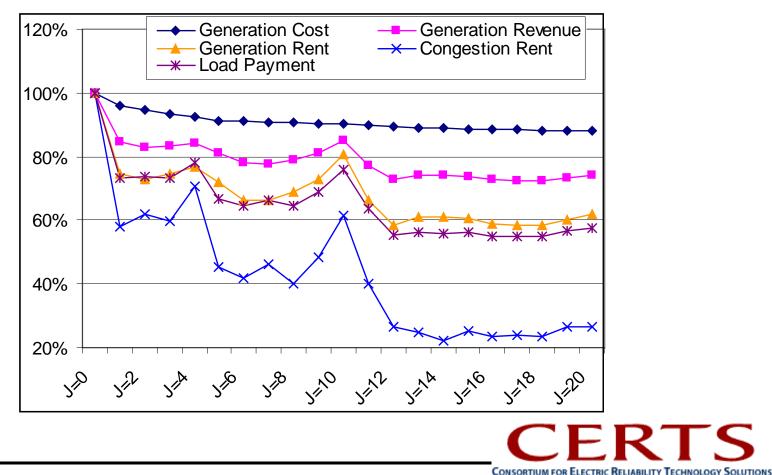








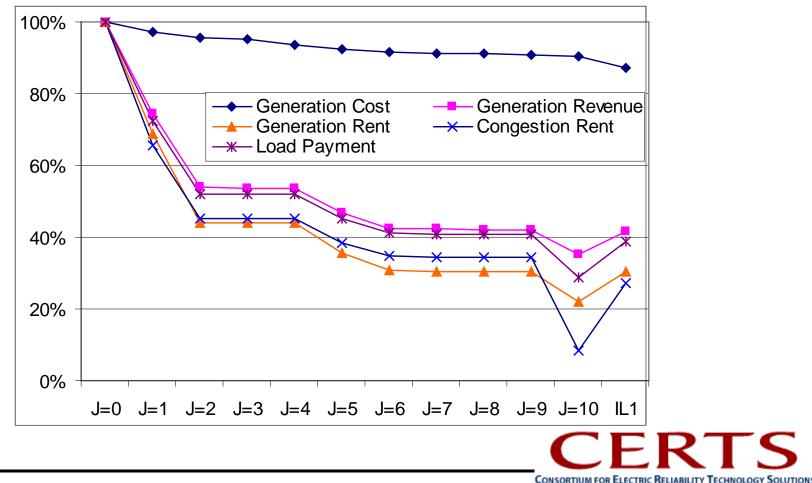
## Results are % of static network's DCOPF solution ISONE – Summer Peak Model







- Results are % of static network's DCOPF solution
- ISONE Connecticut Import Study Model











- Generation Unit Commitment Multi-Period Model
  - Startup costs
  - Shutdown costs
  - Minimum up and down time constraints
    - Facet defining valid inequalities
  - No ramp rate constraints
- Transmission Switching
- N-1 Contingency Constraints







Generation Unit Commitment Nomenclature



#### > Variables:

- >  $u_{gt}$ : Unit commitment variable (1 generator online, 0 generator offline)
- v<sub>gt</sub>: Startup variable (1 generator turned on in period t, 0 otherwise)
- *w<sub>gt</sub>*: Shutdown variable (1 generator turned off in period *t*, 0 otherwise)

#### Parameters:

- >  $SU_g$ : Startup cost, generator g
- >  $SD_g$ : Shutdown cost, generator g
- $\succ UT_g$ : Minimum up time, generator g
- $\rightarrow DT_g$ : Minimum down time, generator g







### Multi-Period Formulation



Objective &
Power Flow
Constraints:

$$\begin{aligned} \text{Minimize:} & \sum_{t} \sum_{g} \left( c_{g} P_{ng0t} + SU_{g} v_{gt} + SD_{g} w_{gt} \right) \end{aligned} (1) \\ & \text{s.t.} \\ \theta^{\min} \leq \theta_{nct} \leq \theta^{\max}, \ \forall n, c, t \end{aligned} (2) \\ & \sum_{\forall k \mid t=n} P_{ijkct} - \sum_{\forall k \mid j=n} P_{ijkct} + \sum_{\forall g \mid s=n} P_{sg0t} - P_{ndt} = 0, \\ & \forall n, c = 0, \text{ transmission contingency states } c, t \end{aligned} (3a) \\ & \sum_{\forall k \mid t=n} P_{ijkct} - \sum_{\forall k \mid j=n} P_{ijkct} + \sum_{\forall g \mid s=n} P_{sgct} - P_{ndt} = 0, \\ & \forall n, \text{ generator contingency states } c, t \end{aligned} (3b) \\ & P_{kc}^{\min} z_{kt} N1_{kc} \leq P_{nmkct} \leq P_{kc}^{\max} z_{kt} N1_{kc}, \forall k, c, t \end{aligned} (4) \\ & B_{k}(\theta_{nct} - \theta_{mct}) - P_{nmkct} + (2 - z_{kt} - N1_{kc})M_{k} \geq 0, \\ & \forall k, c, t \end{aligned} (5a) \\ & B_{k}(\theta_{nct} - \theta_{mct}) - P_{nmkct} - (2 - z_{kt} - N1_{kc})M_{k} \leq 0, \\ & \forall k, c, t \end{aligned} (5b)$$







Generation Unit Commitment Constraints:

$$\begin{split} & P_{g}^{\min} N 1_{gc} u_{gt} \leq P_{ngct} \leq P_{g}^{\max} N 1_{gc} u_{gt}, \ \forall g, c, t \quad (6) \\ & v_{g,t} - w_{g,t} = u_{g,t} - u_{g,t-1}, \ \forall g, t \qquad (7) \\ & \sum_{q=t-UT_{g}+1}^{t} v_{g,q} \leq u_{g,t}, \ \forall g, t \in \{UT_{g}, .., T\} \qquad (8) \\ & \sum_{q=t-DT_{g}+1}^{t} w_{g,q} \leq 1 - u_{g,t}, \ \forall g, t \in \{DT_{g}, .., T\} \qquad (9) \\ & 0 \leq v_{g,t} \leq 1, \ \forall g, t \qquad (10) \\ & 0 \leq w_{g,t} \leq 1, \ \forall g, t \qquad (11) \\ & u_{g,t} \in \{0,1\}, \ \forall g, t . \qquad (12) \end{split}$$





Results – 24HR Gen UC & Optimal Transmission Switching N-1 DCOPF



- Model: IEEE RTS-96 system
- Results show:
  - Optimal network topology varies from hour to hour
  - Changing the network topology can change the optimal generation unit commitment solution
  - Total startup costs may be reduced
  - Peaker units initially required with original topology were not required once transmission switching was incorporated into the problem
- 3.7% overall savings or over \$120,000 (24hr) for this medium sized IEEE test case – can translate into millions for large scale networks for entire year











# IEEE 118 DCOPF & N-1 DCOPF variables & constraints:

IEEE 118	DCOPF		N-1 DCOPF	
	LP	MIP	LP	MIP
Total Variables:	323	509	63k	63k
Binary Variables:	0	186	0	186
Total Linear Constraints:	628	1000	126k	202k
Total Variables (Post Presolve):	315	492	60k	61k
Binary Variables (Post Presolve):	0	177	0	97
Linear Constraints (Post Presolve):	482	833	98k	137k









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Computational Statistics cont'd

#### ISONE (DCOPF)

- To solve for best 2 lines to open, optimality not reached after 50 hours
- Used heuristic of finding next best line to open

ISONE Summer Peak Model	LP	MIP
Total Variables:	12,237	18,889
Binary Variables:	0	6,652
Total Linear Constraints:	23,786	37,090
Upper or Lower Bound Constraints:	12,237	18,889
Total Variables (Post Presolve):	11,101	16,701
Binary Variables (Post Presolve):	0	5,600
Linear Constraints (Post Presolve):	17,063	27,441





Revenue Adequacy in Financial Transmission Rights Market



- FTRs: Hedging mechanism
- Market operator compensates FTR owners with congestion rent (surplus)
- Revenue adequacy not guaranteed if topology changes [Alsac, Bright, et al. 2004]
- Following example illustrate potential congestion revenue shortfall due to tran.smission switching

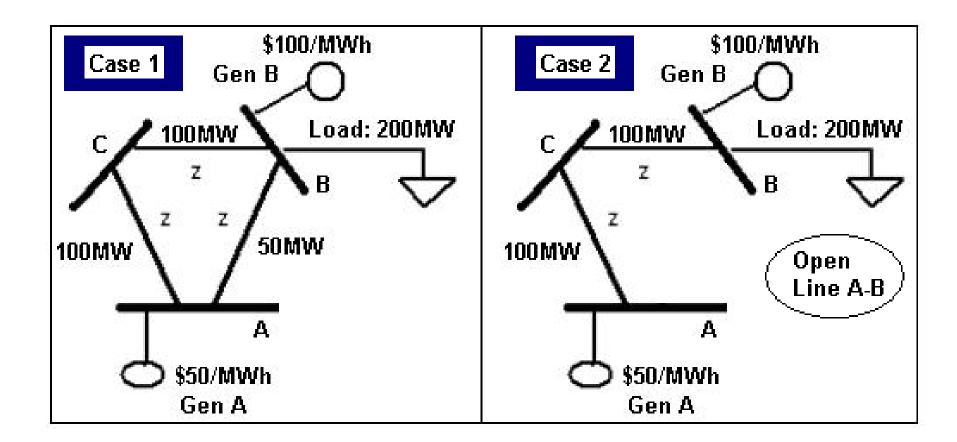






### Revenue Adequacy of FTR s: Example











**Revenue Adequacy of FTRs Cont'd** 



#### Without Switching Line A-B In (Case 1):

BUS:	Gen Pg:	LMP:	Gen Cost:	BRANCH:	Line Flow:	Congestion Rent:
А	75MW	\$50/MWh	\$3,750	From A to B	50MW	\$2,500
В	125MW	\$100/MWh	\$12,500	From A to C	25MW	\$625
С	0MW	\$75/MWh	\$0	From B to C	-25MW	\$625
Total Gen Cost:		<mark>\$16,250</mark>	Total Congestion Rent:		\$3750	

#### With Switching Line A-B Out (Case 2):

BUS	Gen Pg:	LMP:	Gen Cost:	BRANCH:	Line Flow:	Congestion Rent:
A	100MW	\$50/MWh	\$5,000	From A to B	0MW	\$0
В	100MW	\$100/MWh	\$10,000	From A to C	100MW	\$5,000
С	0MW	\$100/MWh	\$0	From B to C	-100MW	\$0
	To	tal Gen Cost:	<mark>\$15,000</mark>	Total Cong	estion Rent:	<mark>\$5,000</mark>









Lines:	FTR Quantity:	FTR Payment Without Switching (Case 1)	FTR Payment With Switching (Case 2)
From A to B	50MW	\$2,500 (LMP gap: \$50/MWh)	\$2,500 (LMP gap: \$50/MWh)
From A to C	100MW	\$2,500 (LMP gap: \$25/MWh)	\$5,000 (LMP gap: \$50/MWh)
From B to C	50MW	-\$1,250 (LMP gap: -\$25/MWh)	\$0 (LMP gap: \$0/MWh)
<b>Total FTR Payments:</b>		\$3,750	\$7,500 (>\$5,000)

Total generation cost decreases but we can create FTR holdings that result in revenue inadequacy for the switching solution. We have revenue adequacy with the no switching solution (case 1) but we do not have it with the switching solution (case 2) even though it increases social welfare.











- Revenue adequacy and FTR settlement
  - Incorporate revenue adequacy feasibility test within transmission switching formulation
  - Do we need a compensation scheme to offset the impact on FTR settlements?
- Benders' decomposition
  - Analyze various sub-problem formats
  - Research techniques to improve solution time
    - Combinatorial cuts
    - Local branching
- Use AC OPF for short term (e.g. hourly) switching problem
  - MINLP very difficult
  - Research heuristic techniques







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## QUESTIONS? Thank you!

http://www.ieor.berkeley.edu/~oren/index.htm

Sector Contraction